

Spectral Analysis and Mapping of Blackgrass Weed by Leveraging Machine Learning and UAV Multispectral Imagery

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Abstract

Accurate weed mapping is a prerequisite for site-specific weed management to enable sustainable agriculture. This work aims to analyse (spectrally) and mapping blackgrass weed in wheat fields by integrating Unmanned Aerial Vehicle (UAV), multispectral imagery and machine learning techniques. 18 widely-used Spectral Indices (SIs) are generated from 5 raw spectral bands. Then various feature selection algorithms are adopted to improve model simplicity and empirical interpretability. Random Forest classifier with Bayesian hyperparameter optimization is preferred as the classification algorithm. Image spatial information is also incorporated into the classification map by Guided Filter. The developed framework is illustrated with an experimentation case in a naturally blackgrass infected wheat field in Nottinghamshire, United Kingdom, where multispectral images were captured by RedEdge on-board DJI S-1000 at an altitude of 20m with a ground spatial resolution of 1.16 cm/pixel. Experimental results show that: (i) a good result (an average precision, recall and accuracy of 93.8%, 93.8%, 93.0%) is achieved by the developed system; (ii) the most discriminating SI is triangular greenness index (TGI) composed of Green-NIR, while wrapper feature selection can not only reduce feature number but also achieve a better result than using all 23 features; (iii) spatial information from Guided filter also helps improve the classification performance and reduce noises.

Keywords: Blackgrass weed; Guided filter; Random Forest; Spectral Index (SI); Unmanned Aerial Vehicle (UAV).

1. Introduction

An increasing world population (9 billion by 2050) is placing an unprecedented demand (a 70% increase) on contemporary agriculture. This global grand challenge is even severer in consideration of the scarcity of the arable land and natural farming resources, and the societal demand for shrinking agriculture's environmental footprint [1]. Weeds, aggressively competing with crops for water, nutrients and sunlight, are responsible for an approximate 35% reduction in potential global crop yields [2]. Improved weed monitoring can help reduce agricultural use of chemicals

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16 (herbicides in particular) and thus contribute to an increased agriculture sustainability.

17 Various weed management strategies are developed in the literature and practice according to various weed growth
18 stages. Pre-sowing or pre-emergence herbicides can be applied before the emergence of weeds. Post-emergence herbi-
19 cides, tillage, hand weeding and weed surfacing are common practices after weeds' emergence. However, conventional
20 weed management strategies are to broadcast over the entire field irrespective of weeds' spatial information. This uni-
21 form strategy results in economical (a high cost due to overdose), environmental (severer ground water contamination)
22 and social (herbicide residues in agriculture products) risks, and also exacerbates the problem of herbicide resistance,
23 since weeds are usually patchily distributed within fields leading to many weed-free areas [3].

24 To tackle these challenges, there is a trend to adopt Site-Specific Weed Management (SSWM) strategy according
25 to weed spatial distribution [4]. In this approach, weed mapping at early stages is desirable for timely herbicide
26 applications. However, many challenges still exist in early (seedling) weed mapping due to various reasons including
27 the similarity of spectral reflectance [2]. Therefore, late-season weed mapping, although not common yet, may provide
28 an alternative in practice. This is because for certain weeds (e.g. blackgrass) weed infestation is relatively stable from
29 year to year [5], as a result, late-season weed mapping can be used for the treatment of the subsequent year by using
30 pre-sowing or pre-emergence herbicides. Weed mapping also plays a vital role in assessing the effectiveness of various
31 herbicide treatments.

32 Blackgrass, an annual grass native to Eurasia, is a major weed of cereal crops in the U.K., especially for autumn sown
33 crops including winter wheat. This weed has significantly adverse effects on crop yields and is prevalent in northern
34 Europe; it is reported that about 70% of fields in the UK are infected by blackgrass [6]. To make it worse, blackgrass
35 has gradually developed herbicide resistance, especially to post-emergence herbicides. Consequently, pre-emergence
36 herbicides have become the main means of chemical control [7]. In addition, according to their effectiveness, practical
37 non-chemical control strategies of blackgrass weeds in wheat fields include spring cropping, pre-sowing plowing, delayed
38 autumn drilling, higher seed rates and competitive cultivars [7].

39 It is evident that accurate, timely and high-resolution weed maps (including blackgrass weed mapping) are key for
40 SSWM practices [3]. Weed mapping by ground sampling is expensive, time-consuming and not suitable for large-scale
41 applications [8]. Remote sensing of weed canopies is drawing increasing research interests, which is mainly enabled by
42 the rapid development of spectroscopic instruments, the advent of easily-accessed and flexible moving platforms such
43 as Unmanned Aerial Vehicle (UAV) and recent advancements in machine/deep learning algorithms. The underlying
44 rationale is that various materials (land covers) in fields (crop, weed and bare soil) usually exhibit different spectral

45 reflectance values due to their varied physical and chemical characteristics, which can be captured by spectroscopic
46 instruments and subsequently be learnt by machine learning algorithms [9], [10].

47 There are several studies on weed mapping in crop fields, where the sensors range from low-cost multispectral
48 cameras [11, 12] to high-cost spectrometers, from low to high spatial resolution, and from ground-based (harvesters,
49 tractors) [13, 14] to airborne-based [15, 16]. UAV remote sensing with a user-defined spatial-temporal resolution, a
50 low cost and high flexibility has become an important remote sensing approach [4]. For example, in [17], the problem
51 of broad-leaf and grass weed detection in wide-row herbaceous crops are considered by using UAV visible imagery and
52 neural network model. Maximum likelihood and Support Vector Machine (SVM) are compared in [18] for weed spatial
53 distribution in onion field. In [5], piloted airborne multispectral imagery (MSI) with a resolution of 25 cm/pixel is
54 adopted for cruciferous weed mapping among cereal crops by VISible-NIR (VIS-NIR) derived Spectral Indices (SIs).
55 To alleviate the problem of crop/weed spectral similarity at early growth stages, crop row spatial information is
56 exploited in [2]. Spatial (crop row) and spectral characteristics are also exploited in [19] for weed mapping in maize
57 fields by six-band MSI. Visual features and geometric information of detected vegetation are also employed to classify
58 crops and weeds in [20] by using RGB-NIR aerial image at an altitude of 3 m.

59 Recently, there is also a trend for weed mapping by deep learning approaches [13, 14, 15, 21]. For instance, the
60 problem of crop/weed semantic segmentation is considered by using images collected by agricultural robots in [13, 14].
61 Deep neural network (e.g. SegNet) was adopted in pioneering work [15, 21] for semantic weed classification from sugar
62 beet by aerial MSI collected by a small UAV at an height of 2m. It is noted, however, that a large amount of labelled
63 data is usually required in deep learning approaches for images (ideally) with a relatively high spatial resolution [22].
64 Deep learning approaches are not applied in the study considering that: (1) only a limited number of pixels are labelled
65 for the MSI due to the challenges in labelling aerial images; (2) the labelled pixels are sparsely distributed in the field
66 of interest (see, Fig 5); (3) the image resolution is far lower than the ones collected by agricultural robots or UAV at
67 a very low height [13, 14, 15], since the drone camera in this study can not be operated at a very low altitude (due to
68 the image calibration and stitching issue at an altitude lower than 10 m); (4) as described in Section 2.1, the labelling
69 approach is not suitable for deep learning approaches, either. The following observations are drawn for the research
70 in terms of research motivation, gaps and challenges:

- 71 (1) There is an urgent need for an automatic remote sensing based weed mapping to enable SSWM at field scales;
- 72 (2) In-season weed mapping is significant and possesses new research challenges over early-season mapping due to

73 the lack of crop row information in wheat fields;

- 74 (3) There are studies for weed mapping by using spectral and/or spatial information, little work is available on
75 systematically selecting appropriate SIs or their optimal combination for a simple but effective classifier;
- 76 (4) To date, the use of UAV, MSI and machine learning for blackgrass weed mapping has not yet been evaluated.

77 The main contribution of this study lies in the initial development of an automatic weed mapping framework by
78 integrating five-band MSI, low-altitude UAV platform and machine learning algorithms, and its real-life validation in
79 a naturally blackgrass infected wheat field. The specific objectives are to:

- 80 (i) Determine whether or not blackgrass weeds can be discriminated from wheat by applying spectral analysis and
81 classification algorithm to aerial MSI;
- 82 (ii) Identify the most discriminating spectral bands, SIs and their optimal combination by using feature generation
83 and selection algorithms;
- 84 (iii) Exploit both spectral and spatial information for an accurate blackgrass probabilistic map;
- 85 (iv) Initially experimentally validate the system in a naturally blackgrass infested wheat field.

86 2. Materials

87 2.1. Study field

88 Experiments were carried out in a naturally blackgrass (*Alopecurus myosuroides*) infected wheat (*Triticum aestivum* L.) field (GPS coordinate, latitude: $53^{\circ}02'45''N$, longitude: $0^{\circ}45'29''W$, altitude: 14m a.s.l.) of Newark, Nottinghamshire, U.K. (please refer to Fig 1 for the location of the test field). Data collection was done on 05/Jun/2018
90 (mid-day of a sunny day), when wheat and blackgrass weeds are in the stages of full ear emergence and early seed
91 shedding. The late-season imaging is mainly due to the significant challenges in blackgrass groundtruth labelling at an
92 early stage in UAV imagery, especially for a naturally blackgrass infected wheat field in this study. As shown in the left
93 bottom plot of Fig 1, red rope (treated as background pixels in labelling) has been used to help agronomists label the
94 aerial image after acquisition and pre-processing. This will also prohibit the application of deep learning approaches,
95 since this information will also be learnt automatically in deep learning framework. It is noted that red rope is to
96 help agronomists build the knowledge of blackgrass weed in the aerial images. Upon knowing its characteristics, a
97

GPS location: 53° 02'45.0"N, 0° 45'29.0"W

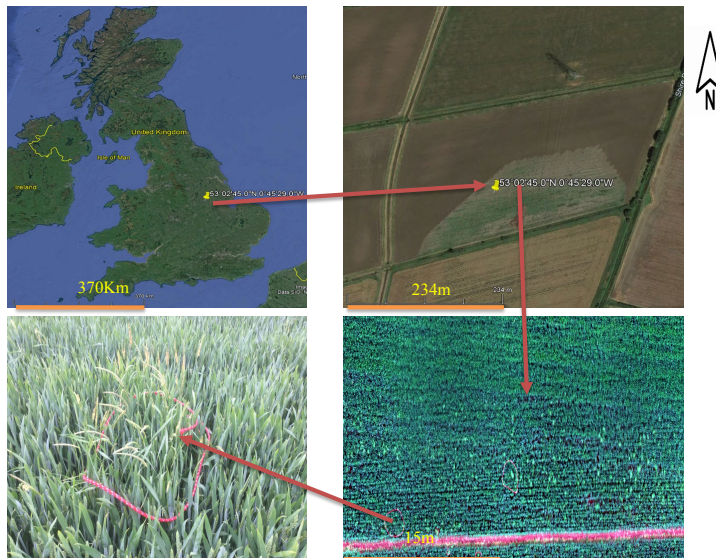


Figure 1: Test wheat field for blackgrass weed mapping including geographic location (Google earth engine), satellite image of the field of interest, false-color UAV image and ground images of blackgrass weed.

98 large number of blackgrass samples (within and beyond the red rope regions) are manually labelled for the purpose of
99 spectral analysis and model construction. It is also noted that the purple line at the bottom right of Fig 1 is a field
100 path (background pixels in labelling).

101 2.2. MSI image acquisition

102 In this study, multispectral camera is adopted for blackgrass weed mapping. This is because compared to hy-
103 perspectral camera [23], multispectral camera is lightweight, with a low cost, and of high spatial resolution and so
104 applicable to large areas of interest. While compared to RGB camera [24], multispectral camera possesses additional
105 spectral bands and is also less affected by environmental variations due to the availability of reflectance calibration
106 panel. To obtain aerial MSI, S1000 Octocopter (DJI, Shenzhen, China) and RedEdge multispectral camera (MicaS-
107 ense, Seattle, WA, USA) are adopted, where the developed system is displayed in Fig 2. The specification of DJI
108 S1000 is referred to [9, 25]. RedEdge camera is a light-weight (135g), small ($5.9\text{cm} \times 4.1\text{cm} \times 3.0\text{cm}$), high-resolution
109 (1280×960 pixels) camera, which can capture five narrow spectral bands with GPS information. The five bands
110 (wavelength/bandwidth) include Blue (475/20 nm), Green (560/20 nm), Red (668/10 nm), RedEdge (717/10 nm) and
111 NIR (840/40 nm).

112 During the flight, a gimbal is adopted to fix the camera pointing vertically downwards so that the the adverse
113 effects of UAV motion/vibration on image quality are attenuated. The flight altitude is set to 20m above ground with

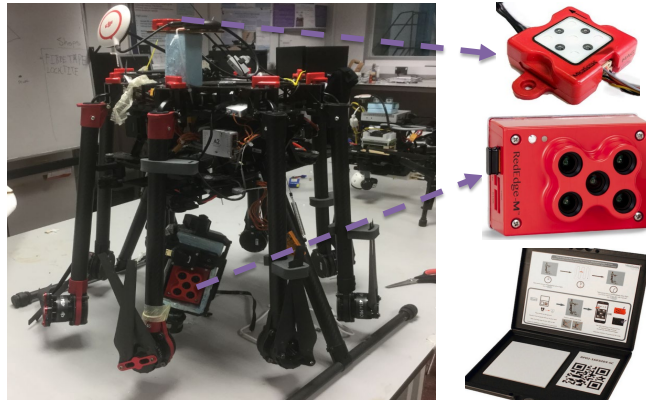


Figure 2: UAV-Camera system: DJI S1000 (left), Downwelling light sensor (top), RedEdge camera (middle) and calibration panel (bottom).

114 a ground spatial resolution of 1.16cm/pixel in the orthomosaic image. DJI Ground Station 4.0 is used to plan, control
 115 and monitor the UAV flight. The flight path, UAV forward velocity (1m/sec.) and camera triggering are set in the
 116 Pix4DCapture App to make sure that an overlap and sidelap up to 75% is guaranteed for the purpose of accurate
 117 image stitching. A total number of 460 x 5 images are obtained in the field trial, where the total covered area after
 118 image stitching is about 0.004 square km. A selected portion of the stiched image with sever blackgrass weed infection
 119 is selected for the spectral analysis and model test.

120 For image reflectance calibration, both Downwelling Light Sensor (DLS) and MicaSense’s Calibrated Reflectance
 121 Panel (CRP) are adopted. DLS is to record data on the amount of light from the sky, which is useful for situations
 122 where ambient light conditions are changing during a flight. While CRP with known reflectance values (i.e. 0.57, 0.57,
 123 0.56, 0.51 and 0.55 for Blue, Green, Red, NIR and RedEdge) is for absolute reflectance calculation. Before and after
 124 each flight, an image of the CRP is taken at about 1m without shadow, which will be used for reflectance calibration
 125 in Pix4DMapper software. Images captured with RedEdge-M conforms to standard formats (TIFF) with standard
 126 metadata such as GPS information (latitude/longitude/altitude and date/time), attitude data (pitch, roll and heading
 127 angles) and camera information (e.g. exposure time, ISO speed, black level).

128 2.3. Image preprocessing by Pix4DMapper

129 Professional photogrammetry software is then required to align the bands, calibrate the images and create georef-
 130 erenced reflectance maps, based on which various SVIs can be calculated. These tasks are conducted by Pix4DMapper
 131 software of version 4.3.31 (Pix4D SA, Switzerland), where more detailed information is referred to [25]. To make it
 132 more intuitive, the overall workflow is displayed in Fig 3, which include UAV-Camera system, flight path planning in
 133 Pix4DCapture, image pre-processing in Pix4DMapper. The outputs of image preprocessing process are spectral bands

and SVI GeoTIFF images of the whole site.

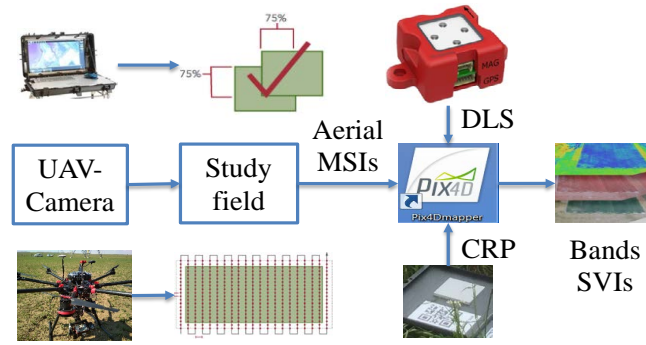


Figure 3: Workflow of MSI image acquisition and preprocessing.

134

135 3. Methods

136 This section introduces the methods for blackgrass weed mapping. The task of automatic blackgrass weed mapping
 137 is formulated as a supervised classification problem. The developed framework seamlessly integrates a number of
 138 advanced techniques: feature generation to enhance feature discrimination ability, feature selection for dimension
 139 reduction, Random Forest (RF) for classification, and Guided Filter for spatial information enhancement. The overall
 framework is displayed in Fig 4.

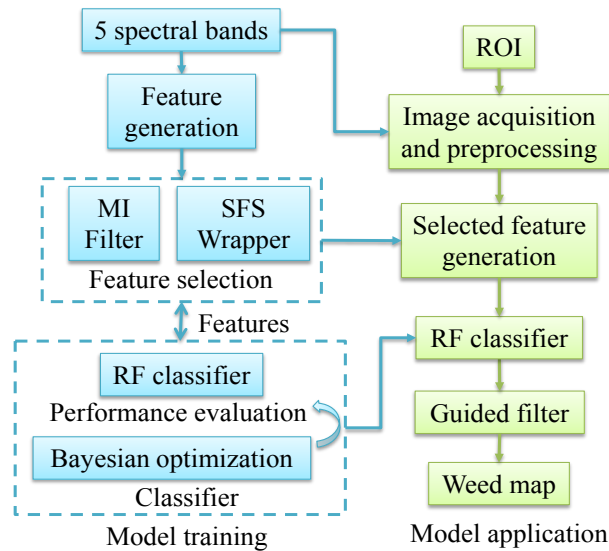


Figure 4: The developed system for blackgrass weed mapping in wheat fields: model training (left) and model application to RoI (right).

140

141 The system in Fig 4 consists of two stages: model training and model application. In training step, 5 raw spectral
 142 bands are first manipulated to generate 18 SI features. Then feature selection is used to reduce feature dimensionality
 143 and improve empirical interpretability, where both filter (Mutual Information (MI) ranking) and wrapper (Sequential

144 Forward Selection (SFS)) feature selection approaches are considered [26] to identify the better one. The selected
 145 features are to train a classification model, where RF classifier with Bayesian hyperparameter optimization is adopted.
 146 In applying the model to the Region of Interest (RoI), the trained RF classifier is applied to the selected spectral
 147 features; then the classification probability maps are further processed by guided filter so that spatial information can
 148 be incorporated into the final weed map.

149 3.1. Aerial imagery with groundtruth labelling

150 The aerial imagery is firstly introduced including its groundtruth labelling. The raw aerial images were first
 151 processed by the procedures in Section 2.3 for spectral band reflectance and SI map generation. The RGB composite
 152 with image adjustment for intensity enhancement is displayed in Fig 5. Random parts of the image are also manually
 153 (via zoom in and zoom out) labelled by “Image Labeller” in Matlab. In particular, 125164 out of 3154051 pixels are
 labelled into three classes: Blackgrass (53635), Wheat (47133) and Background (24396).

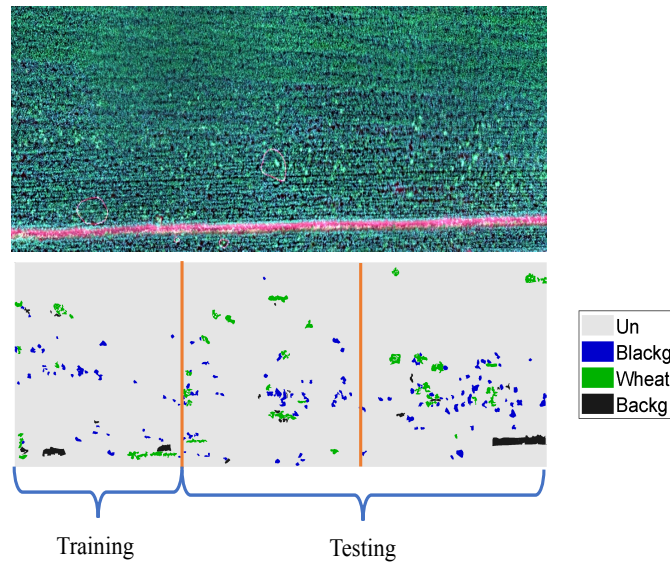


Figure 5: Upper: RGB composite of the RoI with image intensity enhancement; Lower: labelled classes by visual inspection in Matlab “Image Labeller” including Un being unlabelled region. Pixel resolution: 1.16cm/pixel, image size: 3000x1050.

154

155 3.2. Feature generation

156 In order to maximally represent image characteristics, 18 widely-used SIs are generated as the potential features
 157 in addition to 5 raw spectral bands. SI refers to a mathematical expression combining the surface reflectance at
 158 two or three spectral bands in order to enhance spectral differences of various objects. SI is a common technique
 159 in precision agriculture and has been widely applied in a number of areas such as weed mapping [2], yellow rust

160 monitoring [9]. Following preceding work [9], 18 widely-used SIs for RedEdge multispectral camera are generated,
 161 which are summarized in Table 1.

162 3.3. Feature selection

163 Feature Selection (FS) is to select a subset of features for model construction, which is able to simplify the model,
 164 reduce the training time, avoid the curse of dimensionality and enhance generalization by reducing the chance of
 165 overfitting. Suppose the complete feature set is F_s with d being its feature number, selecting the best subset $S_s \subseteq F_s$
 166 results in possible $2^d - 1$ combinations, indicating exhaustive search is impossible due to the NP-hard problem.
 167 Practical methods usually follow certain heuristics. According to various metrics, the existing FS algorithms can
 168 be broadly categorised into three classes including filters, wrappers and embedded methods. Filters rely on proxy
 169 measures (MI, Pearson correlation) to rank features, which is independent of the classifier and also computationally
 170 efficient. Wrappers rely on predictive models to evaluate feature subsets and usually provide the best performance but
 171 with a higher computation load. While Embedded methods perform feature selection as part of the model construction
 172 process and are usually constrained to certain classifiers.

173 In this work, to make the classification model simple but effective, both filter and wrapper approaches are con-
 174 sidered. In particular, MI between features and class label is adopted as the evaluation metric of filter approach,
 175 where the number of selected features is determined by the performance (Out-Of-Bag (OOB) error) of RF classifier.
 176 Moreover, Sequential Forward Selection (SFS) is also adopted as the wrapper strategy to identify the best feature
 177 combination, where RF is adopted to determine whether a feature should be included or not. The framework for MI
 filter and SFS wrapper is displayed in Fig 6. Their principles are briefly introduced in the following subsections.

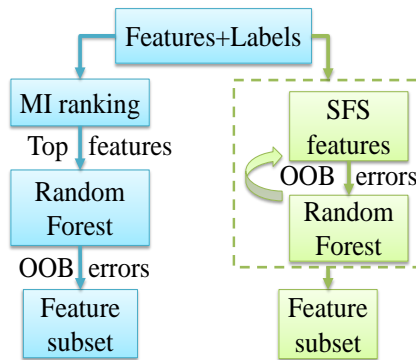


Figure 6: Feature selection: MI filter (left) and SFS wrapper (right), where OOB errors is adopted to evaluate the RF performance.

178

Table 1: SVIs adopted in this study.

Category (No.)	Full name	ABBRE.	Band	Formula
VIS(4)	Nitrogen Reflectance Index	NRI	Green-Red	$(R_g - R_r)/(R_g + R_r)$
	Greenness Index	GI	Green-Red	R_g/R_r
	Green Leaf Index	GLI	Blue-Green-Red	$(2R_g - R_r - R_b)/(2R_g + R_r + R_b)$
	Triangular Greenness Index	TGI	Blue-Green-Red	$-0.5(\lambda_r - \lambda_b)(R_r - R_g) - (\lambda_r - \lambda_g)(R_r - R_b)$
Green-RE(1)	Anthocyanin Reflectance Index	ARI	Green-RE	$R_g^{-1} - R_{re}^{-1}$
Green-NIR(3)	Green NDVI	GNDVI	Green-NIR	$(R_{nir} - R_g)/(R_{nir} + R_g)$
	Triangular Vegetation Index	TVI	Green-NIR	$0.5[120(R_{nir} - R_g) - 200(R_{nir} - R_g)]$
	Chlorophyll II Index-Green	CIG	Green-NIR	$R_{nir}/R_g - 1$
Red-NIR(4)	Normalized Difference Vegetation Index	NDVI	Red-NIR	$(R_{nir} - R_r)/(R_{nir} + R_r)$
	Soil Adjusted Vegetation Index	SAVI	Red-NIR	$1.5(R_{nir} - R_r)/(R_{nir} + R_r + 0.5)$
	Ratio Vegetation Index	RVI	Red-NIR	R_{nir}/R_r
	Optimized Soil Adjusted Vegetation Index	OSAVI	Red-NIR	$1.16(R_{nir} - R_r)/(R_{nir} + R_r + 0.16)$
RE-NIR(2)	Chlorophyll II Index-RedEdge	CIRE	RE-NIR	$R_{nir}/R_{re} - 1$
	Normalized Difference RedEdge Index	NDREI	RE-NIR	$(R_{nir} - R_{re})/(R_{nir} + R_{re})$
VIS-RE-NIR(4)	Enhanced Vegetation Index	EVI	Blue-Red-NIR	$2.5(R_{nir} - R_r)/(R_{nir} + 6R_r - 7.5R_b + 1)$
	Transformed Chlorophyll II Absorption and Reflectance Index	TCARI	Green-Red-RE	$3[(R_{re} - R_r) - 0.2 * (R_{re} - R_g)(R_{re}/R_r)]$
	Chlorophyll II Vegetation Index	CVI	Green-Red-NIR	$R_{nir}R_r/R_g^2$
	Simplified Canopy Chlorophyll II Content Index	SCCCI	Red-RE-NIR	NDREI/NDVI

179 3.3.1. MI filter

180 There are various feature scoring algorithms. According to various criteria to evaluate the relationship between
181 features and class label, these algorithms include MI, Fisher score, Minimum Redundancy and Maximum Relevance
182 (MRMR) and ReliefF based ones. In comparison with other approaches, MI is not only simple but also can reflect the
183 statistical dependency between two random variables, and therefore is adopted. MI is usually defined for two discrete
184 random variables (feature quantization is adopted to discretize continuous variables into discrete bins) and a higher
185 value means a higher statistical relevance. MI value for random variables Y and Z is defined by

$$MI(Y, Z) = \sum_{y \in Y} \sum_{z \in Z} P(y, z) \log \left(\frac{P(y, z)}{P(y)P(z)} \right), \quad (1)$$

186 where $P(y)$, $P(z)$ and $P(y, z)$ represent marginal probability distribution of Y and Z , and the joint probability distri-
187 bution of Y and Z . Then the top features identified by MI ranking can be selected as the features for RF classifier
188 construction so that the optimal feature number can be determined.

189 3.3.2. Sequential Forward Selection (SFS)

190 SFS is a typical search strategy for wrappers feature selection. In this approach, features are added sequentially
191 into the feature set, where the evaluation metric for adding a feature is defined as the OOB error of RF. To avoid
192 distracting readers from the main contributions, SFS with RF is summarized in Algorithm 1 (see, Appendices).

193 3.4. Random forest classifier

194 The task of classification can be achieved by many algorithms such as classification tree, K-Nearest Neighbours,
195 discriminant analysis, Support Vector Machine [27]. RF is preferred for the task with a small number of labelled data;
196 because RF achieves good performance in term of accuracy and robustness while with a relatively low computation
197 cost. In addition, it can not only return the class label but also the probability in the range of [0,1]. RF is an
198 ensemble learning method, where a number of decision trees are trained (by bootstrap sampling) with the final class
199 output being the mode of individual decision trees. RF, in comparison to individual decision tree, can effectively avoid
200 overfitting and improve robustness. In order to improve its performance, its hyperparameters are automatically tuned
201 by Bayesian optimization. RF classifier with Bayesian optimization is summarized in Algorithm 2 (see, Appendices).

202 By applying the trained RF to the RoI, one can obtain the initial pixel-wise classification maps

$$P = \{P_1, \dots, P_C\} \text{ with } P_k = \{p_k^1, \dots, p_k^n\}, \quad (2)$$

203 where $P_k, k = 1, \dots, C$ denotes the probability map for class k with C being the class number; $p_k^i \in [0, 1]$ denotes the
 204 probability that pixel i belongs to class k .

205 3.5. Guided filter for spatial information

206 In real-life applications, pixels in a local region are more likely to share the same class label. This type of spatial
 207 information should also be considered. Inspired by the hyperspectral image classification in [28], spatial filtering is
 208 adopted to regularize the initial spectral classification maps. Guided filter in [29] is preferred due to its fine properties
 209 in enhancing the smoothness of local areas and preserving the edge information of the reference image.

210 Guided filter assumes a local linear model between guidance image I (input image itself or an reference image)
 211 and filter output Q in a local window w_k centred at pixel k :

$$Q_i = a_k I_i + b_k, \forall i \in w_k, \quad (3)$$

212 where i denotes pixel index, (a_k, b_k) are some unknown linear coefficients being constant in w_k . To determine the
 213 coefficients, a cost function is defined, which minimizes the differences between output image Q and input image P ,

$$E(a_k, b_k) = \sum_{i \in w_k} [(a_k I_i + b_k - P_i)^2 + \epsilon a_k^2], \quad (4)$$

214 where ϵ is a regularization parameter preventing a_k being too large. The model (3) and the approximation solution
 215 of (4) ensure that $\nabla Q \approx \bar{a} \nabla I$ with \bar{a} being the approximation solution of a . Therefore, the edge information in the
 216 reference image I can be preserved in filtering output image Q .

217 In this work, various three-band images including RGB image, the first three principal components of PCA analysis,
 218 and the first three SIs by SFS feature selection algorithm are adopted as the reference image for the Guided filter.
 219 Then (3) with the solution of (4) is adopted to regularize the initial probabilistic maps $P_i (i = 1, \dots, C)$ in (2), given
 220 by

$$\hat{P}_i = \text{Guided filter}(I, P_i). \quad (5)$$

221 After all C initial probabilistic maps are processed by Guided filter, the final class label of pixel i is determined by the
 222 maximum of filtered maps $\hat{P}_i (i = 1, \dots, C)$. The overall procedure is summarized in Algorithm 3 (see, Appendices).

223 3.6. Performance evaluation

224 Various metrics are adopted for performance evaluation. OOB error is adopted to measure the prediction error of
 225 RF classifier to avoid overfitting in feature selection algorithms and hyperparameter optimization. OOB error denotes

226 the mean prediction error on each training sample x_i , using only the trees that did not have x_i in their bootstrap
 227 aggregating (or bagging) samples. It is reported that OOB error helps avoid the need for an independent validation
 228 dataset. In addition, other popular metrics are also adopted wherever necessary such as accuracy, precision and recall.
 229 These metrics rely on a number of definitions including True Positive (TP), False Positive (FP), True Negative (TN)
 230 and False Negative (FN) [9]. Accuracy, a good measure for symmetric datasets, can then be defined by

$$Accuracy = \sum_i TP / All, \text{ with } All = TP + FP + TN + FN. \quad (6)$$

231 Precision and Recall, effective measures for data with uneven distributions, can also be defined for a specific class,

$$\begin{aligned} Precision &= TP / (TP + FP) \\ Recall &= TP / (TP + FN) \end{aligned} \quad (7)$$

232 Their mean values for various land cover classes can then be calculated.

233 4. Results

234 4.1. Spectral analysis

235 Spectral analysis is first conducted, where the mean reflectance values (along with $0.5-\sigma$ area) of five original bands
 236 and 18 SVIs for various land cover classes including Blackgrass (Blackg), Wheat and Background (Backg) are displayed
 237 in Figs 7 and 8. Moreover, the correlation analysis between different spectral bands and SVIs is also performed. The
 correlation map is displayed in Fig 9, where a brighter pixel means a higher correlation value.

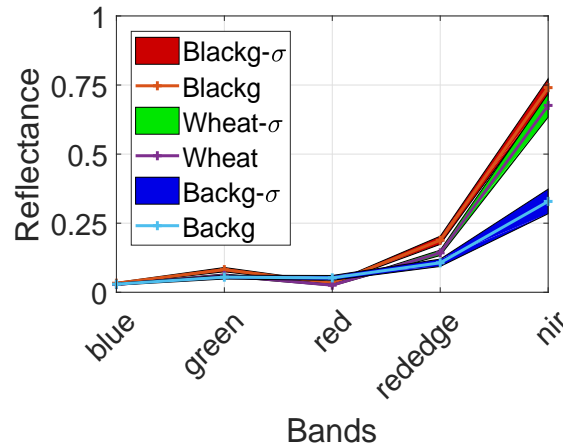


Figure 7: Mean reflectance and $0.5-\sigma$ range of five spectral bands for three land cover classes in the wheat field.

238
 239 The following observations can be drawn from Figs 7, 8 and 9. As seen in Fig. 7, various materials have distinct
 240 spectral reflectance values (curves), which can be learnt by machine learning algorithms for classification. As seen

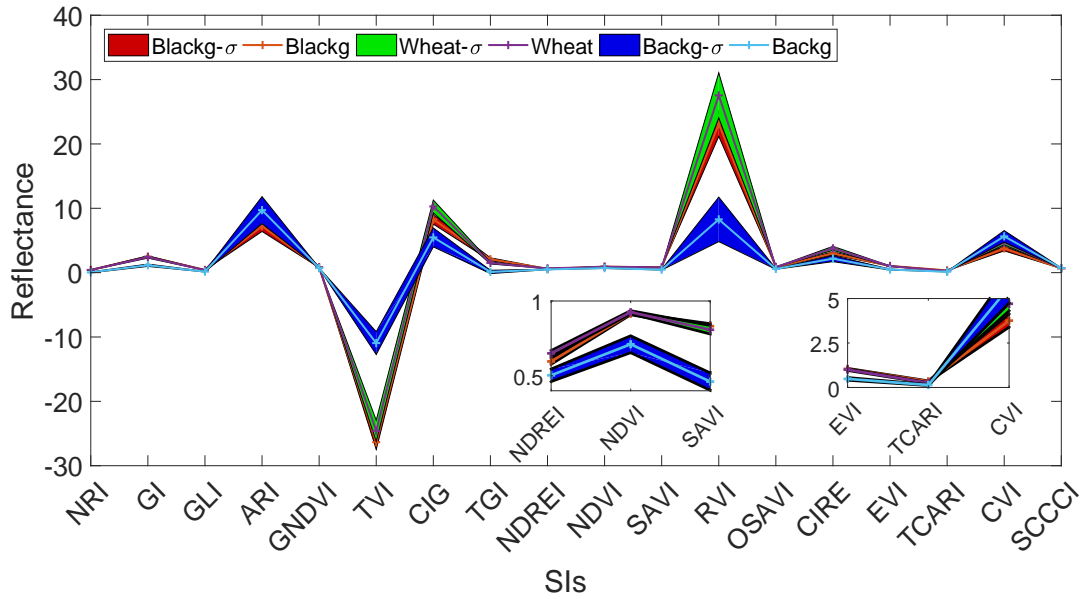


Figure 8: Mean reflectance and $0.5\text{-}\sigma$ range of 15 SVIs for three land cover classes in the wheat field.

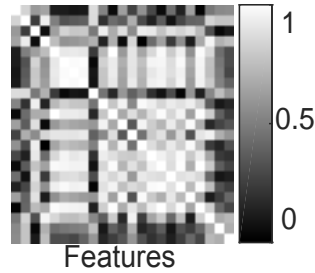


Figure 9: Correlation map of spectral bands & SVIs, where greyscale represents the level of correlation with black (0) and white (1).

241 in Figs. 7 and 8, reflectance differences are distinct in various spectral bands/SIs for various materials, so various
 242 spectral bands/SIs have various discriminating abilities. As seen in Fig 9, many features have high correlation values
 243 (brighter), implying a high feature redundancy.

244 These observations on the one hand show the rationale of using classification for blackgrass weed mapping and
 245 on the other hand imply that feature selection is critical for a simple but effective classification model. The latter
 246 problem is even severer for the scenario with a limited number of labelled data in this study.

247 4.2. Feature selection

248 Considering that feature selection is generally time-consuming due to the large number of feature combinations (and
 249 consequently different machine learning models to be trained), without loss of generality, only 15% of the randomly
 250 labelled data is used in feature selection. In MI filter, the continuous variables are discretized into 10 discrete bins.
 251 “TreeBagger” in Matlab with default parameters and 50 trees is first adopted to obtain the OOB error. Their results

are displayed in Fig 10, where vertical axis denotes the average OOB error and horizontal axis represents the features that are firstly selected by the algorithms. To demonstrate the discriminating ability of top (TGI) and bottom (blue) features selected by MI filter, their probability histograms are displayed in Fig 11.

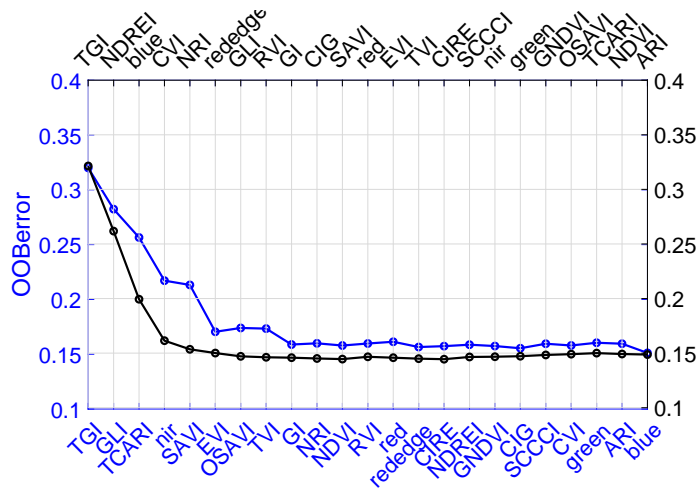


Figure 10: Results of MI (blue) and SFS (dark) for feature selection.

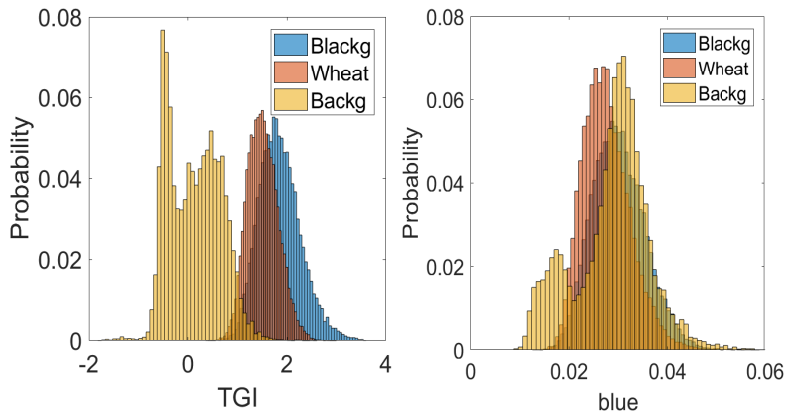


Figure 11: Histogram of best feature (TGI) and worst feature (blue) features by MI.

The following observations can be drawn from Figs 10, 11, and experimental comparisons. First, the best feature by MI filter and SFS wrapper is the same, that is TGI. Second, the best performance of MI filter occurs when all 23 features are selected, where the OOB error is 15.09%; while the best performance of SFS wrapper occurs when selected 12 features are adopted, where the OOB error is 14.43%. The OOB error of SFS wrapper is 14.68% when selected 8 features are adopted, which is very close to the best one and better than MI filter. So SFS wrapper generates a simple, yet effective model. Third, although Blue band has a very low MI value with class label (Fig 10) and a low discriminating ability alone (Fig 11), its combination with other features may result in good performance (Fig 10).

262 This implies that the MI filter is useful in assessing individual features, while SFS wrapper excels in identifying the
 263 best feature combination. Finally, the training time of SFS wrapper is 12 times of MI filter, since $(1+23)*23/2=276$
 264 RF classifiers are built in SFS wrapper compared to 23 classifiers in MI filter. Therefore, the first 8 features by SFS
 265 wrapper are adopted for model construction. In the following subsection, the parameters of RF classifier are optimized
 266 to enhance its performance by Bayesian optimization.

267 4.3. Algorithm verification

268 Bayesian optimization is adopted to tune the hyperparameters of RF classifier, where two key parameters are
 269 considered: minLS and numPTS. minLS is to specify trees' depth/complexity and numPTS controls the number of
 270 predictors to sample at each node in tree growing. $minLS \in [1, maxMinLS]$ is selected with maxMinLS being 18 and
 271 $numPTS$ in $[1, numF]$ with $numF$ being the feature number. Tree number is chosen 100, 'AcquisitionFunctionName' is
 272 chosen 'expected-improvement-plus'. Then two algorithm verification approaches are adopted as below.

273 4.3.1. Random split

274 In random split test, the random 15% of the labelled dataset is for algorithm training and the remaining random
 275 85% is for algorithm testing, where the confusion matrix (calculated on the validation set) is shown in left plot of Fig
 12. In left plot of Fig 12, the target and output class denote ground truth and predicted class. The diagonal cells

Output Class	Blackg	39097 36.7%	4933 4.6%	45 0.0%	88.7% 11.3%
	Wheat	6388 6.0%	34756 32.7%	535 0.5%	83.4% 16.6%
	Backg	105 0.1%	375 0.4%	20157 18.9%	97.7% 2.3%
	Recall	85.8% 14.2%	86.8% 13.2%	97.2% 2.8%	88.4% 11.6%
		Blackg	Wheat	Backg	Precision
Output Class	Blackg	34549 38.8%	6437 7.2%	191 0.2%	83.9% 16.1%
	Wheat	5191 5.8%	26554 29.8%	893 1.0%	81.4% 18.6%
	Backg	24 0.0%	271 0.3%	15012 16.8%	98.1% 1.9%
	Recall	86.9% 13.1%	79.8% 20.2%	93.3% 6.7%	85.4% 14.6%
		Blackg	Wheat	Backg	Precision
		Target Class			

Figure 12: Confusion matrix for random split test (left) and spatial split test (right).

276
 277 in green show the number/percentage of correct classification; the off-diagonal cells are where the misclassification
 278 occurs. For Blackg class, 39097 in green is TP and 4933 + 45 in red is FP, 6388 + 105 in red is FN. So precision for
 279 Blackg class is $39097/(39097 + 4933 + 45) = 88.7\%$, while recall for Blackg class is $39097/(39097 + 6388 + 105) = 85.8\%$.

280 Similarly, precision and recall for Wheat and Backg classes are 83.4%, 86.8%, and 97.7%, 97.2%. As a result, the
 281 mean precision and recall for RF classifier are 89.9% and 89.9%. The cell at bottom right displays the overall accuracy
 282 (88.4%). Precision and recall for background class are very high, since its reflectance values are significantly different
 283 from other classes and can be easily classified.

284 4.3.2. Spatial split

285 Different from random split test, in spatial split test, the ROI in Fig 5 is vertically split into three equal parts,
 286 where the labelled pixels in the leftmost part is for algorithm training and the remaining two parts are for algorithm
 287 testing. The confusion matrix is shown in the right plot of Fig 12. One can see that the performance of spatial split is
 288 slightly worse than the random split, this is mainly due to the lack of diversity in spatial split test. This implies that
 289 in real-world applications, more diverse datasets from different locations are desirable in order to improve algorithm
 290 generalization.

291 4.4. Application to RoI

292 The optimized RF classifier with selected features is then applied to the whole RoI in Section 3.1. The classification
 293 results by only spectral feature are shown in Fig 13 (a). The Guided filter in Section 3.5 is also applied to the initial
 294 probabilistic maps to incorporate spatial information in reference images. Three reference images are tested: RGB
 295 composite (with image enhancement), the top three principal components (the values in each PC are transformed into
 296 $[0, 1]$) by PCA (PCA-Top3) and the top three SIs (the values of each SI are also transformed into $[0, 1]$) identified by
 297 SFS wrapper (SFS-Top3). Their comparative results are shown in Fig. 13 (b), (c) and (d). Their performance is also
 298 summarized in Table 2.

Table 2: Performance comparisons for various reference images.

Approach	precision	recall	accuracy
Spectral	89.9%	89.9%	88.4%
RGB	93.4%	93.5%	92.5%
PCA-Top3	93.9%	94.0%	93.1%
SFS-Top3	93.8%	93.8%	93.0%

299 The following observations are drawn from Fig 13, and Table 2. First, it follows from Fig 13 that pixel-wise
 300 classification by only spectral feature may result in random noises and including spatial information by Guided filter

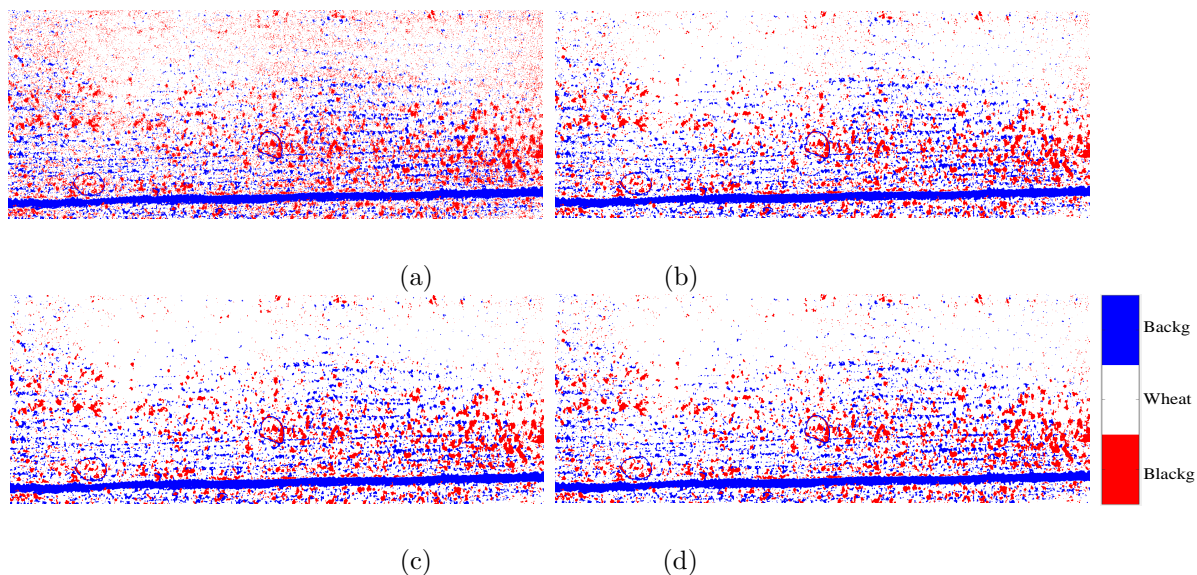


Figure 13: Classification map by using only spectral feature (a); Classification results by Guided filter regularization: RGB (b), SFS-Top3 (c) and PCA-Top3 (d).

301 (Fig 13) can improve the result by reducing the noises while preserving the edge information in reference image.
 302 Secondly, all Guided filter approaches (Table 2) outperform the purely spectral based ones; PCA and SFS have similar
 303 performance, slightly better than RGB based one. As a by-product, the probabilistic blackgrass weed map is displayed
 in Fig 14, which can be used for weed management in subsequent year.

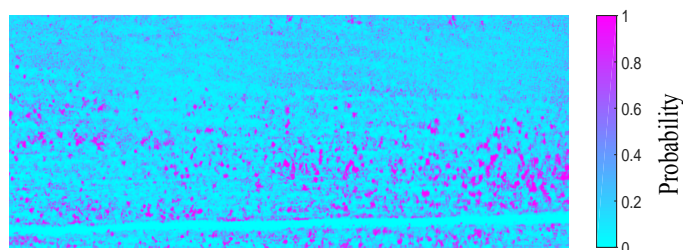


Figure 14: Blackgrass weed probabilistic map with Guided filter regularization by SFS-Top3 reference image.

304

305 5. Discussions

306 Site-specific weed management (SSWM) is paramount for sustainable agriculture (i.e. generating more and better
 307 outputs with less inputs while with decreased environmental footprint) in order to meet the world's future food security
 308 and sustainability needs. Instead of ground field sampling, remote/proximal sensing is drawing increasing research
 309 interests due to its potential for large scale applications with less human involvement.

310 UAV remote sensing for precision agriculture is still a developing technology and has initially been applied to a

311 number of areas such as disease, drought and nitrogen monitoring [4, 9] due to its user-defined spatial, spectral and
312 temporal resolutions and suitability for application at farmland scales. Even for weed mapping, there are already
313 a number of studies [2, 5, 15, 16, 19, 20, 30]. It is noted, however, that early (seedling) weed detection [2, 19] is
314 only possible for certain wheat/weed combinations by using very high-resolution images or hyperspectral images [23].
315 Unfortunately, wheat is monocotyledonous crop, which makes it extremely challenging for early (seedling) blackgrass
316 mapping by using UAVs due to various reasons such as wheat/blackgrass spectral similarity, low spatial resolution [16],
317 challenges in ground truth labelling. Therefore, this work (the first one in using UAV multispectral remote sensing
318 for blackgrass weed mapping) is focused on late-season weed mapping, which is still very useful in a number of SSWM
319 practices such as designing SSWM for subsequent years, applying in-season post-emergence herbicides, assessing the
320 effectiveness of herbicide applications [16, 6]

321 Different from conventional studies [2, 5] for weed mapping by using MSI, where only a very limited number
322 of spectral vegetation indices are adopted for model learning, this work first generates a relatively large number of
323 spectral features to enhance feature discriminating abilities [9]. On this basis, advanced feature selection algorithms
324 are further adopted to reduce weak features and identify the best (reduced-order) feature combination. With selected
325 features, RF classifier is adopted for classification task in this work (i.e. learning from a limited number of labelled
326 data) due to its fine properties in term of accuracy and robustness while with a relatively low computation cost. The
327 hyperparameters of RF are further optimized by using Bayesian optimization to guarantee better performance.

328 Another novelty of this work is to adopt Guided filter [29] to regularize the probabilistic maps so that spatial
329 information can be incorporated for better classification performance [28]. To identify a suitable reference image for
330 Guided filter, different three-band images are extracted from 5 spectral bands and 18 spectral vegetation indices by
331 using RGB composite, PCA analysis and SFS Wrapper feature selection. Finally, the blackgrass weed mapping system
332 by using aerial MSI is applied to ROI with a promising result in term of Precision, Recall and Accuracy.

333 Regarding image segmentation algorithm, this study only considered the random forest algorithm with hyperpa-
334 rameter optimization. Interested readers are referred to the recent study [27], which compares and assesses different
335 Geographic Object-Based Image Analysis (GEOBIA) and machine learning algorithms using UAV multispectral im-
336 agery via a case study in a citrus orchard and an onion crop. More importantly, different from this study, operational
337 interest and aspects such as requested time and computing resources as well as the expertise needed to implement
338 them are also available in [27] for a practical application.

339 Regarding the multispectral sensor in this study, for the time being, the UAV has to be operated at an altitude of

340 about 20 meters so that centimetre-resolution image can be obtained for the purpose of a good image segmentation.
341 However, flight height of 30-50 meters and more would be more desirable to cover a relatively large field of interest in a
342 short time. Therefore, new multispectral camera of high geometrical and spectral resolution would be more desirable
343 for practical implementation.

344 Though the experimental results are very positive, there is still much room for further development in terms of
345 data, algorithm and experimental verification. Several aspects are as below:

- 346 (1) Only spectral and spatial features are considered in this study; temporal information should also be investigated
347 to achieve an early and more reliable weed mapping;
- 348 (2) With the advent of a large volume of labelled (high-resolution) images for precision agriculture applications,
349 deep features rather than hand-crafted features may be considered by using end-to-end deep neural network.
- 350 (3) More aerial datasets collected under various conditions (e.g. time, weather, UAV altitude, wheat varieties) will
351 be used to enhance the robustness and improve the generalization of the developed framework.

352 **6. Conclusions**

353 This work exploits the potentials of five-band multispectral camera, small airborne platform and machine learning
354 algorithms (e.g. feature generation and selection, Bayesian parameter optimization, and spatial information enhance-
355 ment by Guided filter) for the automatic mapping of blackgrass weeds in winter wheat. A blackgrass weed mapping
356 system is initially developed by learning from spectral-spatial features of labelled aerial MSI. The system is initially
357 validated on a naturally blackgrass infected wheat field, where aerial MSIs were collected at an altitude of 20m with
358 a ground spatial resolution of 1.16cm/pixel. Comparative experimental results show that the developed system can
359 achieve a satisfying classification result with an average precision, recall and accuracy of 93.8%, 93.8% and 93.0%
360 when wheat and blackgrass weeds are in the stages of full ear emergence and early seed shedding. The SI with the
361 best discriminating ability is TGI. It is also discovered that wrapper feature selection can substantially reduce feature
362 dimension from original 23 to 8 while achieving better performance than using all 23 features. Spatial information
363 from Guided filter is proved to be effective in helping attenuate the noises of pixel-wise spectral classification and
364 improve classification performance.

365 **Appendices**

Algorithm 1: SFS with Random Forest

- (a) Start with an empty set $Y_0 = \emptyset, k = 0$ with full feature set $Y = \{y_1, \dots, y_d\}$;
- (b) Select the next best feature x^+ by

$$x^+ = \arg \min_{x \in (Y - Y_k)} OOBErr(Y_k + x),$$

where $OOBErr(Z)$ denotes OOB error of the Random Forest classifier trained by using feature set Z ;

- (c) Update $Y_{k+1} = Y_k + x^+$ with $k = k + 1$;
- (d) Repeat Steps (b) (c) until termination rules (desired feature number or $OOBErr$ increment) are satisfied.
-

Algorithm 2: Random Forest with Bayesian optimization

- (a) Set tree number and stopping rules;
- (b) Choose hyperparameters as $\lambda \in \Omega$, then train classifier with λ . Define objective function as the mean of $OOBErr$

$$\lambda_{opt} = \arg \min_{\lambda \in \Omega} OOBErr(\lambda);$$

- (c) Sequentially perform: 1. fitting a Gaussian process for data points $\{\lambda_i, OOBErr(\lambda_i)\}$ with new data point updating; 2. identifying new point for evaluation by maximizing the acquisition function;
- (d) Terminate iteration when stopping criterion are satisfied.
-

Algorithm 3: Guided filter for image regularization

- (a) Given an initial pixel-wise probabilistic maps $P = \{P_1, \dots, P_C\}$ with only spectral information;
- (b) Process the initial probabilistic maps by Guided filter, resulting in filtered maps $\hat{P} = \{\hat{P}_1, \dots, \hat{P}_C\}$;
- (c) Obtain the class label for pixel j by the maximum of the posterior maps, given by

$$[M_i] = \arg \max_{j \in [1, C]} \{\hat{P}_1, \dots, \hat{P}_C\}.$$

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369 References

- 370 [1] J. A. Foley, N. Ramankutty, K. A. Brauman, E. S. Cassidy, J. S. Gerber, M. Johnston, N. D. Mueller, C. OConnell, D. K.
371 Ray, P. C. West, *et al.*, “Solutions for a cultivated planet,” *Nature*, vol. 478, no. 7369, p. 337, 2011.
- 372 [2] M. Pérez-Ortiz, J. Peña, P. A. Gutiérrez, J. Torres-Sánchez, C. Hervás-Martínez, and F. López-Granados, “A semi-
373 supervised system for weed mapping in sunflower crops using unmanned aerial vehicles and a crop row detection method,”
374 *Applied Soft Computing*, vol. 37, pp. 533–544, 2015.
- 375 [3] J. M. Peña-barragán, F. López-granados, M. Jurado-expóstto, and L. García-torres, “Mapping *ridolfia segetum* patches in
376 sunflower crop using remote sensing,” *Weed Research*, vol. 47, no. 2, pp. 164–172, 2007.
- 377 [4] C. Zhang and J. M. Kovacs, “The application of small unmanned aerial systems for precision agriculture: a review,”
378 *Precision agriculture*, vol. 13, no. 6, pp. 693–712, 2012.
- 379 [5] A. I. de Castro, M. Jurado-Expósito, J. M. Peña-Barragán, and F. López-Granados, “Airborne multi-spectral imagery for
380 mapping cruciferous weeds in cereal and legume crops,” *Precision Agriculture*, vol. 13, no. 3, pp. 302–321, 2012.
- 381 [6] J. Lambert, H. Hicks, D. Childs, and R. Freckleton, “Evaluating the potential of unmanned aerial systems for mapping
382 weeds at field scales: a case study with *alopecurus myosuroides*,” *Weed research*, vol. 58, no. 1, pp. 35–45, 2018.
- 383 [7] P. Lutman, S. Moss, S. Cook, and S. Welham, “A review of the effects of crop agronomy on the management of a *lopecurus*
384 *myosuroides*,” *Weed Research*, vol. 53, no. 5, pp. 299–313, 2013.
- 385 [8] L. Rew and R. Cousens, “Spatial distribution of weeds in arable crops: are current sampling and analytical methods
386 appropriate?,” *Weed Research*, vol. 41, no. 1, pp. 1–18, 2001.
- 387 [9] J. Su, C. Liu, M. Coombes, X. Hu, C. Wang, X. Xu, Q. Li, L. Guo, and W.-H. Chen, “Wheat yellow rust monitoring by
388 learning from multispectral uav aerial imagery,” *Computers and electronics in agriculture*, vol. 155, pp. 157–166, 2018.
- 389 [10] Z. Mi, X. Zhang, J. Su, D. Han, and B. Su, “Wheat stripe rust grading by deep learning with attention mechanism and
390 images from mobile devices,” *Frontiers in Plant Science*, vol. 11, 2020.

- 391 [11] G. Modica, G. Messina, G. De Luca, V. Fiozzo, and S. Praticò, “Monitoring the vegetation vigor in heterogeneous citrus
392 and olive orchards. a multiscale object-based approach to extract trees crowns from uav multispectral imagery,” *Computers
393 and Electronics in Agriculture*, vol. 175, p. 105500, 2020.
- 394 [12] N. Wilke, B. Siegmann, J. A. Postma, O. Muller, V. Krieger, R. Pude, and U. Rascher, “Assessment of plant density for
395 barley and wheat using uav multispectral imagery for high-throughput field phenotyping,” *Computers and Electronics in
396 Agriculture*, vol. 189, p. 106380, 2021.
- 397 [13] S. Haug, A. Michaels, P. Biber, and J. Ostermann, “Plant classification system for crop/weed discrimination without
398 segmentation,” in *IEEE winter conference on applications of computer vision*, pp. 1142–1149, IEEE, 2014.
- 399 [14] A. Milioto, P. Lottes, and C. Stachniss, “Real-time semantic segmentation of crop and weed for precision agriculture robots
400 leveraging background knowledge in cnns,” in *2018 IEEE International Conference on Robotics and Automation (ICRA)*,
401 pp. 2229–2235, IEEE, 2018.
- 402 [15] I. Sa, Z. Chen, M. Popović, R. Khanna, F. Liebisch, J. Nieto, and R. Siegwart, “weednet: Dense semantic weed classification
403 using multispectral images and mav for smart farming,” *IEEE Robotics and Automation Letters*, vol. 3, no. 1, pp. 588–595,
404 2018.
- 405 [16] F. López-granados, “Weed detection for site-specific weed management: mapping and real-time approaches,” *Weed Re-
406 search*, vol. 51, no. 1, pp. 1–11, 2011.
- 407 [17] J. Torres-Sánchez, F. J. Mesas-Carrascosa, F. M. Jiménez-Brenes, A. I. de Castro, and F. López-Granados, “Early detection
408 of broad-leaved and grass weeds in wide row crops using artificial neural networks and uav imagery,” *Agronomy*, vol. 11,
409 no. 4, p. 749, 2021.
- 410 [18] G. Rozenberg, R. Kent, and L. Blank, “Consumer-grade uav utilized for detecting and analyzing late-season weed spatial
411 distribution patterns in commercial onion fields,” *Precision Agriculture*, pp. 1–16, 2021.
- 412 [19] J. M. Pena, J. Torres-Sánchez, A. I. de Castro, M. Kelly, and F. López-Granados, “Weed mapping in early-season maize
413 fields using object-based analysis of unmanned aerial vehicle (uav) images,” *PloS one*, vol. 8, no. 10, p. e77151, 2013.
- 414 [20] P. Lottes, R. Khanna, J. Pfeifer, R. Siegwart, and C. Stachniss, “Uav-based crop and weed classification for smart farming,”
415 in *Robotics and Automation (ICRA), 2017 IEEE International Conference on*, pp. 3024–3031, IEEE, 2017.
- 416 [21] I. Sa, M. Popović, R. Khanna, Z. Chen, P. Lottes, F. Liebisch, J. Nieto, C. Stachniss, A. Walter, and R. Siegwart,
417 “Weedmap: a large-scale semantic weed mapping framework using aerial multispectral imaging and deep neural network
418 for precision farming,” *Remote Sensing*, vol. 10, no. 9, p. 1423, 2018.

- 419 [22] J. Su, D. Yi, B. Su, Z. Mi, C. Liu, X. Hu, X. Xu, L. Guo, and W.-H. Chen, "Aerial visual perception in smart farming:
420 Field study of wheat yellow rust monitoring," *IEEE Transactions on Industrial Informatics*, vol. 17, no. 3, pp. 2242–2249,
421 2021.
- 422 [23] F. López-Granados, M. Jurado-Expósito, J. M. Peña-Barragán, and L. García-Torres, "Using remote sensing for identifi-
423 cation of late-season grass weed patches in wheat," *Weed Science*, vol. 54, no. 2, pp. 346–353, 2006.
- 424 [24] J. Su, M. Coombes, C. Liu, Y. Zhu, X. Song, S. Fang, L. Guo, and W.-H. Chen, "Machine learning-based crop drought
425 mapping system by uav remote sensing rgb imagery," *Unmanned systems*, vol. 8, no. 01, pp. 71–83, 2020.
- 426 [25] J. Su, C. Liu, X. Hu, X. Xu, L. Guo, and W.-H. Chen, "Spatio-temporal monitoring of wheat yellow rust using uav
427 multispectral imagery," *Computers and electronics in agriculture*, vol. 167, p. 105035, 2019.
- 428 [26] S. Song, Y. Gong, Y. Zhang, G. Huang, and G.-B. Huang, "Dimension reduction by minimum error minimax probability
429 machine," *IEEE Transactions on Systems, Man, and Cybernetics: Systems*, vol. 47, no. 1, pp. 58–69, 2016.
- 430 [27] G. Modica, G. De Luca, G. Messina, and S. Praticò, "Comparison and assessment of different object-based classifications
431 using machine learning algorithms and uavs multispectral imagery: a case study in a citrus orchard and an onion crop,"
432 *European Journal of Remote Sensing*, vol. 54, no. 1, pp. 431–460, 2021.
- 433 [28] X. Kang, S. Li, and J. A. Benediktsson, "Spectral–spatial hyperspectral image classification with edge-preserving filtering,"
434 *IEEE transactions on geoscience and remote sensing*, vol. 52, no. 5, pp. 2666–2677, 2014.
- 435 [29] K. He, J. Sun, and X. Tang, "Guided image filtering," in *European conference on computer vision*, pp. 1–14, Springer,
436 2010.
- 437 [30] E. R. Hunt Jr, P. C. Doraiswamy, J. E. McMurtrey, C. S. Daughtry, E. M. Perry, and B. Akhmedov, "A visible band index
438 for remote sensing leaf chlorophyll content at the canopy scale," *International Journal of Applied Earth Observation and*
439 *Geoinformation*, vol. 21, pp. 103–112, 2013.