

1 **Near-trapping effect of wave-cylinders interaction on pore water pressure and liquefaction**  
2 **around a cylinder array**

3 Zaibin Lin<sup>a</sup>, Dubravka Pokrajac<sup>b</sup>, Yakun Guo<sup>c</sup>, Chencong Liao<sup>d</sup>, Tian Tang<sup>e</sup>  
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- 5 a. Now Centre for Mathematical Modelling and Flow Analysis, School of Computing,  
6 Mathematics and Digital Technology, Manchester Metropolitan University, Manchester, M1  
7 5GD, United Kingdom  
8 Formerly School of Engineering, University of Aberdeen, AB24 3UE, UK  
9 Corresponding author: [zaibin.lin@gmail.com](mailto:zaibin.lin@gmail.com),  
10 b. School of Engineering, University of Aberdeen, AB24 3UE, UK  
11 c. Faculty of Engineering and Informatics, University of Bradford, BD7 1DP, UK,  
12 d. Collaborative Innovation Centre for Advanced Ship and Deep-Sea Exploration, State Key  
13 Laboratory of Ocean Engineering, Department of Civil Engineering, Shanghai Jiao Tong  
14 University, Shanghai, 200240, China  
15 e. Bekaert Technology Centre, Bekaert Company, Zvevegem, Belgium  
16  
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18 **Abstract:** The near-trapping effects on wave-induced dynamic seabed response and liquefaction  
19 close to a multi-cylinder foundation in storm wave conditions are examined. Momentary liquefaction  
20 near multi-cylinder structures is simulated using an integrated wave-structure-seabed interaction  
21 model. The proposed model is firstly validated for the case of interaction of wave and a four-cylinder  
22 structure, with a good agreement with available experimental measurements. The validated model is  
23 then applied to investigate the seabed response around a four-cylinder structure at 0° and 45°  
24 incident angles. The comparison of liquefaction potential around individual cylinders in an array  
25 shows that downstream cylinder is well protected from liquefaction by upstream cylinders. For a  
26 range of incident wave parameters, the comparison with the results for a single pile shows the  
27 amplification of pressure within the seabed induced by progressive wave. This phenomenon is  
28 similar to the near-trapping phenomenon of free surface elevation within a cylinder array.  
29

30 **Key words:** Wave-Structure-Seabed Interaction (WSSI); seabed response; four-cylinder foundation;  
31 near-trapping phenomenon; momentary liquefaction  
32

33 **1. Introduction**

34 Multi-cylinder structures, one of the most common offshore foundations, are vulnerable to  
35 environmental impact of waves and currents, and the associated dynamic seabed response. The  
36 wave-induced run-up, forcing, and seabed instability around foundations may result in the collapse  
37 of offshore structures. For the critical centre-to-centre spacing between cylinders and a given range  
38 of incident wave numbers, the near-trapping phenomenon can occur within an array of cylinder (Ohl  
39 et al., 2001a). This phenomenon causes the local amplification of wave amplitude, which occurs due  
40 to the trapping of undisturbed incident wave inside an array of cylinders. As a result, the  
41 wave-induced run-up and forcing, as well as the associated seabed response in the vicinity of  
42 multi-cylinder foundation can be significantly greater than in the case of single cylinder (Kamath et

43 al., 2016). The effect of these phenomena on the safety of offshore structures and their foundations is  
44 of particular interest and important due to the increasing applications of multi-cylinder foundations  
45 in offshore engineering.

46  
47 Near-trapping phenomenon is a dominant factor considered in the design of sufficient air gap under  
48 the deck of offshore structures. This phenomenon has been systematically and intensively  
49 investigated by numerous researchers. To obtain the velocity potential surrounding the various  
50 arrangements of two cylinders and force components induced by linear water waves, Spring and  
51 Monkmeyer (1974) analytically solved the potential theory formulations using a direct matrix  
52 solution and multiple scattering (Twersky, 1952). Based on the same assumption used in Spring and  
53 Monkmeyer (1974), Linton and Evans (1990) simplified the theory, and proposed new formulae to  
54 estimate the free surface elevation around an array of cylinders, together with new formulae to  
55 calculate the first and second-order mean forces. Using eigenfunction expansions and an integral  
56 representation, Malenica et al. (1999) introduced a semi-analytical approach to solve for velocity  
57 potential with an incident monochromatic wave for estimating the second-order wave diffraction in  
58 the vicinity of an array of circular cylinders. The experimental investigations of the near-trapping  
59 phenomenon under regular and irregular incident waves with two incident wave directions are  
60 analysed by Ohl et al. (2001a; b) who pointed out that Malenica et al. (1999) overestimated the  
61 second order amplitude under the regular wave with 45° heading.

62  
63 The rapid development of computing resources and techniques of Computational Fluid Dynamics  
64 (CFD) has made the full scale three-dimensional (3D) simulation of wave-structure interaction in  
65 ocean/offshore engineering problems possible. Extensive investigations were carried out to study  
66 these problems. An open source CFD model, REEF3D, was developed to investigate fully nonlinear  
67 wave-structure interaction with various arrangements of cylinder groups, including two cylinders in  
68 tandem (Kamath et al., 2015; Bihs et al., 2016) and four cylinders in an array (Kamath et al., 2016).  
69 In REEF3D continuity equations and Reynolds-averaged Navier-Stokes (RANS) equations, together  
70 with  $k-\omega$  turbulence model are discretised using Finite Difference Method (FDM). The free surface  
71 between water and air is tracked by Level Set Method (LSM). In the study of Kamath et al. (2016), a  
72 pronounced amplification of the wave force on upstream cylinder was found by comparing the  
73 simulated results for the cases with and without the downstream cylinders in a four-cylinder array.  
74 Another broadly adopted open access CFD code in coastal/offshore engineering is the OpenFOAM  
75 with free C++ library for solving a wide range of fluid flow and solid mechanics problems using  
76 Finite Volume Method (FVM). With the help of the open source wave generation tool waves2Foam  
77 (Jacobsen et al., 2012) in OpenFOAM and the application of a slip boundary condition on the  
78 cylinder surface, Paulsen et al. (2014b) performed the intensive investigations of the fully nonlinear  
79 wave-cylinder interaction for a range of Keulegan–Carpenter ( $KC$ ) numbers ( $KC = U_{z=0}T/D$ , where  
80  $U_{z=0}$  is the velocity amplitude at  $z=0$  with  $z$  pointing vertically,  $T$  is wave period, and  $D$  is the  
81 diameter of cylinder, Sumer and Fredsøe 2006). By analysing the numerical results, it was concluded  
82 that the process of return flow from the back of cylinder and the passage of the wave crest made the  
83 dominant contributions to the occurrence of secondary load cycle. For the purpose of more efficient  
84 computation, Paulsen et al. (2014a) proposed an innovative and fully nonlinear domain

85 decomposition approach, which involves coupling potential flow theory model (OceanWave3D,  
86 Engsig-Karup et al., 2009) and waves2Foam library. The good agreement between numerical and  
87 experimental results for irregular waves has demonstrated the accuracy and applicability of the  
88 coupled model. Chen et al. (2014) also elaborated a comprehensive study for exploring the  
89 applicability and capacity of OpenFOAM in evaluating fully nonlinear wave-cylinder interaction  
90 under regular and focused waves. Moreover, both wave generation and active absorbing boundaries  
91 were developed in Higuera et al. (2013a) (IHFOAM) for simulating wave-induced coastal  
92 engineering processes (Higuera et al., 2013b), and wave interaction with porous structures (Higuera  
93 et al., 2014a; Higuera et al., 2014b). A new moving boundary decomposed into multi-paddles and an  
94 enhanced active wave absorption boundary were integrated into IHFOAM (Higuera et al., 2015). All  
95 aforementioned research has been mainly concerned with wave interaction with coastal/offshore  
96 structures. However, the attention should also be paid to another important issue, namely the wave  
97 induced dynamic response in a porous seabed which occurs as a result of fully nonlinear  
98 wave-structure interactions.

99

100 Seabed stability in the vicinity of coastal/offshore structures is one of the most important issues in  
101 engineering design (Sumer and Fredsøe, 2002; Jeng, 2013; Sumer, 2014; Jeng, 2018). At the early  
102 stage of seabed stability research, analytical approximations on the basis of poro-elastic Biot's theory  
103 (Biot, 1941) were extensively used for investigating wave-induced seabed response. A considerable  
104 amount of both the theoretical and experimental porous seabed research before 2003 has been  
105 reviewed and summarized in Jeng (2003). In recent years, the applicability of three different soil  
106 models, including fully dynamic (FD), partially dynamic (PD), and quasi-static (QS) model, was  
107 investigated in Ulker and Rahman (2009) and Ulker et al. (2009). Their conclusions are consistent  
108 with Jeng and Cha (2003), who showed that the maximum discrepancy between the calculated  
109 results is within 3%. and they proposed the applicability for the three above-mentioned models in  
110 partially/fully saturated porous seabed. Considering the combined effect of current and nonlinear  
111 wave, Liao et al. (2013) proposed an analytical approximation to investigate the soil response within  
112 a porous seabed, and concluded that this effect had a considerable impact in the upper zone beneath  
113 seabed surface. However, due to underlying assumptions and simplifications these analytical  
114 approximations are not able to fully describe the complicated process of wave-induced seabed  
115 stability in the proximity of coastal/offshore structures.

116

117 Due to its practical importance and engineering applications, extensive laboratory experimental  
118 modelling studies have been conducted to investigate wave-induced soil response in a porous seabed.  
119 To understand the mechanism of pore water pressure and scour around a mono-pile foundation, Qi  
120 and Gao (2014) performed experimental studies with various combined wave and current parameters.  
121 Liu et al. (2015) conducted laboratory experiment in a one-dimensional (1-D) soil column to  
122 examine the pore pressure development under sinusoidal wave pressure applied at one end of the  
123 column. The thickness of sandy deposit was slightly reduced after a long-term dynamic wave loading.  
124 The oscillatory excess pore pressure within a well-mixed seabed, consisting of silt and sand, and the  
125 influence of the ratio of sand/silt in mixture were experimentally studied by Zhang et al. (2016) with  
126 a series of incident waves. Recently, Sun et al. (2019) conducted laboratory experiments to

127 investigate the dynamic soil response and liquefaction potential around a buried pipeline in a trench  
128 layer. In the context of wave-induced soil response, the experimental studies have the capacity of  
129 directly capturing the realistic behaviour. However, the scope of physical experiments is limited by  
130 scale-effects and cost.

131

132 Numerical modelling is the effective alternative approach adopted by numerous researchers. Without  
133 considering the wave diffraction and reflection, Li et al. (2011) estimated the wave-induced pore  
134 pressure around pile foundation by solving 3D Biot's equation using FEM. Hereafter, a series of  
135 investigations by Jeng and his co-workers has been performed to examine dynamic behaviour of the  
136 soil in a marine seabed around coastal/offshore structures, such as pipeline (Zhao et al., 2016; Lin et  
137 al., 2016), breakwaters (Zhang et al., 2011; Jeng et al., 2013; Ye et al., 2013; Ye et al., 2016), and pile  
138 supported structures (Sui et al., 2017, 2019; Zhao et al., 2017). In all these studies, the equations  
139 governing the motion of two-phase fluid (RANS and VOF) and the response of seabed were solved  
140 by FVM and FEM, respectively. Another monolithically integrated model solving both types of  
141 governing equations by using FEM approach was proposed in Lin et al. (2016) to investigate the  
142 wave-induced seabed instability (liquefaction potential) in the neighbourhood of partially/fully  
143 buried pipeline. Liu et al. (2007) were first to develop a soil solver in OpenFOAM based on the  
144 discretised Biot's equation, using FVM for the estimation of wave-induced seabed response  
145 surrounding submerged structure. However, this coupled model could not run in a parallel manner as  
146 demonstrated in Liu et al. (2007). An extension of poro-elastic model to poro-elasto-plasticity soil  
147 model was proposed and implemented in OpenFOAM in Tang (2014), Tang and Hededal (2014), and  
148 Tang et al. (2015). In Li et al. (2018) this proposed model was used to investigate the wave-induced  
149 momentary liquefaction in the vicinity of gravity-based structure considering the linear elastic  
150 structure response of the foundation. For the research on wave-induced seabed response around  
151 single/multi-cylinder foundations, Chang and Jeng (2014) performed a numerical investigation of the  
152 seabed instability close to a high-rising structure foundation, and concluded that the replacement of  
153 surrounding soil layer with a coarse sand layer with greater permeability was a sufficient protection  
154 from potential liquefaction. Most recently, by integrating FUNWAVE (Wei et al., 1999; Shi et al.,  
155 2001; Kirby et al., 2003) and fully dynamic (FD) form of Biot's equations, Sui et al. (2016)  
156 discussed the dynamic soil response caused by small steepness wave. It was concluded that the  
157 dynamic behaviour of a porous seabed and a mono-pile were all governed by fully dynamic form of  
158 Biot's equations. Lin et al. (2017) proposed a one-way integrated model solving both wave and soil  
159 model in OpenFOAM to investigate the nonlinear wave-induced soil response around a  
160 large-diameter mono-pile foundation. It was concluded that increasing penetration depth of  
161 mono-pile foundation resulted in the decrease of the maximum liquefaction depth around foundation.  
162 Recently, the investigation in Zhang et al. (2017) concluded that the existence of upstream piles in an  
163 offshore platform may reduce the wave velocity when it approaches downstream piles. Moreover,  
164 Tong et al. (2017) suggested that the existence of upstream pile may reduce the wave-induced seabed  
165 response near the downstream pile in a twin pile group. Though many studies have been conducted  
166 to examine the wave-induced soil response of a porous seabed around various coastal/offshore  
167 structures, the soil dynamics in a porous seabed in a multi-cylinder foundation subject to storm wave  
168 has not yet been fully understood. A very recent work on the coupled Fluid-Structure-Seabed model

169 has been proposed by Duan et al. (2019), who used IHFOAM and  $u$ - $p$  approximation for the  
 170 investigation of the seabed response near mono-pile foundation in combined wave-current  
 171 environment.

172

173 This study focuses on the near-trapping effects on dynamic seabed response and liquefaction close to  
 174 a multi-cylinder foundation in storm wave condition, which has not been studied yet. The segregated  
 175 FVM solver proposed in Lin et al. (2017), which incorporates waves2Foam and Biot's equations, is  
 176 adopted here and further applied to investigate the unknown issue of storm wave-induced soil  
 177 response around a multi-cylinder foundation. The governing equations for wave and seabed model  
 178 are described in the Section 2. In Section 3, the simulation of near-trapping phenomenon is validated  
 179 in detail against available experimental results. Section 4 discusses the distribution of wave pressure,  
 180 free surface elevation, and liquefaction depth in the vicinity of multi-cylinder structure under two  
 181 incident wave headings and compares these results with those obtained for a single cylinder. The  
 182 main conclusions are summarized in Section 5.

183

## 184 2. Numerical model

185 Two numerical domains are used in the present study, one for incident wave at  $0^\circ$ , as shown in Figure  
 186 1, and another one for  $45^\circ$ , as shown in Figure 2. Each numerical domain has two sub-domains,  
 187 namely a two-phase fluid flow domain (including water and air) and a porous seabed domain. The  
 188 two-phase fluid flow domain above the seabed is simulated using waves2Foam (Jacobsen et al.,  
 189 2012), while the porous seabed behaviour is governed by Quasi-Static (QS) Biot's model. The two  
 190 sub-models are integrated through the extended General Grid Interpolation (GGI), which  
 191 incorporates the interpolation of the face and point from zone to zone in terms of non-matched mesh  
 192 at the interface of flow and seabed sub-domain (Tuković et al., 2014).

193

### 194 2.1 Wave model

195 The two-phase flow above the seabed surface is simulated by the following mass and momentum  
 196 equations together with a free-surface tracing function, namely Volume of Fluid (Hirt and Nichols,  
 197 1981; Berberović et al., 2009)

$$\nabla \cdot \mathbf{u} = 0 \quad (1)$$

$$\frac{\partial \rho \mathbf{u}}{\partial t} + \nabla \cdot (\rho \mathbf{u}) \mathbf{u}^T = -\nabla p^* - (\mathbf{g} \cdot \mathbf{x}) \nabla \rho + \nabla \cdot (\mu \nabla \mathbf{u}) \quad (2)$$

$$\frac{\partial \alpha}{\partial t} + \nabla \cdot \mathbf{u} \alpha + \nabla \cdot \mathbf{u}_r \alpha (1 - \alpha) = 0 \quad (3)$$

198 where  $\mathbf{u}$  is the flow velocity;  $\rho$  is the density of fluid;  $t$  is the time;  $p^* = p - \rho \mathbf{g} \cdot \mathbf{x}$  is the wave  
 199 pressure in excess of static pressure;  $\mathbf{g}$  is the gravitational acceleration;  $\mathbf{x}$  is the Cartesian  
 200 coordinate vector;  $p$  is the pressure;  $\mu$  is dynamic viscosity;  $\mathbf{u}_r = \mathbf{u}_w - \mathbf{u}_a$  is the relative flow  
 201 velocity vector ( $\mathbf{u}_w$  and  $\mathbf{u}_a$  are velocity of water and air phase, respectively, Berberović et al.,  
 202 2009);  $\alpha$  is the volume fraction function.  $\alpha = 1$  indicates the computational cell is occupied by  
 203 water, while  $\alpha = 0$  denotes that a cell is full of air, and the cell with water-air mixture has  
 204  $0 < \alpha < 1$ . The momentary fluid density and dynamic viscosity are obtained from following  
 205 equations:

$$\rho = \alpha\rho_w + \rho_a(1 - \alpha) \quad (4)$$

$$\mu = \alpha\mu_w + \mu_a(1 - \alpha) \quad (5)$$

206 where the sub-indices  $w$  and  $a$  correspond to water and air, respectively.

207

208 At the seabed, mono-pile surface, and lateral boundaries of numerical wave flume, the boundary  
 209 layer effects are not considered and hence slip boundary is adopted as boundary condition. This is  
 210 consistent with the study performed by Paulsen et al. (2014b). A pressure outlet condition is specified  
 211 at the atmospheric boundary on the top of the two-phase flow domain, where air and water can flow  
 212 out and zero-gradient is applied on the velocity vector fields, but only air can flow in, with a  
 213 fixed-value condition and water volume fraction being 0 (Chen et al., 2014). For the detailed  
 214 description of wave generation (inlet boundary) and wave absorption (outlet boundary) zone, the  
 215 reader is referred to Jacobsen et al. (2012).

216

## 217 2.2 Seabed model

218 In the hydraulically isotropic porous seabed, the wave-induced dynamic behaviour of soil is  
 219 governed by QS Biot's equations (Biot, 1941). The mass balance equation adopted in present study is

$$\nabla^2 p_p - \frac{\gamma_w n_s \beta_s}{k_s} \frac{\partial p_p}{\partial t} = \frac{\gamma_w}{k_s} \frac{\partial \varepsilon_s}{\partial t} \quad (6)$$

220 where  $p_p$  is the pore water pressure,  $\gamma_w$  is the unit weight of water,  $n_s$  is the porosity of soil, and  
 221  $k_s$  is the Darcy's permeability. The compressibility of pore fluid  $\beta_s$  and the volumetric strain  $\varepsilon_s$   
 222 are defined, respectively, as:

$$\beta_s = \frac{1}{K_w} + \frac{1 - S_r}{P_{w0}} \quad (7)$$

$$\varepsilon_s = \nabla \cdot \mathbf{v} = \frac{\partial u_s}{\partial x} + \frac{\partial v_s}{\partial y} + \frac{\partial w_s}{\partial z} \quad (8)$$

223 where  $K_w$  is the true bulk modulus of elasticity of water (taken as  $2 \times 10^9$  N/m<sup>2</sup>, Yamamoto et al.,  
 224 1978);  $S_r$  is the saturation degree of soil;  $P_{w0}$  is the absolute pore water pressure;  $\mathbf{v} = (u_s, v_s, w_s)$   
 225 is the vector of soil displacement.

226

227 The force equilibrium equation for a poro-elastic seabed can be expressed as:

$$G \nabla^2 \mathbf{v} + \frac{G}{1 - 2\nu} \nabla \varepsilon_s = \nabla p_p \quad (9)$$

228 where  $G$  is the shear modulus of soil in relation to Young's modulus ( $E$ ) and Poisson's ratio ( $\nu$ ):

$$G = \frac{E}{2(1 + \nu)} \quad (10)$$

229

230 The stress-strain relationships for a poro-elastic seabed can be determined on the basis of Hooke's  
 231 law as

$$\sigma'_x = 2G \left( \frac{\partial u_s}{\partial x} + \frac{\nu}{1-2\nu} \varepsilon_s \right), \quad \sigma'_y = 2G \left( \frac{\partial v_s}{\partial y} + \frac{\nu}{1-2\nu} \varepsilon_s \right) \quad (11)$$

$$\sigma'_z = 2G \left( \frac{\partial w_s}{\partial z} + \frac{\nu}{1-2\nu} \varepsilon_s \right), \quad \tau_{xy} = \tau_{yx} = G \left( \frac{\partial u_s}{\partial y} + \frac{\partial v_s}{\partial x} \right) \quad (12)$$

$$\tau_{xz} = \tau_{zx} = G \left( \frac{\partial u_s}{\partial z} + \frac{\partial w_s}{\partial x} \right), \tau_{yz} = \tau_{zy} = G \left( \frac{\partial v_s}{\partial z} + \frac{\partial w_s}{\partial y} \right) \quad (13)$$

232 where  $\sigma'_i$  is effective normal stress,  $\tau_{ij}$  is shear stress, the subscripts  $i,j=x,y,z$  denote the directions  
 233 of Cartesian coordinates.

234

235 To solve QS Biot's equations, the following boundary conditions are prescribed at the boundaries of  
 236 porous seabed domain and cylinder surface. The upper boundary of seabed domain, namely seabed  
 237 surface ( $y=0$  in Figure 2 and Figure 3), is the pressure boundary with the pore water pressure,  $p_p$ ,  
 238 equal wave pressure,  $p^*$ . Furthermore, the vertical shear stresses and effective normal stress are set  
 239 as 0 at the seabed surface:

$$\sigma'_y = \tau_{xy} = \tau_{yz} = 0, p_p = p^* \text{ at } y = 0 \quad (14)$$

240

241 The bottom of seabed ( $y = -h_s$ , where  $h_s$  is the soil depth, Figure 2 and Figure 3) is selected as an  
 242 impermeable rigid boundary, where no vertical flow and no soil displacement occur:

$$u_s = v_s = w_s = \frac{\partial p_p}{\partial y} = 0 \text{ at } y = -h_s \quad (15)$$

243

244 The lateral boundaries of seabed domain are set as impermeable rigid boundaries (Chang and Jeng,  
 245 2014):

$$u_s = v_s = w_s = 0, \frac{\partial p_p}{\partial x} = 0 \text{ at } x = 0 \text{ and } x = L_s \quad (16)$$

$$u_s = v_s = w_s = 0, \frac{\partial p_p}{\partial z} = 0 \text{ at } z = -W_s/2 \text{ and } z = W_s/2 \quad (17)$$

246

247 The sizes of both flow and seabed domain are designed with sufficient length ( $L_s$ ) and width ( $W_s$ ) to  
 248 eliminate the effect from lateral boundaries. Ye and Jeng (2012) suggested that the length of seabed  
 249 domain should be more than double wavelength to avoid the effect of lateral boundaries on the  
 250 simulation results within zone of interest, so  $L_s$  and  $W_s$  are taken as 4.5 times the wavelength ( $L_w$ )  
 251 and 16 times the diameter of cylinder ( $D$ ). The centres of two different layouts of four cylinders in  
 252 Figure 2 and Figure 3 and the centres of both flow and seabed domains coincide, so the simulation  
 253 results around cylinders are not affected by the lateral boundary conditions. In addition, the cylinders  
 254 are assumed to be rigid impermeable objects and their surfaces are treated as no-flow boundary  
 255 conditions with zero pore water pressure gradient:

$$\frac{\partial p_p}{\partial \mathbf{n}} = 0 \quad (18)$$

256 where  $\mathbf{n}$  is the direction normal to the surface of a cylinder. No-flow boundary condition is  
 257 generally adopted for the surface of rigid object buried/penetrated into a porous seabed (Chang and  
 258 Jeng, 2014; Lin et al., 2016). Therefore, the interaction between soil and cylinder foundation, which  
 259 is caused by the fluid-induced cylinder vibration, is not considered here. For the related works  
 260 considering two-way coupled soil-structure interactions, readers are referred to Tong et al. (2019).

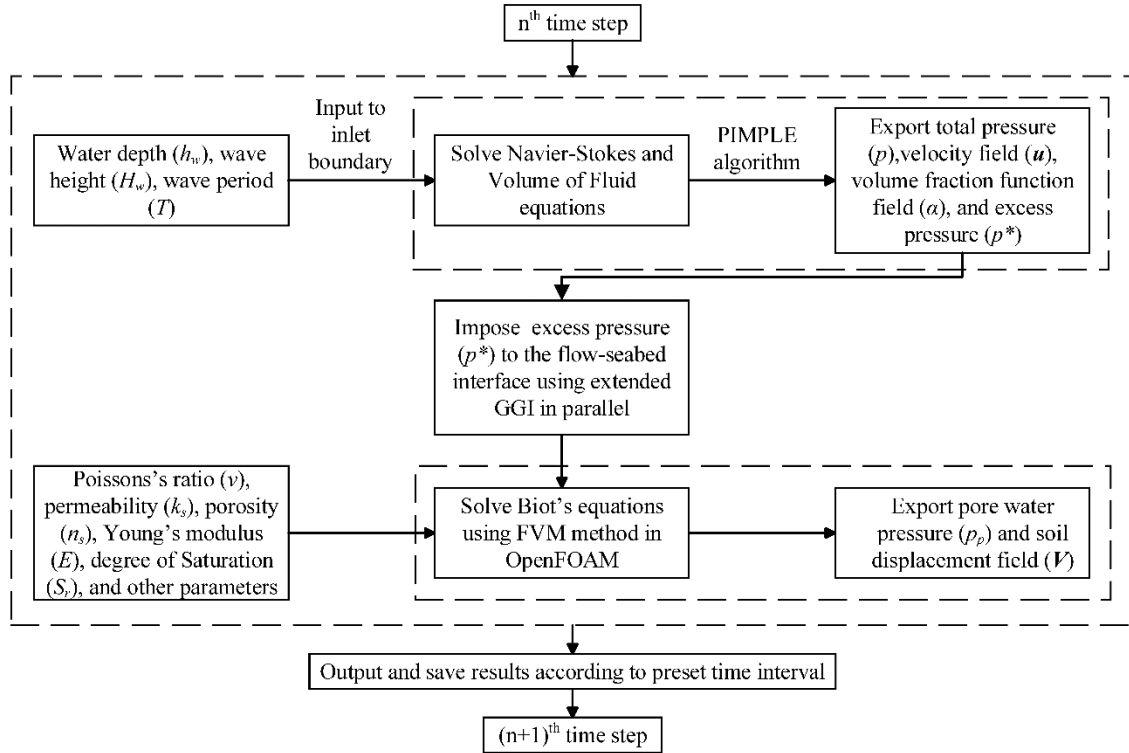


Figure 1 Integrated process of WSSI model

261

262 2.3 Integrated process between wave and seabed model

263 The aforementioned sub-models are integrated through one-way process, as shown in Figure 1.  
 264 Within one time step the integrated model solves the wave and seabed models individually: the  
 265 dynamic wave pressure ( $p^*$ ) at the flow-seabed interface calculated by the wave model  
 266 (waves2Foam) is imposed as the boundary condition to the seabed model by using extended general  
 267 grid interpolation (GGI) in parallel (Tuković et al., 2014). The detailed interpretation of integration  
 268 process can be found in Lin et al. (2017). In the present study, the adjustable time step for both flow  
 269 and seabed model is determined by Courant-Friedrichs-Lewy (CFL) condition with the value of 0.5.

270

271

Table 1 Wave and cylinder parameters for validation

Experiments	Case	Wave amplitude, $A$ (m)	Wave period, $T$ (s)	Water depth, $h_w$ (m)	Cylinder diameter, $D$ (m)	$k_w r$	$k_w A$
Ohl et al. (2001b)	1	0.0925	1.25	2	0.406	0.524	0.238
	2	0.049					0.126
	3	0.0589	1.326	2	0.406	0.465	0.135

Note:  $k_w$  is wave number;  $r$  is cylinder radius.

272

273 **3. Validation**

274 The wave and soil components of the present integrated model have been validated for a mono-pile  
 275 in Lin et al. (2017). In this section, the cases with an array of four cylinders are validated against the  
 276 available experimental data for the two layouts shown in Figure 2 and Figure 3 with  $0^\circ$  and  $45^\circ$



277 incident waves, respectively. The parameters for validation are listed in Table 1, where  $A$  is wave  
 278 amplitude,  $T$  is wave period,  $D$  is cylinder diameter,  $k_w$  is wave number, and  $r$  is cylinder radius. For  
 279 the validation of the soil model, readers are referred to Lin et al. (2017). Hence in this section, only  
 280 the capability of the wave model to simulate the free surface elevation due to wave interaction with  
 281 four cylinders is investigated.  
 282

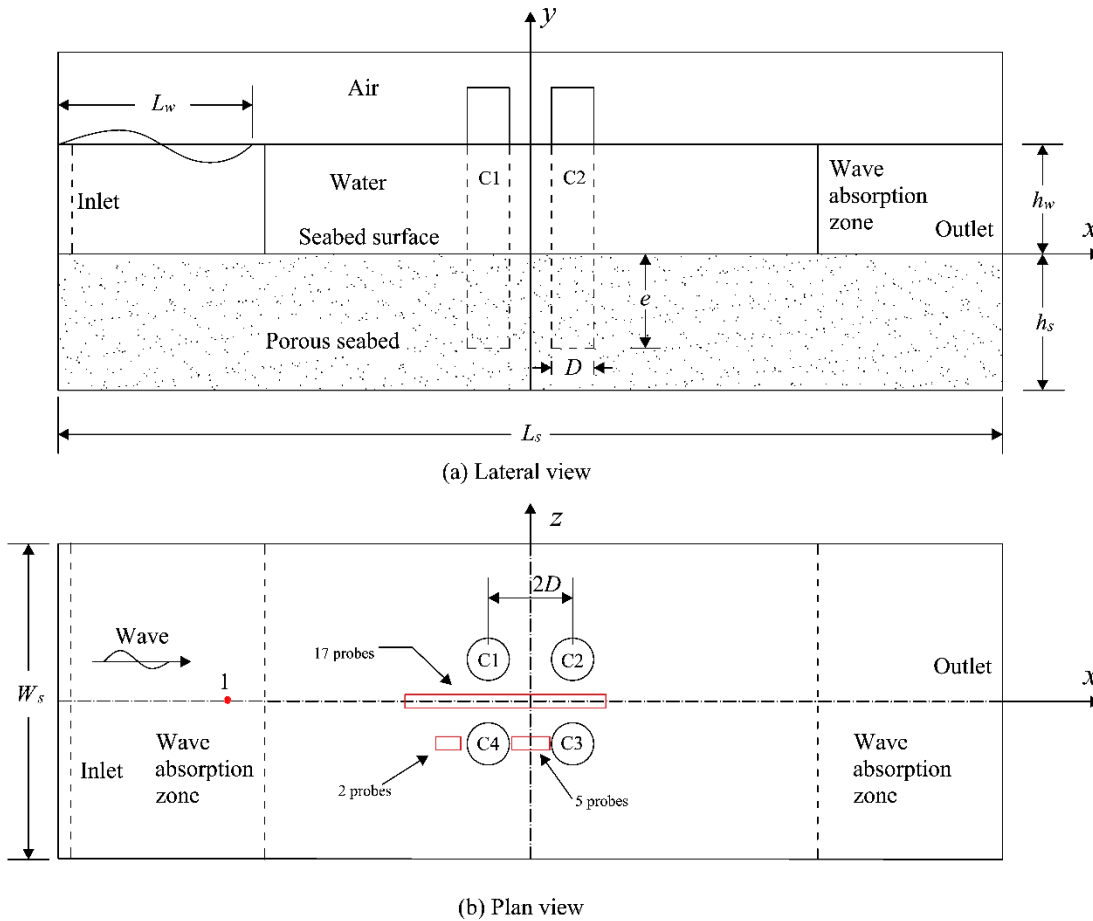


Figure 2 Sketch of the numerical wave tank with  $0^\circ$  incident wave. (a) Lateral view, (b) Plan view; the red dot 1 in plan view is the wave probe for measuring incident wave; the red rectangular zones are locations of other wave probes.

283

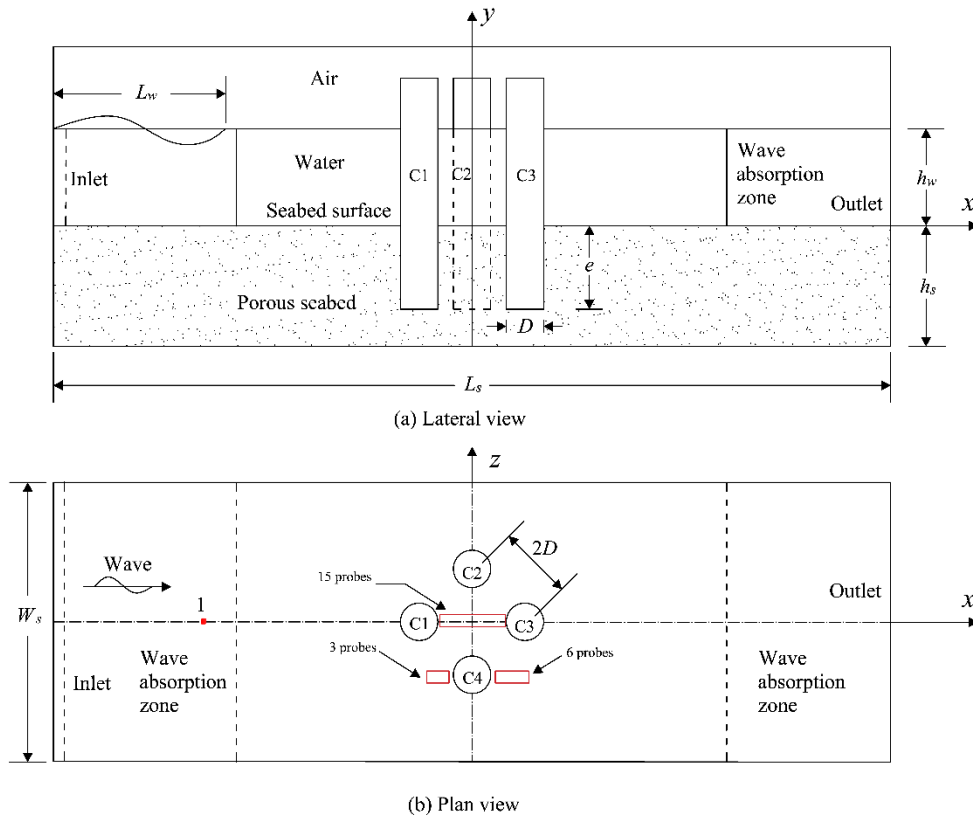


Figure 3 Sketch of the numerical wave tank with  $45^\circ$  incident wave. (a) Lateral view, (b) Plan view; the red dot 1 in plan view is the wave probe for measuring the incident wave; the red rectangular zones are locations of other wave probes.

284

285 The wave with two incident angles ( $0^\circ$  and  $45^\circ$ ) is considered. The experimental results performed in  
 286 Ohl et al. (2001a) are used to validate free surface elevation surrounding an array of closely placed  
 287 cylinders, where the space between the centres of two neighbouring cylinders is  $2D$ . The overall  
 288 configurations of 3-D numerical domains are the same as those in Figure 2 and Figure 3, except that  
 289 the soil subdomain is excluded, because it was not present in the experiments. The locations of wave  
 290 probes are listed in Table 2. Near-trapping phenomenon is investigated for several different types of  
 291 regular waves, including high and low steepness wave (see Table 1). The still water level and the  
 292 diameter of the individual cylinders are 2m and 0.406m, respectively. In accordance with the studies  
 293 of mesh sensitivity conducted in Paulsen et al. (2014b), the mesh for flow domain is refined to at  
 294 least a resolution of 15 points per wave height for validations and further applications.

295

296 The first validation of wave model is carried out with Case 3 ( $A = 0.0589$  m,  $T = 1.325$  s) and the  
 297 comparisons between simulated and experimental results are presented in Figure 4 for two incident  
 298 regular waves ( $0^\circ$  and  $45^\circ$ ). It can be seen in Figure 4(a) that the free surface elevation ( $\eta$ ) of the  
 299 incident wave is in a fairly good agreement with the experimental result in an empty wave tank  
 300 without any cylinders. For experiments/simulations with an array of cylinders the comparison in  
 301 Figure 4(b) shows the simulated free surface elevation with  $0^\circ$  heading wave at wave probe A9  
 302 agrees well with the experimental data, except for the slight discrepancy of the amount of water

303 merging after each wave crest and before the wave trough. It can be seen in Figure 5 that the small  
 304 jump between wave crest and trough is caused by the small amount of water propagating from  
 305 downstream to upstream. This small amount of water continues to propagate from the centre of the  
 306 array to wave gauge A9, and merges with incoming wave trough, leading to the smaller free surface  
 307 elevation at wave gauge A9. In Figure 4(c), the same experimental data at wave probe A9 are  
 308 compared with the simulated results at the centre of array ( $x=0, z=0$ ), which is only 0.05m away from  
 309 A9, measured along the central line in the upstream direction. Figure 4(c) demonstrates that a slight  
 310 shifting of the observation point yields a better agreement at the aforementioned discrepancy.

311  
 312

Table 2 Wave probe locations in Figure 2 and Figure 3

Probe ( $0^\circ$ )	$x$ (m)	$z$ (m)	Probe ( $45^\circ$ )	$x$ (m)	$z$ (m)
1	-4.5	0	1	-4.5	0
B10	-1.15	0	D9	-0.35	0
B9	-1.05	0	E6	-0.3	0
B8	-0.95	0	D8	-0.25	0
B7	-0.85	0	E5	-0.2	0
B6	-0.75	0	D7	-0.15	0
B5	-0.65	0	E4	-0.1	0
B4	-0.55	0	D6	-0.05	0
B3	-0.45	0	D5	0	0
A12	-0.35	0	D4	0.05	0
A11	-0.25	0	E3	0.1	0
A10	-0.15	0	D3	0.15	0
A9	-0.05	0	E2	0.2	0
A8	0.05	0	D2	0.25	0
A7	0.15	0	E1	0.3	0
A6	0.25	0	D1	0.35	0
A5	0.35	0	D12	-0.325	-0.575
A4	0.45	0	D11	-0.275	-0.575
B12	-0.765	-0.407	D10	-0.225	-0.575
B11	-0.665	-0.407	E12	0.22	-0.575
B2	-0.15	-0.407	E11	0.32	-0.575
B1	-0.05	-0.407	E10	0.37	-0.575
A3	0.05	-0.407	E9	0.42	-0.575
A2	0.1	-0.407	E8	0.47	-0.575
A1	0.15	-0.407	E7	0.52	-0.575

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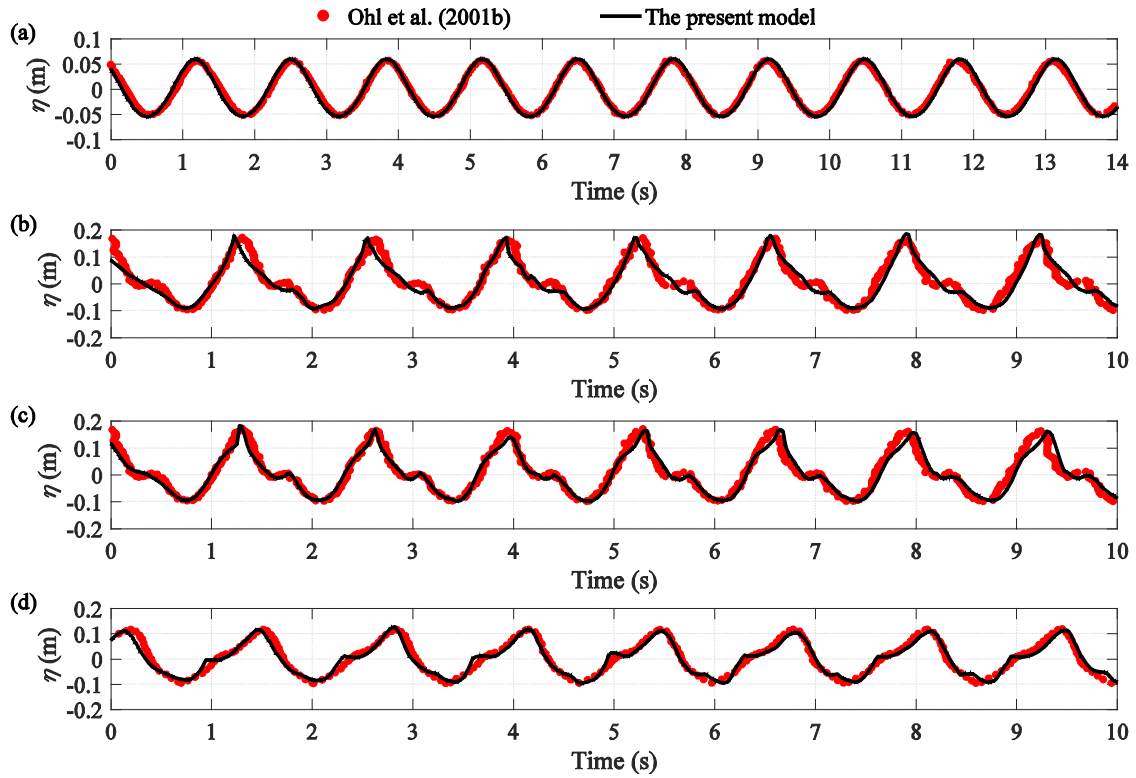
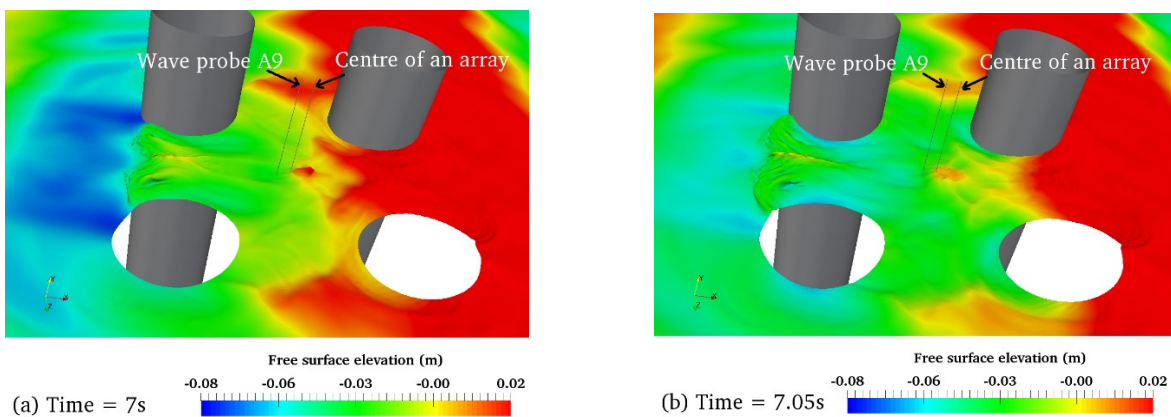


Figure 4 Time history of free surface elevation ( $\eta$ ) of simulated and experimental results (Case 3 in Table 1). (a) Wave probe 1; (b) Wave probe A9 with  $0^\circ$  heading; (c) Centre of an array ( $x=0$  and  $z=0$ ) with  $0^\circ$  heading; (d) Wave probe E2, with  $45^\circ$  heading.

315

316 For a  $45^\circ$  heading wave with same parameters as  $0^\circ$  heading, the simulated and experimental results  
 317 are compared in Figure 4(d), where a generally good agreement is demonstrated, with just a minor  
 318 discrepancy before the arrival of individual wave crest. Comparison of the magnitude of both  
 319 simulated and experimental results in Figure 4(b-d) with those for incident wave in Figure 4(a)  
 320 shows that significant amplifications of the magnitude of both wave crest and wave trough resulted  
 321 from wave-cylinders interaction. This amplification process of free surface elevation is termed  
 322 near-trapping phenomenon. On the basis of above validations, it can be concluded that the  
 323 developments of free surface elevation at typical locations within an array of cylinders are well  
 324 predicted by numerical simulations.



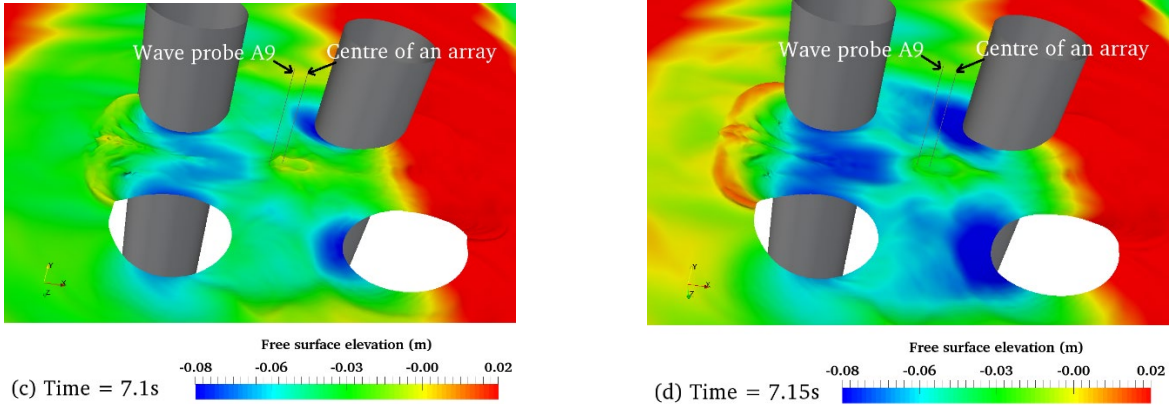


Figure 5 Snapshots of free surface elevation ( $\eta$ ) at different moments for Case 3 in Table 1. (a) Time = 7s; (b) Time = 7.05s; (c) Time = 7.1s; (d) Time = 7.15s.

325

326 Further validations of wave model results for free surface elevation in the vicinity of cylinders are  
 327 performed in frequency domain. For this purpose the time history of simulated results at various  
 328 locations of wave probes indicated in Figure 2 and Figure 3 are processed by Fast Fourier  
 329 Transforms (FFTs). The same processing procedure and approach used in Ohl et al. (2001a) are  
 330 adopted here to extract the spectral peaks at single ( $f = f_i$ ,  $f_i$  is incident wave frequency), double ( $f =$   
 331  $2f_i$ ), triple ( $f = 3f_i$ ) incident wave frequencies, and all spectral components within the range of  
 332 ( $f \pm 0.25f_i$ ). These separated frequency components are termed first-, second-, and third-order  
 333 harmonics, respectively. After that, each separated spectral component is further processed by  
 334 Inverse FFTs (IFFTs) to obtain the corresponding time series, from which mean values of all the  
 335 peaks are computed and compared with those for data measured at various locations of wave probes.

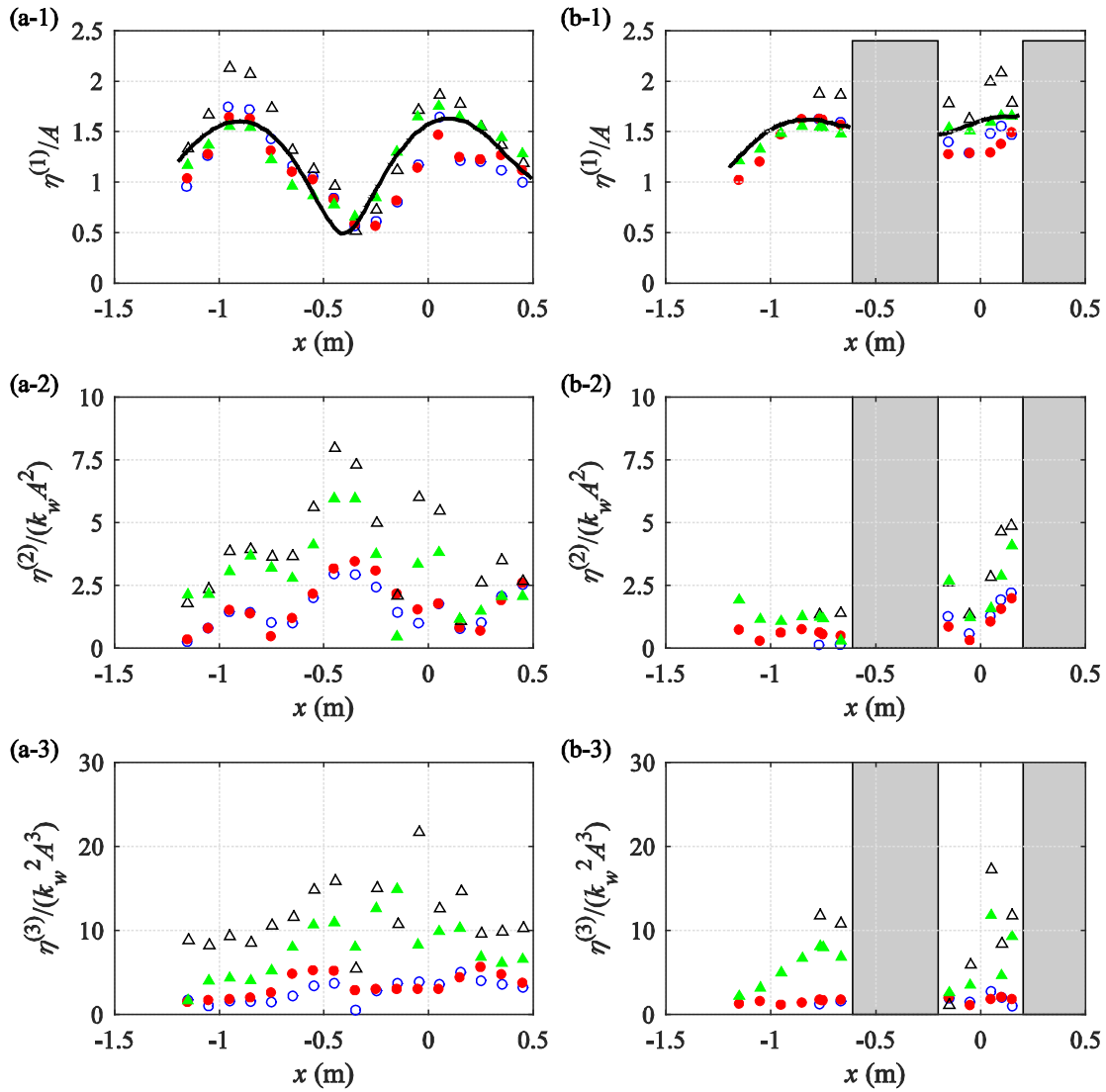


Figure 6 Comparison between simulated and experimental results of Case 1 and Case 2 with  $0^\circ$  heading. (1) First-order harmonics; (2) Second-order harmonics; (3) Third-order harmonics. (a) and (b) indicate the probes at central and lateral sides, respectively.  $\circ$ : case 1 in Ohl et al. (2001b);  $\Delta$ : case 2 in Ohl et al. (2001b);  $\bullet$ : case 1 of present model;  $\blacktriangle$ : case 2 of present model;  $\text{—}$ : analytical solutions of Linton and Evans (1990).

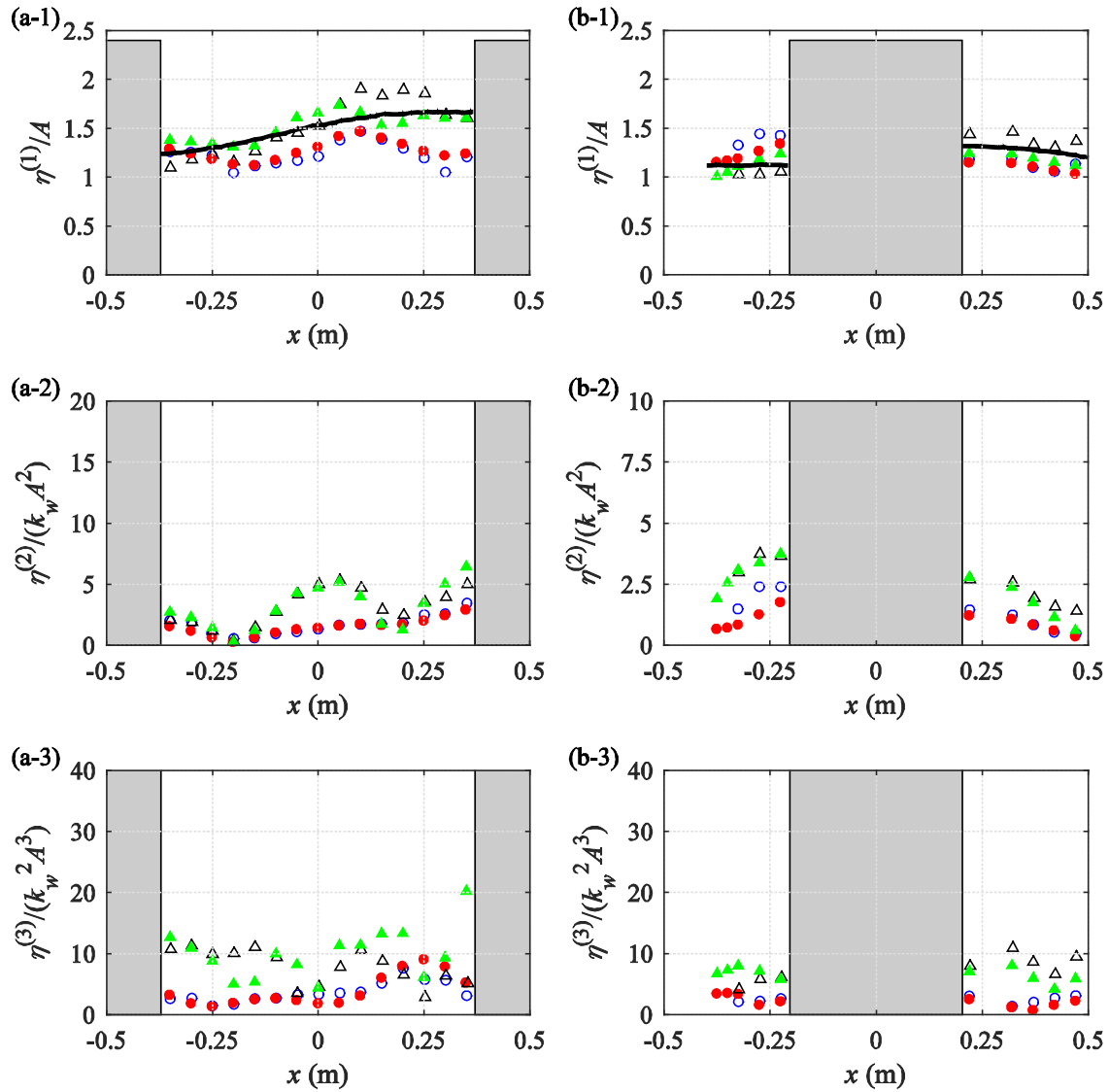


Figure 7 Comparison between simulated and experimental results for Case 1 and Case 2 with 45° heading. (1) First-order harmonics; (2) Second-order harmonics; (3) Third-order harmonics. Columns (a) and (b) indicate the probes at central and lateral sides, respectively.  $\circ$ : case 1 in Ohl et al. (2001b);  $\Delta$ : case 2 in Ohl et al. (2001b);  $\bullet$ : case 1 of present model;  $\blacktriangle$ : case 2 of present model;  $\text{—}$ : analytical solutions of Linton and Evans (1990).

337

338 On the basis of aforementioned post-processing, additional comparisons of different order harmonics  
 339 at various locations, up to third-order, are presented in Figure 6 for 0° incident angle and in Figure 7  
 340 for 45° angle. The wave parameters of each validation case can be found in Table 1. For 0° heading  
 341 (Figure 6) there are some discrepancies for Case 2 with smaller steepness wave, whereas the  
 342 agreement for the Case 1 with greater steepness wave is much better. For the incident wave with 45°  
 343 heading (Figure 7) there is good agreement for both Case 1 and Case 2. In both Figure 6 and Figure 7,  
 344 the Case 1 with greater steepness wave has a better agreement with experimental results, rather than  
 345 Case 2 with small wave steepness. From the comparisons of first-order component in Figure 6 and  
 346 Figure 7, the evident amplification of free surface elevation, also named near-trapping phenomenon,

347 can be noticed along the central line and at lateral sides of four cylinders. Overall, it can be  
 348 concluded that the near-trapping phenomenon has been well captured in the present numerical model  
 349 that can be used to investigate dynamic seabed response around an array of cylinders.

350

#### 351 4. Applications

352 Cylinder foundations supporting offshore wind turbines or platforms are usually protected from the  
 353 onset of scour. When exposed to harsh ocean environments, scour protections surrounding cylinder  
 354 foundations are vulnerable to liquefaction. However, the studies concerning liquefaction potential in  
 355 the vicinity of closely placed cylinder foundations have not been reported yet. The previous  
 356 investigation in Lin et al. (2017), performed for the wave condition from the Danish ‘Wave loads’  
 357 project (Paulsen et al., 2014b), with  $KC = 8.85$ , and  $k_w D = 0.2$ , revealed that the maximum  
 358 wave-induced liquefaction depth in the vicinity of a mono-pile foundation may occur at the lateral  
 359 sides of the cylinder. In order to study liquefaction in the vicinity of an array of circular cylinders in  
 360 storm wave conditions and compare it with the results for the single cylinder case, the same wave  
 361 condition as in Lin et al. (2017) is adopted in the present study. The remaining parameters of incident  
 362 wave used in present application are given in Table 3, with  $k_w A$  being 0.14 in all simulations, and  
 363  $k_w D$  ranging from 0.2 to 0.43. A constant  $k_w A$  value and varying  $k_w D$  values were adopted because of  
 364 the results of Cong et al. (2015), who showed that near-trapping phenomenon is insensitive to  $k_w A$ ,  
 365 but highly sensitive to  $k_w D$ . The soil parameters used in this study are listed in Table 4. For the  
 366 studies of varying soil parameters, readers are referred to Chang and Jeng (2014) for details.  
 367 Individual cylinders are assumed to be rigid objects, and the movement of the cylinder foundations is  
 368 not simulated. Two layouts of four cylinders investigated in this section are shown in Figure 2 and  
 369 Figure 3. The location of a point along the perimeter of a cylinder is defined by its angle  $\theta$ , as shown  
 370 in Figure 8.

371

372

Table 3 Wave properties for the investigation of wave-cylinders-seabed interaction

Case	Wave amplitude, $A$ (m)	Wave period, $T$ (s)	Wave length, $L_w$ (m)	$k_w D$	Water depth, $h_w$ (m)
1	2.43	9.2	108.45	0.35	
2	2.88	10.5	129.12	0.29	
3	3.425	12.05	153.12	0.25	20
4	4.215	13.6	188.5	0.2	
5	1.94	7.88	86.79	0.43	

373

374

Table 4 Parameters for seabed and cylinders

Seabed characteristics			
Seabed thickness, $h_s$ (m)	38	Poisson’s ratio, $\nu$	0.4
Young’s modulus, $E$ (Pa)	$2.8 \times 10^8$	Permeability, $k$ (m/s)	$1 \times 10^{-4}$
Degree of saturation, $S_r$	0.98	Soil porosity, $n_s$	0.38
Cylinder characteristics			
Diameter, $D$ (m)	6	Penetration depth, $e$ (m)	18



375  
376

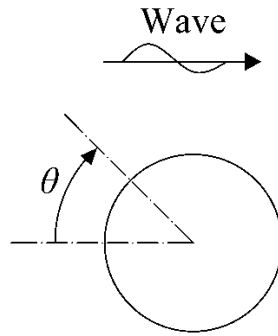


Figure 8  $\theta$ -location around a cylinder

377

378 **4.1 Liquefaction development around cylinders in an array**

379 Momentary liquefaction can take place at a point at a depth  $L_d (= -y)$  beneath the seabed surface  
 380 when the difference between the pore pressure at this level,  $p_p$ , and the pressure on a seabed surface  
 381 above the point,  $P_b$ , becomes sufficiently large to balance or even exceed the overburden soil weight  
 382 per unit area. As a result soil matrix becomes incapable of carrying any load and momentary  
 383 liquefaction occurs. This process contributes to the scour around a cylinder founded in a sand bed  
 384 (Tonkin et al., 2003). It should be noted that both the  $p_p$ , and  $P_b$  denote pressure in excess of  
 385 hydrostatic pressure, so that the overburden soil weight is reduced by the buoyancy force. Due to the  
 386 assumptions that the cylinder is hollow instead of solid, and the vibration of the cylindrical  
 387 foundations is not taken into account, the liquefaction criterion is (Jeng, 2013; Sumer, 2014):

$$(\gamma_s - \gamma_w)L_d \leq p_p - P_b \quad (19)$$

388 with  $\gamma_s$  and  $\gamma_w$  denoting seabed and water unit weight, respectively. In present study,  $\gamma_s = 1.9 \gamma_w$   
 389 is used to evaluate the weight of the overburden soil.

390

391 In this section, the development of liquefaction in the proximity of individual cylinders in an array is  
 392 analysed for Case 2 with wave period  $T = 10.5$  s (Table 3). The liquefaction depth has been evaluated  
 393 using criterion (19). Results for each cylinder at the outer surface 0.1m away from the cylinder  
 394 surface are shown in Figure 9 and Figure 10. In order to show the amplification of liquefaction  
 395 induced by near-trapping phenomenon, the liquefaction depth ( $L_d$ ) near a four-cylinder foundation is  
 396 normalized by the single maximum liquefaction depth ( $L_{dmax}^{MP}$ ) around a mono-pile foundation in the

397 entire liquefaction zone, i.e. within  $-17.5m < x < 17.5m$  and  $-17.5m < z < 17.5m$ . The  $L_{dmax}^{MP}$  values of

398 all the single cylinder cases from Table 3 are listed in Table 5. Figure 9(a) and (b) indicate that for  $0^\circ$   
 399 wave heading there are two local minima of the liquefaction depth around both C1 and C2 cylinders,  
 400 occurring at  $\theta$  equal  $0^\circ$  and  $180^\circ$ , and two local maxima, at  $\theta$  equal  $90^\circ$  and  $270^\circ$ . Between these  
 401 local minima and maxima liquefaction depth near the cylinder varies monotonically – it increases  
 402 from  $\theta=0^\circ$  to  $\theta=90^\circ$ , decreases from  $\theta=90^\circ$  to  $\theta=180^\circ$ , and then repeats this cycle from  $\theta= 180^\circ$  to  
 403  $\theta=360^\circ$ . The liquefaction depth at the upstream end of cylinder, at  $\theta=0^\circ$ , is somewhat smaller for C2,

404 indicating a degree of sheltering by C1.

405

406

407 Table 5 the minimum free surface elevation ( $\eta_{\min}^{\text{MP}}$ ), the minimum pore water pressure ( $P_{b\min}^{\text{MP}}$ ) on the

408 seabed surface, and the maximum liquefaction depth ( $L_{d\max}^{\text{MP}}$ ) around a mono-pile foundation

Case	1	2	3	4
$\eta_{\min}^{\text{MP}}$ (m)	-2.84	-3.55	-4.97	-4.32
$P_{b\min}^{\text{MP}}$ (Pa)	$-1.42 \times 10^4$	$-1.90 \times 10^4$	$-2.00 \times 10^4$	$-2.40 \times 10^4$
$L_{d\max}^{\text{MP}}$ (m)	1.26	1.8	1.86	2

409

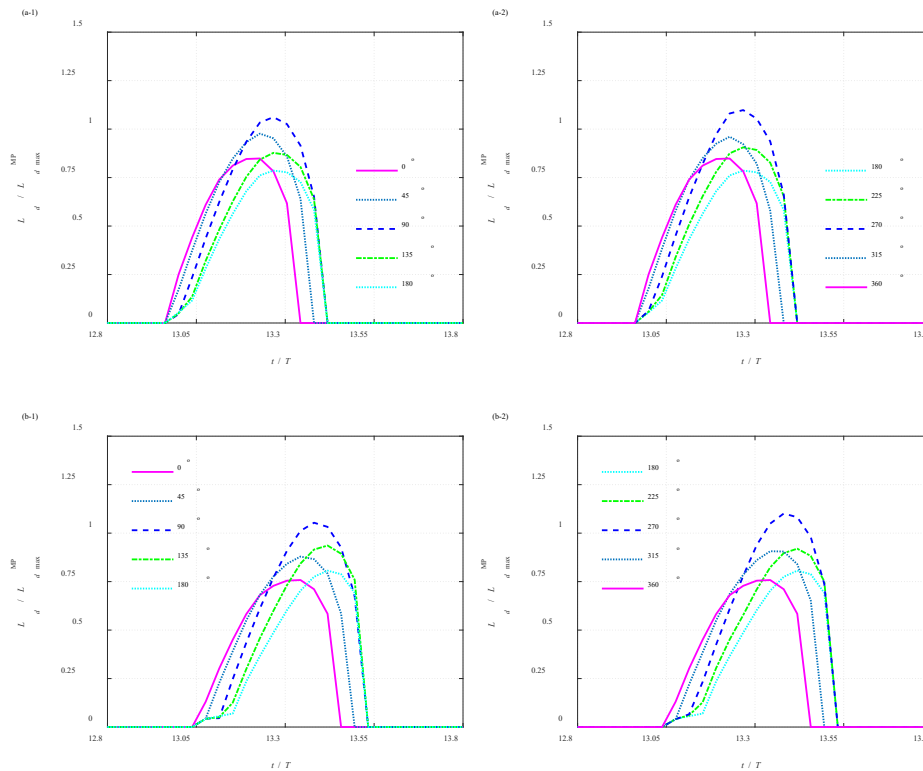


Figure 9 Development of liquefaction depth at various  $\theta$ -locations with  $0^\circ$  incident wave. (a) C1 cylinder; (b) C2 cylinder. Refer to Figure 8 for the definition of  $\theta$ , and to Figure 2 for the location of cylinders.

410

411 Development of liquefaction depth for  $45^\circ$  incident wave is shown in Figure 10. Owing to the  
 412 symmetry of liquefaction development along the lateral sides of C1 and C3 cylinders, results are  
 413 shown only for a half of their perimeter, from  $\theta=0^\circ$  to  $\theta=180^\circ$ , in Figure 10(a) and (b), respectively.  
 414 For the same reason results are presented along the entire perimeter for C2, but not for C4, where

415 they are identical. The overall development of liquefaction depth around the perimeter of each  
 416 individual cylinder is similar to that already seen for  $0^\circ$  heading wave. However, there is a notable  
 417 difference between the values of the local minima of liquefaction depth at  $\theta=0^\circ$  for cylinders C1 and  
 418 C3 – the former is much deeper than the latter, leading to the conclusion that the upstream end of C3  
 419 is protected by the three upstream cylinders. Comparison of the liquefaction development for groups  
 420 of cylinders (Figure 9 and 10) with that for mono-pile (Figure 11) shows that the maximum  
 421 momentary liquefaction depth in all cases takes place at  $\theta=90^\circ$  and the magnitudes of liquefaction  
 422 depth at all locations in both four-cylinder cases have been significantly amplified.  
 423

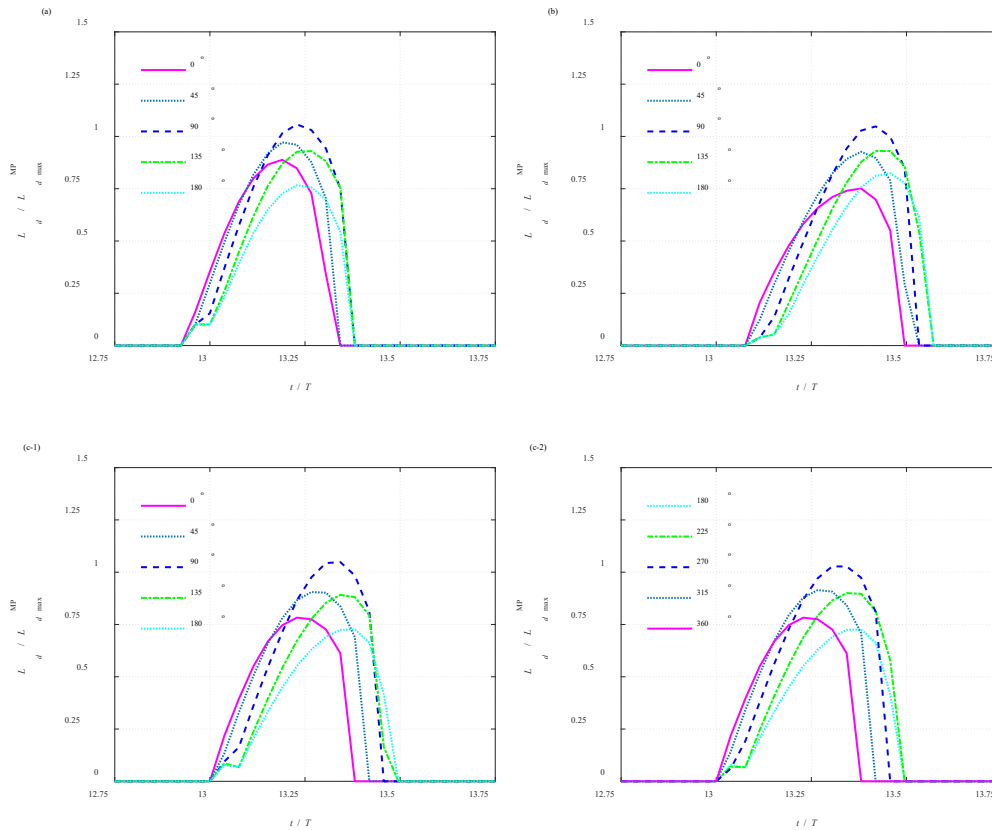


Figure 10 Development of liquefaction depth at various  $\theta$ -locations with  $45^\circ$  incident wave. (a) C1 cylinder; (b) C3 cylinder; (c) C2 cylinder. Refer to Figure 8 for the definition of  $\theta$ , and to Figure 3 for the location of cylinders.

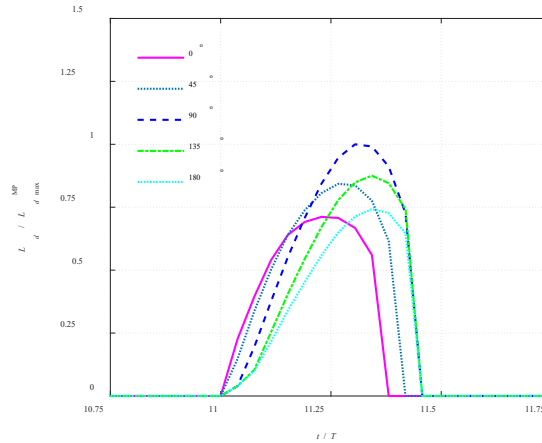


Figure 11 Development of liquefaction depth at various  $\theta$ -locations with a mono-pile foundation. Refer to Figure 8 for the definition of  $\theta$ .

424

#### 425 **4.2 Vertical distribution of pore water pressure around cylinders**

426 For momentary liquefaction, the primary cause is attributed to the difference between the pore water  
 427 pressure at seabed surface and a position beneath. As shown in section 4.1, the development of  
 428 liquefaction depth around each cylinder in a cylinder array has been amplified by the near-trapping  
 429 phenomenon of incident wave, which reduces the minimum free surface elevation during wave  
 430 passage, and decreases the minimum wave-induced pressure at the seabed, resulting in deeper  
 431 momentary liquefaction. In this section, in order to better understand the distribution of the  
 432 maximum liquefaction depth around the perimeter of each cylinder, the liquefaction depth is  
 433 estimated along an outer surface 0.1m away from cylinder surface at the moment when liquefaction  
 434 depth reaches its maximum, such as  $t/T= 13.3$  in Figure 9(a), and compared with those of a  
 435 mono-pile foundation. Liquefaction depths are shown in Figures 12, 13, and 14 on the top of the  
 436 contour plot of pore water pressure recorded at the same moment ( $p_p$ ), normalized with the minimum  
 437 pore water pressure ( $P_{bmin}^{MP}$ , listed in Table 5) on the seabed surface in a mono-pile foundation case.

438 The distribution of the liquefaction depth around the mono-pile perimeter is in qualitative agreement  
 439 with experimental results of Tonkin et al. (2003), who also found the deepest scour at the cylinder  
 440 side ( $\theta=90^\circ$ ), albeit for tsunami waves rather than non-linear periodic waves used in the present  
 441 study.

442

443 Figure 12 for  $0^\circ$  wave heading shows that the distributions of both pore water pressure and  
 444 liquefaction depth around C1 and C2 cylinders are non-symmetric, unlike distributions along a  
 445 mono-pile case foundation in Figure 13, which are symmetric with respect to  $\theta=180^\circ$ . A slightly  
 446 non-symmetric distribution of liquefaction depth and pore water pressure near C2 cylinder is also  
 447 indicated for  $45^\circ$  wave heading, in Figure 13(b), while these distributions near C1 and C3 cylinders  
 448 are symmetric. For both  $0^\circ$  and  $45^\circ$  incident wave cases the inner zone ( $180^\circ < \theta < 360^\circ$ ) towards the  
 449 centre of the cylinder array shows more significant liquefaction than that of the outer zone  
 450 ( $0^\circ < \theta < 180^\circ$ ), away from the cylinder array centre. Moreover, the overall liquefaction depth and pore  
 451 water pressure on seabed surface in the vicinity of each cylinder in a cylinder array are greater than

452 those around a mono-pile foundation. As stated earlier, this can be explained by the near-trapping  
 453 phenomenon induced by wave-cylinders interaction above the seabed.

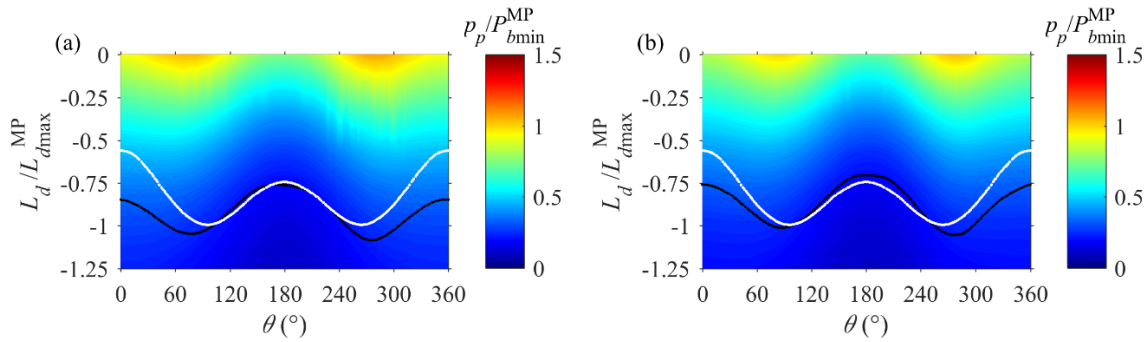


Figure 12 Pore water pressure and liquefaction depth for  $0^\circ$  incident wave along an outer surface at 0.1m distance from cylinder at the moment when the maximum liquefaction depth occurs. (a) C1 cylinder at  $t/T=13.3$ ; (b) C2 cylinder at  $t/T=13.4$ . Black line shows liquefaction depth around individual cylinders in a cylinder array and white line shows liquefaction depth around mono-pile foundation. Refer to Figure 8 for the definition of  $\theta$ , and to Figure 2 for the location of cylinders.

454

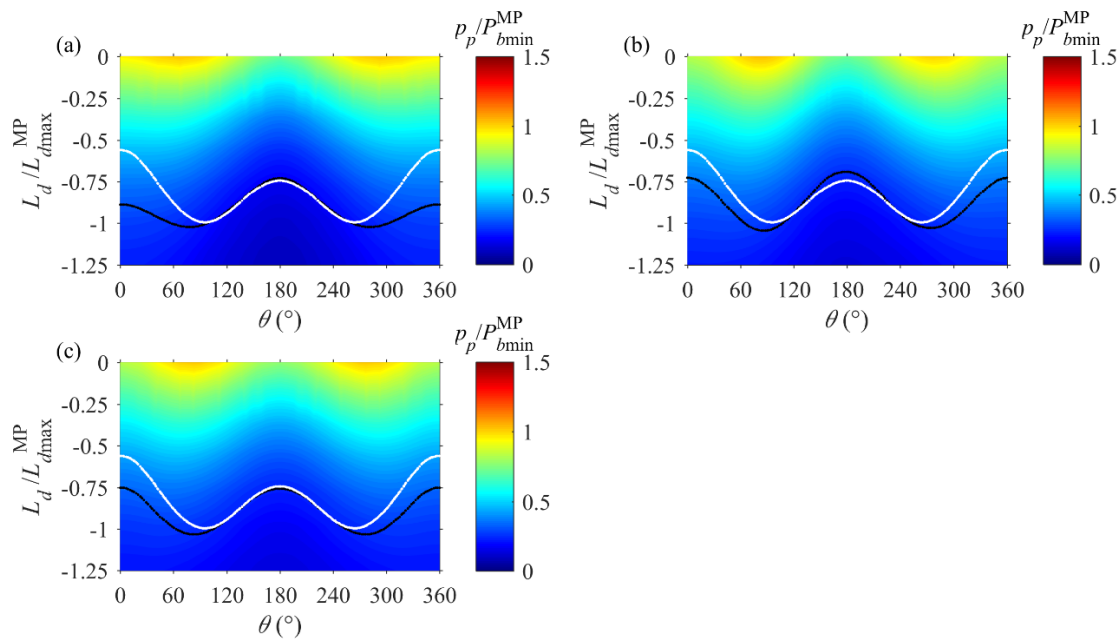


Figure 13 Pore water pressure and liquefaction depth for  $45^\circ$  incident wave along an outer surface at 0.1m distance from cylinder at the moment when the maximum liquefaction depth occurs. (a) C1 cylinder at  $t/T=13.3$ ; (b) C2 cylinder at  $t/T=13.37$ ; (c) C3 cylinder at  $t/T=13.45$ . Black line shows liquefaction depth around individual cylinders in a cylinder array and white line shows liquefaction depth around mono-pile foundation. Refer to Figure 8 for the definition of  $\theta$ , and to Figure 3 for the location of cylinders.

455

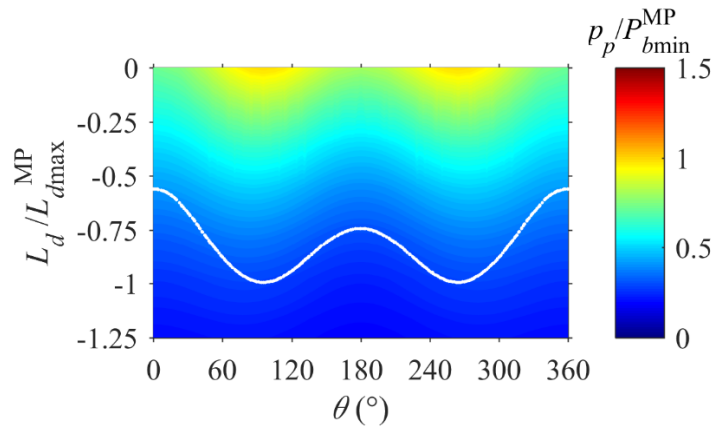


Figure 14 Pore water pressure and liquefaction depth along an outer surface at 0.1m distance from mono-pile foundation at the moment  $t/T=11.35$  when the maximum liquefaction depth occurs. White line shows liquefaction depth around mono-pile foundation. Refer to Figure 8 for the definition of  $\theta$ .

456

### 457 **4.3 Spatial distribution of the maximum values of liquefaction, pore water pressure on seabed** 458 **surface, and free surface elevation**

459 This section investigates the spatial distribution of the wave-induced liquefaction around individual  
 460 cylinders in an array. Figure 15 shows the spatial distribution (in  $x-z$  plane) of the maximum  
 461 liquefaction depth ( $L_d$ ) within a wave period (calculated from stable results after 8 wave periods) for  
 462 Case 1 to Case 4. As before the maximum liquefaction depth is normalized with the maximum  
 463 liquefaction depth ( $L_{dmax}^{MP}$ ) of a mono-pile foundation with the identical incoming wave. The

464 analogous post-processing is also applied to the minimum water pressure on the seabed surface ( $P_{bmin}$ )  
 465 and the minimum free surface elevation ( $\eta_{min}$ ), and the associated results are shown in Figure 16 and  
 466 Figure 17, respectively. Since liquefaction depth in the Case 5 with a mono-pile foundation is small,  
 467 the discussion of this case will be presented later, in section 4.5.

468

469 Comparison of the normalized maximum liquefaction depths for  $0^\circ$  and  $45^\circ$  incident waves with  
 470 those for a mono-pile foundation case (Figure 15) shows that the amplification factors for the  
 471 maximum liquefaction depth range approximately from 1.05 to 1.2. Moreover, under the action of  $0^\circ$   
 472 incident wave amplification of liquefaction depth is more noticeable (Figure 15a), then for  $45^\circ$   
 473 incident wave (Figure 15b), especially at the lateral sides of front cylinders (C1 and C4 for  $0^\circ$   
 474 incident wave, and C1 for  $45^\circ$  incident wave). The maximum momentary liquefaction zones are  
 475 located at the lateral sides of individual cylinders, and between the two front cylinders (C1 and C4)  
 476 for  $0^\circ$  incident wave. This agrees with Cong et al. (2015) who concluded that the amount of  
 477 incoming wave is trapped in the zone between C1 and C4 and the inner zone of a four-cylinder  
 478 structure is shielded without significant amplification. At the lateral sides of cylinders in Figure 15(a),  
 479 the decrease of  $k_w D$  from 0.35 (shorter wave) to 0.25 (longer wave) leads to the more significant  
 480 amplification on liquefaction depth, but for  $k_w D$  of 0.2 (Case 4) the amplification factor reduces to  
 481 approximately 1.05. A possible explanation is that due to the greater wave length in Case 4 the  
 482 four-cylinder group behaves as a unity. The distribution of liquefaction around a cylinder group is

483 therefore similar to that around a mono-pile foundation, where the smaller liquefaction depth is also  
484 shown in front of the cylinder array.

485

486 Figure 16 shows the spatial distribution of the minimum wave-induced pressure on seabed surface,  
487  $P_b$ . It is very similar to the distribution of the maximum liquefaction depth shown in Figure 15,  
488 indicating that reduction of  $P_b$  is the primary cause of the momentary liquefaction. The minimum  
489 seabed pressure  $P_b$  is in turn associated with the minimum free surface elevation, shown in Figure 17.  
490 However, although their general distribution is similar, free surface elevation seems to be more  
491 violent and contains higher-order harmonic components (Readers are referred to the Fig.8 and Fig.9  
492 in Lin et al. (2017) for the temporal comparisons of these three variables). This is because wave  
493 pressure attenuation with water depth is frequency dependent, so the attenuation of wave pressure for  
494 higher harmonic components is faster than that for lower frequency harmonics, hence higher order  
495 harmonic components attenuate between the water surface and the seabed surface and do not reach  
496 the latter. Consequently the near-trapping phenomenon of wave-induced pressure on seabed surface  
497 and the resulting momentary liquefaction are somewhat different from that of free surface elevation,  
498 which contains higher-order harmonic components. The spatial distribution of the minimum free  
499 surface elevation ( $\eta_{\min}$ ) in Figure 17 further confirms that the incident wave though trapped inside the  
500 cylinder array causes lower water levels within the inner zone compared with those outside.

501

502 To demonstrate the overall effect of the near-trapping on a cylinder group, and compare it with a  
503 mono-pile, the amplification factors averaged over the previously defined liquefaction zone ( $-17.5\text{m}$   
504  $< x < 17.5\text{m}$  and  $-17.5\text{m} < z < 17.5\text{m}$ ) are shown in Figure 18, together with the minimum and the  
505 maximum amplification factors. It can be seen that the average amplification factor does not linearly  
506 increase with the decrease of  $k_w D$  and the increase of wave period. The sudden increase of  
507 amplification factor at  $k_w D = 0.25$  ( $T = 12.05\text{s}$ ) is also confirmed by both experimental results and  
508 numerical simulation in Cong et al. (2015) for investigating the effect of near-trapping phenomenon,  
509 but the overall development of amplification factors tends to stabilize with the increase of wave  
510 period. It can be noticed that the developments of amplification factor with  $k_w D$  for liquefaction  
511 depth, wave pressure on seabed surface, and free surface elevation, follow similar patterns. Moreover,  
512 the amplification factors for liquefaction depth and wave pressure on seabed surface are similar,  
513 while the effect of the near-trapping phenomenon on free surface elevation is more pronounced. The  
514 incident wave for two different incident angles are found to be trapped in a four cylinder structure,  
515 and result in the noticeable amplification factor compared to that of a mono-pile case. For the  
516 incoming wave angles, it can be seen that the incident wave with  $0^\circ$  heading seems to be trapped  
517 easier than that of  $45^\circ$  headings and mono-pile case, leading to greater amplification factors.

518

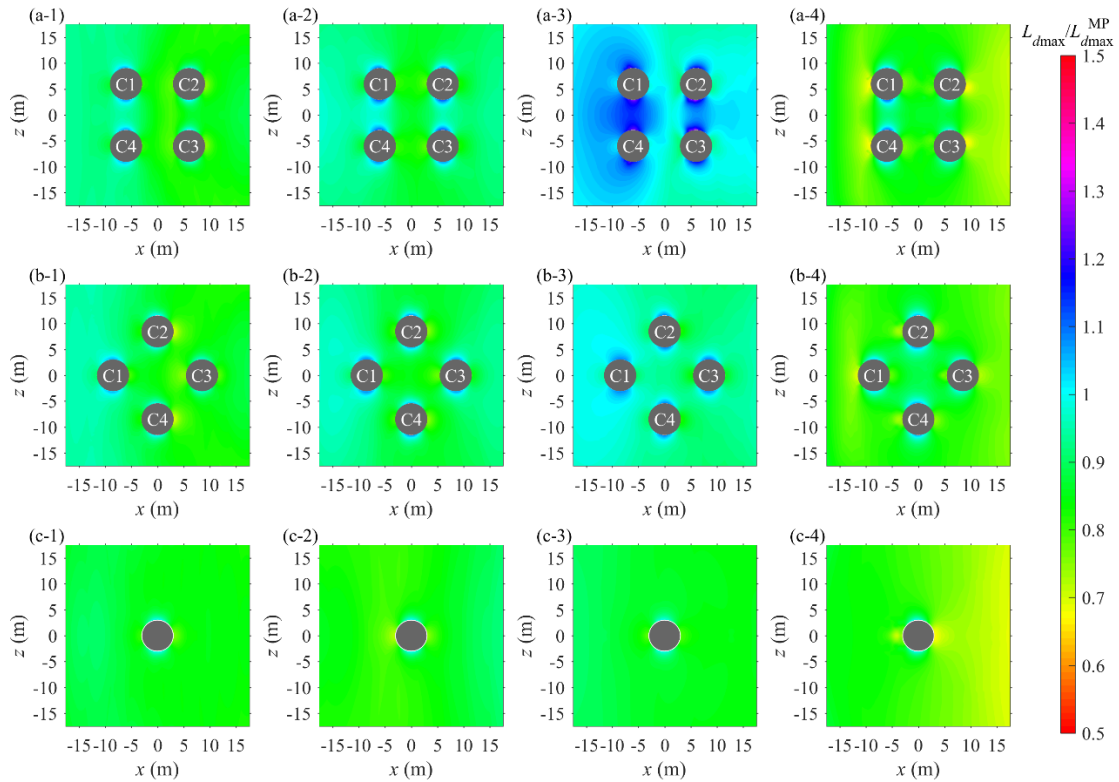


Figure 15 Spatial distribution of the normalized maximum liquefaction depth ( $L_{dmax}$ ) within a wave period over the maximum liquefaction depth ( $L_{dmax}^{MP}$ ) in the mono-pile case with same incident wave. (a)  $0^\circ$  incident wave; (b)  $45^\circ$  incident wave; (c) a mono-pile case. The numbering indicates the case number in Table 3.



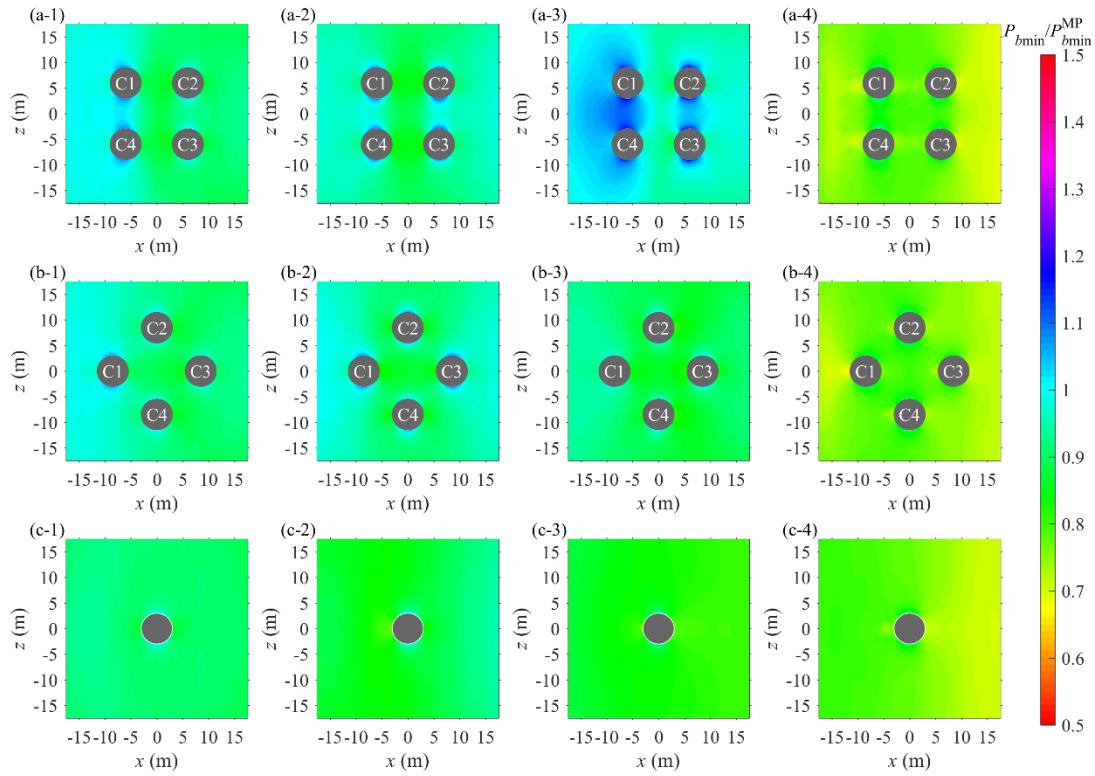


Figure 16 Spatial distribution of the normalized minimum pore water pressure at seabed ( $P_{bmin}$ ) within a wave period over the minimum pore water pressure ( $P_{bmin}^{MP}$ ) in the mono-pile case with same incident wave. (a)  $0^\circ$  incident wave; (b)  $45^\circ$  incident wave; (c) a mono-pile case. The numbering indicates the case number in Table 3.

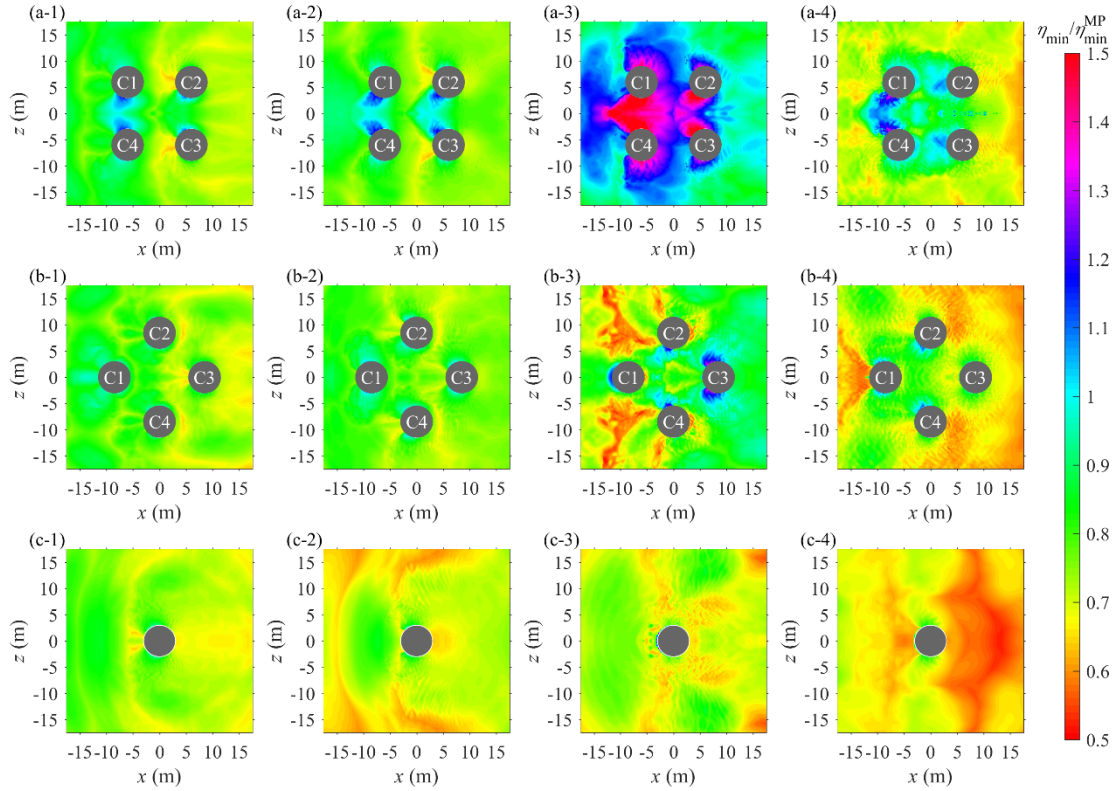


Figure 17 Spatial distribution of the normalized minimum free surface elevation ( $\eta_{\min}$ ) within a wave period over the minimum free surface elevation ( $\eta_{\min}^{\text{MP}}$ ) in the mono-pile case with same incident wave. (a)  $0^\circ$  incident wave; (b)  $45^\circ$  incident wave; (c) a mono-pile case. The numbering indicates the case number in Table 3.

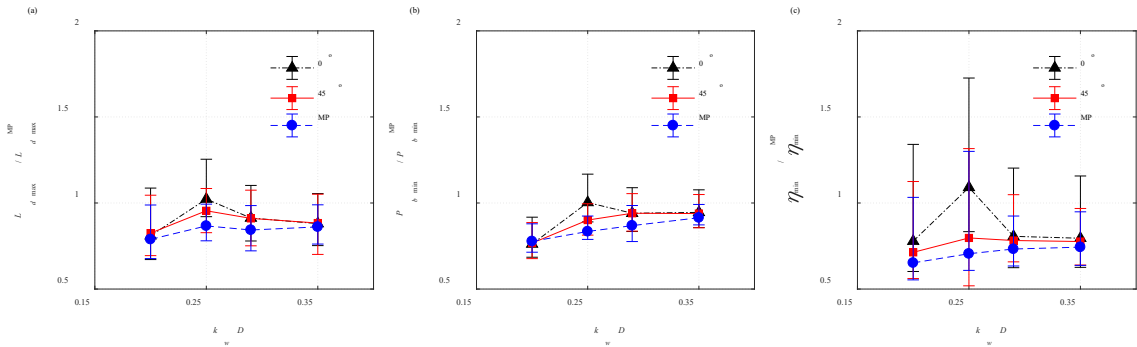


Figure 18 Average, the minimum, and the maximum amplification factors for different layouts and  $k_w D$ ; (a) liquefaction depth  $L_d$ ; (b) seabed surface pressure  $P_b$ ; (c) free surface elevation  $\eta$ .

521

#### 522 4.4 Influence of incident angle

523 For a better understanding of how the maximum liquefaction depth is distributed around each  
 524 cylinder surface, the maximum liquefaction across the same vertical circular plane as in Figure 9 and  
 525 Figure 10 for two incident wave angles are compared with the result of a single cylinder case (Figure  
 526 11) and presented in Figure 19. Good protection effect of the upstream cylinder (C1) on the vicinity  
 527 of the front ( $0^\circ$ ) and back ( $180^\circ$ ) of downstream cylinder (C2 with  $0^\circ$  wave heading and C3 with  $45^\circ$

528 wave heading) can be confirmed in all cases with both incident angles. A special attention needs to  
 529 be paid to the back side of each downstream cylinder, where the maximum momentary liquefaction  
 530 depth is smaller than that at the back side of upstream cylinder. This can also be attributed to the  
 531 protection effect from front cylinders. Comparing the liquefaction depth around individual cylinders  
 532 in an array with the result of a mono-pile foundation case, it is evident that the liquefaction depth  
 533 with a four-cylinder foundation is overall greater, and the upstream cylinder(s) experience more  
 534 significant liquefaction threat than other cylinders in an array.

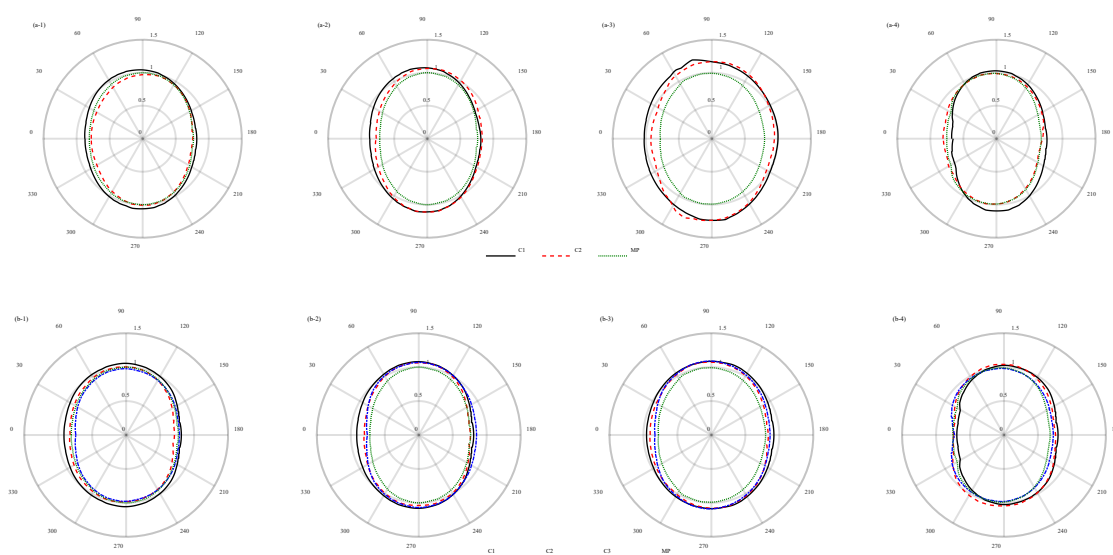


Figure 19 Polar plot of the normalized of the maximum liquefaction depth ( $L_{dmin}$ ) within a wave period over the maximum liquefaction depth ( $L_{dmax}^{MP}$ ) in the mono-pile case with same incident wave. (a)  $0^\circ$  incident wave; (b)  $45^\circ$  incident wave. Refer to Figure 8 for the definition of  $\theta$ , and to Figure 2 for the location of cylinders. The numbering indicates the case number in Table 3.

535  
 536 On the basis of the spatial distribution of wave-induced pressure on seabed surface in Figure 16, the  
 537 minimum value is located at the lateral sides of each cylinder. For momentary liquefaction, the  
 538 primary cause is the wave-induced pressure under wave trough. Therefore, the maximum momentary  
 539 liquefaction is distributed at both lateral sides of each circular cylinder. Figure 19 further confirms  
 540 this: the maximum liquefaction depth over a wave period indeed takes place at both lateral sides of  
 541 each cylinder. Moreover, for  $0^\circ$  incident wave (Figure 19a) the distribution of the maximum  
 542 liquefaction depth in the vicinity of both upstream and downstream cylinders (C1 and C2) is  
 543 non-symmetric. In contrast, Figure 19(b) shows that for  $45^\circ$  incident wave the distribution of the  
 544 maximum liquefaction depth in the vicinity of the lateral cylinder C2 is fairly symmetric.

#### 545 546 **4.5 Liquefaction around foundation under shorter waves**

547 As aforementioned in section 4.3, the liquefaction depth near a mono-pile foundation in Case 5  
 548 (Table 3) is small, so this case is now discussed separately from other four cases. The maximum  
 549 liquefaction depth over a wave period in Case 5 is presented in Figure 20, where in both incident  
 550 wave directions liquefaction is most pronounced in front of a cylinder array and liquefaction depth at

551 the back of a cylinder array is smaller. This further confirms the good protection of downstream  
 552 cylinders by upstream cylinders, which was discussed in sections 4.3 and 4.4: the upstream cylinders  
 553 (C1 and C4 with  $0^\circ$  wave heading; C1 with  $45^\circ$  wave heading) may encounter more significant  
 554 liquefaction threat than the downstream cylinders. Regarding the mono-pile foundation, shorter  
 555 incident wave generates much smaller liquefaction depth in the vicinity of the cylinder.

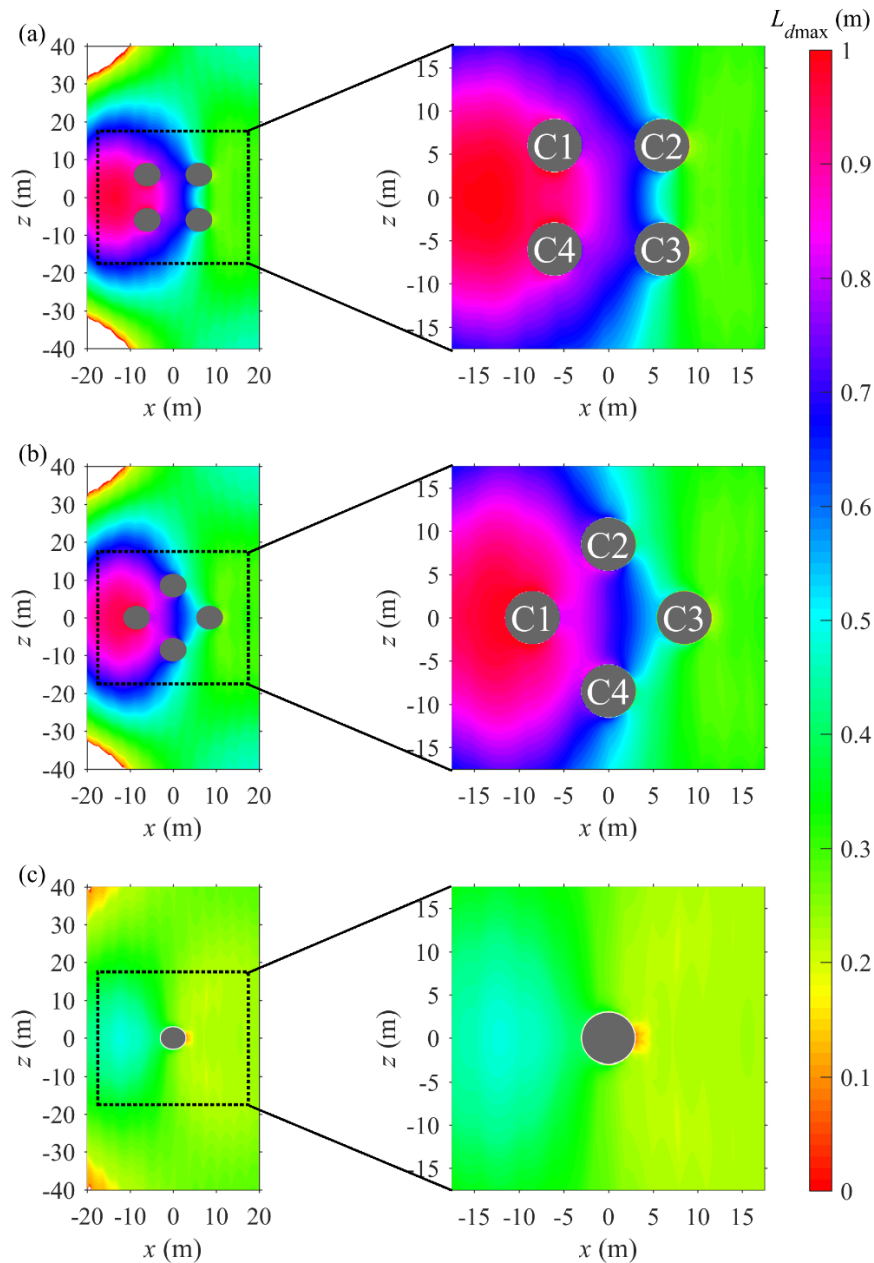


Figure 20 Spatial distribution of the maximum liquefaction depth with (a)  $0^\circ$  incident wave, (b)  $45^\circ$  incident wave, and (c) a mono-pile foundation.

556  
 557 As before, spatial distributions of liquefaction depth are compared with the spatial distribution of the  
 558 normalized the minimum wave-induced pressure on seabed surface and free surface elevation shown  
 559 in Figure 21. Spatial distributions of liquefaction depth and the seabed pressure are almost identical,  
 560 whereas the spatial distribution of the minimum free surface elevation is similar to them, especially

561 in the region near the front cylinders, but also contains higher order harmonics absent from other two.  
 562 In addition, the normalized minimum wave-induced pressure on seabed surface shown in Figure  
 563 21(a), indicates that the approximate range of the amplification factor, resulting from near-trapping  
 564 phenomenon of incoming wave within a cylinder array, is from 1.1 to 1.4. With shorter incident wave  
 565 (Case 5 with  $k_w D = 0.43$ ), the near-trapping effect tends to be more significant, with greater  
 566 amplification factor, while the liquefaction depth, compared to longer wave (Case 1 with  $k_w D = 0.35$   
 567 and  $L_d$  of roughly 1.38m), is smaller, roughly 1m, due to the smaller magnitude of wave-induced  
 568 pressure under wave trough. Nevertheless, the soil response near a cylinder array under such shorter  
 569 waves should still be examined in terms of liquefaction potential, especially for cylinder arrays  
 570 where the near-trapping phenomenon is capable of reducing the minimum wave-generated pressure  
 571 at seabed, compared to a single cylinder.

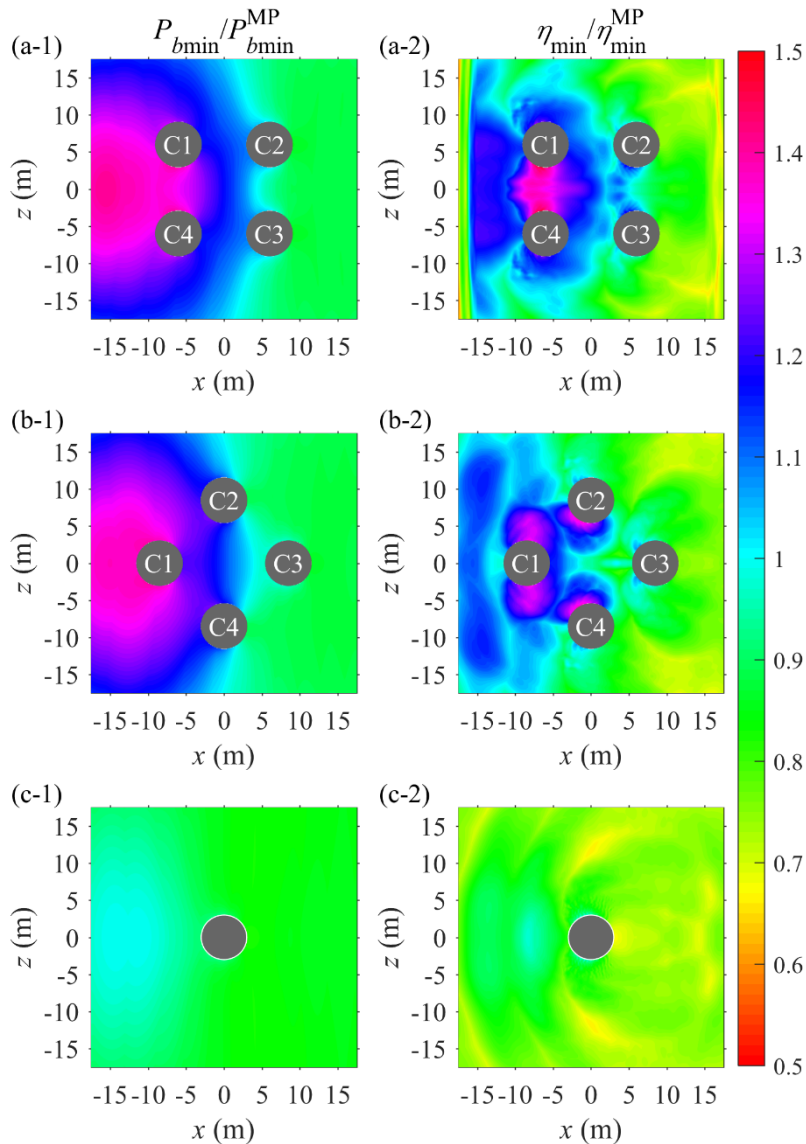


Figure 21 Spatial distribution of the normalized minimum wave-induced pressure ( $P_{bmin}$ ; see subplots a-1, b-1, c-1) on seabed surface and free surface elevation ( $\eta_{min}$ ; see subplots a-2, b-2, c-2) in a wave period. (a)  $0^\circ$  incident wave; (b)  $45^\circ$  incident wave; (c) a mono-pile foundation.

## 573 **5. Conclusions**

574 Previous study (Lin et al., 2017) demonstrated that the presence of mono-pile foundation has  
575 significant effect on the distribution of wave-induced pore water pressures and associated potential  
576 liquefaction. Nevertheless, the understanding of the liquefaction potential around a cylinder array  
577 under storm wave remains an unsolved issue. With the WSSI model proposed in Lin et al. (2017), an  
578 investigation of wave-induced seabed response and liquefaction potential in the vicinity of closely  
579 placed four cylinders has been carried out, for two incident wave angles, namely  $0^\circ$  and  $45^\circ$ , and for  
580 a range of wave conditions. The following conclusions can be drawn from this study:

581

582 (1) The capability of present wave model to simulate wave-cylinders interaction has been  
583 demonstrated. It shows that good accuracy can be obtained, even for higher order components,  
584 and for the steep wave. This agrees with the conclusion drawn in Sun et al. (2016) for single  
585 cylinder case. This study extends this conclusion to cylinder arrays. The near-trapping  
586 phenomenon is well captured and the wave sub-model in the coupled WSSI model is capable of  
587 simulating wave-cylinders interaction.

588 (2) The magnitudes of wave-induced free surface elevation and pressure in the vicinity of a cylinder  
589 array, as well as associated liquefaction depth, are amplified by the near-trapping phenomenon  
590 occurring during interaction of wave with an array of cylinders. Compared with the results of a  
591 mono-pile foundation case under same wave parameters, the amplification factor for liquefaction  
592 depth, wave-induced pressure, and free surface elevation is approximately in the range from 1.05  
593 to 1.2. In general, the amplification factor decreases with the increase of wave period. This is  
594 also demonstrated in Cong et al. (2015) by experimental and numerical investigations of free  
595 surface elevation. Although the numerical results of soil model are highly sensitive to the soil  
596 parameters used in the study, the overall phenomenon of soil response under near-trapping  
597 effects can still be captured as wave-induced pore pressures within the seabed are well predicted  
598 numerically and irrelevant to soil parameters. The potential for liquefaction needs to be  
599 examined even in the case with shorter wave and smaller wave height, in which no liquefaction  
600 takes place around the mono-pile foundation, but may still happen near a cylinder array, due to  
601 the effect of near-trapping phenomenon.

602 (3) The overall liquefaction depth near a four-cylinder group under  $0^\circ$  incident wave is greater than  
603 that under  $45^\circ$  incident wave. This is because the wave with  $0^\circ$  incident direction has significant  
604 near-trapping phenomenon inside the cylinder array, which leads to smaller seabed pore pressure  
605 than for  $45^\circ$  incident wave. As a result, the porous seabed at the inner zone of a four-cylinder  
606 array is more vulnerable to liquefaction threat than that at the outer zone in both incident wave  
607 directions since lower wave-induced pressures occur in this zone. Non-symmetric spatial  
608 distributions of wave-induced pressure, liquefaction depth, and the minimum free surface  
609 elevation are found under  $0^\circ$  wave heading, while those under  $45^\circ$  wave heading are symmetric.

610 (4) In a four-cylinder array, upstream cylinders provide good protection from momentary  
611 liquefaction for downstream cylinders. As before, this directly corresponds to the spatial  
612 distribution of the minimum wave-induced pressure on seabed around cylinders. Furthermore,  
613 the momentary liquefaction depth is largest at the lateral sides of each cylinder. Good protection  
614 from momentary liquefaction therefore needs to be placed in these zones.

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 620 manuscript.

621  
 622 **Nomenclature**

$A$	Wave amplitude	[m]
$D$	Diameter of pipeline or cylinder	[m]
$e$	Penetration depth	[m]
$E$	Young's modulus	[MPa]
$\mathbf{g}$	Gravitational acceleration vector	[m/s <sup>2</sup> ]
$G$	Shear modulus of soil	[N/m <sup>2</sup> ]
$h_s$	Soil depth	[m]
$h_w$	Mean water level or water depth	[m]
$H_w$	Wave height	[m]
$k_s$	Darcy's permeability	[m/s]
$k_w$	Wave number	[m <sup>-1</sup> ]
$K_0$	Coefficient of earth pressure at rest	[-]
$K_w$	True bulk modulus of elasticity of water	[N/m <sup>2</sup> ]
$L_d$	Liquefaction depth	[m]
$L_{dmax}^{MP}$	The maximum liquefaction depth of a mono-pile foundation	[m]
$L_s$	Soil domain length	[m]
$L_w$	Wave length	[m]
$\mathbf{n}$	The normal to the body surface	[-]
$n_s$	Porosity of soil	[-]
$p$	Total pressure	[kPa]
$P_{bmin}^{MP}$	The minimum pore water pressure on the seabed surface in a mono-pile foundation case	[kPa]

$p_p$	Pore water pressure	[kPa]
$p_w$	Hydrostatic water pressure	[kPa]
$P_0$	The maximum pore water pressure	[kPa]
$P_b$	Pore water pressure on the seabed surface	[kPa]
$P_{w0}$	Absolute pore water pressure	[kPa]
$S_r$	Saturation degree of soil	[-]
$t$	Time	[s]
$T$	Wave period	[s]
$\mathbf{u}$	Velocity field	[m/s]
$\mathbf{u}_a$	Air velocity	[m/s]
$\mathbf{u}_r$	Relative velocity field	[m/s]
$\mathbf{u}^T$	Transpose matrix of velocity field	[m/s]
$\mathbf{u}_w$	Water velocity	[m/s]
$\mathbf{v}$	$\mathbf{v} = (u_s, v_s, w_s)$ , the vector of soil displacement	[m]
$\mathbf{x}$	$\mathbf{x} = (x, y, z)$ , Cartesian coordinate vector where $y$ is the vertical coordinate, $x$ and $z$ are the horizontal coordinates.	[m]
$W_s$	Soil domain width	[m]
$\alpha$	Volume fraction function	[-]
$\beta_s$	Compressibility of pore fluid	[m <sup>2</sup> /N]
$\gamma_s$	Unit weight of soil	[kN/m <sup>3</sup> ]
$\gamma_w$	Unit weight of water	[kN/m <sup>3</sup> ]
$\varepsilon_s$	Volume strain	[-]
$\eta$	Free surface elevation	[m]
$\eta_{\min}$	The minimum free surface elevation	[m]
$\eta_{\min}^{\text{MP}}$	The minimum free surface elevation in the mono-pile case	[m]
$\theta$	Angle along circular cylinder circumference	[°]
$\theta_w$	Wave direction	[°]



$\mu$	Dynamic viscosity	[kg/sm]
$\mu_w$	Dynamic viscosity of water	[kg/sm]
$\mu_a$	Dynamic viscosity of air	[kg/sm]
$\nu$	Poisson's ratio	[-]
$\rho$	Fluid density	[kg/m <sup>3</sup> ]
$\rho_w$	Water density	[kg/m <sup>3</sup> ]
$\rho_a$	Air density	[kg/m <sup>3</sup> ]
$\sigma_{ij}$	The rate of the strain tensor	[-]
$\sigma'$	Effective normal stress	[kPa]
$\tau$	Shear stress	[kPa]
$\omega$	Frequency of incident wave	[s <sup>-1</sup> ]

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