

# Unsupervised feature learning and clustering of particles imaged in raw holograms using an autoencoder

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Digital holography is a useful tool to image microscopic particles. Reconstructed holograms give high-resolution shape information that can be used to identify the types of particles. However, the process of reconstructing holograms is computationally intensive and cannot easily keep up with the rate of data acquisition on low-power sensor platforms. In this work, we explore the possibility of performing object clustering on holograms that have not been reconstructed, *i.e.* images of raw interference patterns, using the latent representations of a deep-learning autoencoder and a self-organising mapping network in a fully unsupervised manner. We demonstrate this concept on synthetically generated holograms of different shapes, where clustering of raw holograms achieves an accuracy of 94.4%. This is comparable to the 97.4% accuracy achieved using the reconstructed holograms of the same targets. Directly clustering raw holograms takes less than 0.1 second per image using a low-power CPU board. This represents a three-order of magnitude reduction in processing time compared to clustering of reconstructed holograms, and makes it possible to interpret targets in real time on low-power sensor platforms. Experiments on real holograms demonstrate significant gains in clustering accuracy through the use of synthetic holograms to train models. Clustering accuracy increased from 47.1% when the models were trained only on the real raw holograms, to 64.1% when the models were entirely trained on the synthetic raw holograms, and further increased to 75.9% when models were trained on the both synthetic and real datasets using transfer learning. These results are broadly comparable to those achieved when reconstructed holograms are used, where the highest accuracy of ~70% achieved when clustering raw holograms outperforms the highest accuracy achieved when clustering reconstructed holograms by a significant margin for our datasets.

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## 1. INTRODUCTION

Holography is a non-invasive high-resolution imaging technique that retains a large depth-of-field [1]. Digital holographic microscopes can be used to generate focused images of microscopic particles that are suspended in fluids, such as marine micro-particles [2–4] and biological cells *in vivo* [5, 6]. Since raw holograms consist of the interference patterns generated when

particles are in the path of coherent light, it is normally necessary to first reconstruct holograms at specific distances (the focused reconstructions) to extract the shapes of the particles before further analysis, *e.g.* object classification or size analysis, can be performed. However, hologram reconstruction is a computationally intensive process. It becomes more expensive when the distance to the target is not known prior to reconstruction, since

hologram reconstruction needs to go through the whole recording volume to detect the focal plane. Although efforts have been made to speed up this process using field-programmable gate arrays (FPGAs) [7, 8] and parallel processing using graphics cards [9], these methods significantly increase the cost, power consumption and complexity of embedded sensing platforms.

Recent demonstrations of supervised deep-learning techniques to efficiently reconstruct raw holograms [10–12] give the possibility for real-time interpretation of digital holograms on compact, low-power devices. However, the need for large training datasets is a limiting factor because reconstruction and focus detection in holograms is time consuming. At the same time the fact that deep-learning algorithms can extract useful features from raw holograms motivates investigation into direct interpretation using deep-learning autoencoders [13, 14]. A key feature of autoencoders is that they can learn latent representations in a fully unsupervised manner (*i.e.* without the need for any human input to generate training data), which greatly simplifies the training process. Unlike traditional feature extraction methods, *e.g.* principal component analysis (PCA) [15], autoencoders can model more complex, nonlinear relationships between inputs and their extracted features, *i.e.* latent representations [16]. This flexibly makes autoencoders effective at learning features from datasets gathered under different conditions or when different instruments are used. The latent representations extracted by autoencoders can be used for clustering without the need for any human supervision. This has been effectively demonstrated for various types of optical image [17–20]. However, there have been no previous studies investigating their use for clustering of raw digital holograms.

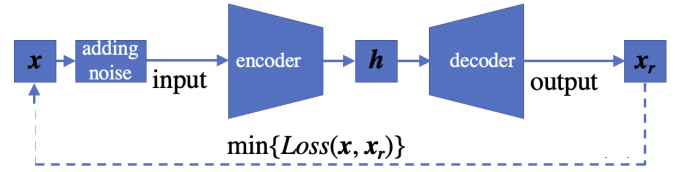
In this paper, we investigate how to learn features from raw holograms and cluster holograms based on these features using an end-to-end unsupervised workflow. Even though unsupervised methods do not require human input to generate labelled training data, they still require large amounts of unlabelled data to learn useful features, which can be challenging to obtain in applications where targets of interest are sparse and have unbalanced class distributions (*e.g.* marine micro-particle imaging). Therefore, we investigate how to improve the efficiency of training unsupervised models using synthetically generated data. The concept of directly interpreting raw holograms is first demonstrated entirely using synthetic holographic data. Next, we explore methods to analyse real holograms using transfer learning [21], where models are first pre-trained on synthetic holograms before training on a small number of real holograms. The performance of this proposed method is compared to alternative transfer learning methods that use generic image databases, and methods that use only synthetic holograms for training. The proposed workflow is demonstrated on a low power CPU board to show its practical use for *in situ* applications.

## 2. FEATURE LEARNING USING AUTOENCODERS

An autoencoder consists of two components: an encoder and a decoder, as shown in Fig. 1. The encoder reduces an input image  $x$  into a latent representation  $h$  that has a lower number of dimensions than the original image. The decoder does the reverse, using the latent representation  $h$  to restore<sup>1</sup> an image,  $x_r$ ,

<sup>1</sup> In this paper the output of the decoder is called restoration (image generated from the latent representation); the output of the hologram reconstruction algorithm is called reconstruction (focused image that has been generated from the raw interference patterns).

that is as close to the initial input image  $x$  as possible. Typically, noise is added to inputs so that the encoder learns to denoise images and extract more robust representations of the original inputs [14, 22].



**Fig. 1.** Flowchart of an autoencoder with denoising.  $x$ ,  $h$  and  $x_r$  signify an input image, its latent representation and restored image respectively.  $Loss(x, x_r)$  is a loss function which calculates the error between  $x$  and  $x_r$ .

The model learns by minimising the difference, or loss, between  $x$  and  $x_r$  for all the images in a training dataset. The process can be described as follows:

$$\{\varphi : x \rightarrow h; \phi : h \rightarrow x_r; \varphi, \phi \leftarrow \min(Loss(x, x_r))\} \quad (1)$$

where  $\varphi$  and  $\phi$  are the mappings of the encoder and decoder respectively. The training attempts to find the optimal weights in  $\varphi$  and  $\phi$  to minimise the loss between  $x$  and  $x_r$ . Once trained, the encoder can be used independently to extract latent representations  $h$  that have reduced dimensions compared to  $x$  and  $x_r$ , and can be used as features for unsupervised clustering or supervised classification of the inputs.

The autoencoder used in this work is based on the AlexNet architecture [23, 24]. The original architecture of AlexNet consists of 8 layers in total, taking input image dimensions of  $227 \times 227 \times 3$ , using 5 convolutional layers (the first, second and fifth layer are each followed by max pooling layers) and 3 fully-connected layers. The relatively simple architecture compared to more recent convolutional neural networks (CNNs) makes it suitable for use in autoencoders, as demonstrated in [19, 20, 25].

In this work, two modifications are made to the original AlexNet architecture as described in Section 1 of the [supplementary document](#). Since typical holographic images are monochrome, the input data size is changed to  $227 \times 227 \times 1$  instead of  $227 \times 227 \times 3$ , which caters for the RGB colour channels in conventional imaging. The three fully-connected layers in the original architecture are useful for solving highly complex classification problems [26]. However, these fully-connected layers comprise 94% of the parameters in AlexNet and allow geometric structures in the input images to be lost in the extracted features [27]. In contrast, the convolutional layers preserve spatial locality [23]. Since raw holograms have a high degree of geometric structure (interference fringes around object silhouettes), we replaced the three fully connected layers by two convolutional layers (each followed by a max pooling layer). This modification efficiently preserves geometric characteristics in the extracted features, which improves the learning efficiency for spatially structured images like raw holograms, and speeds up the training process with a reduced network size. Details of these improvements are described in Section 3-B of the [supplementary document](#).

The first modified convolutional layer uses 96 filters with a kernel size of  $3 \times 3$  and scanning stride of  $1 \times 1$ . The same padding strategy [28] is used in this layer, which results in this

118 layer outputting a datum of size  $6 \times 6 \times 96$ . After max pooling  
 119 with a pooling size of  $3 \times 3$  and a scanning stride of  $3 \times 3$ , the  
 120 output datum size becomes  $2 \times 2 \times 96$ . The second convolutional  
 121 layer controls the number of the latent features. Its output size  
 122 is  $2 \times 2 \times 40$ . ReLU (rectified linear unit) activation functions  
 123 are used in these two convolutional layers. After max pooling,  
 124 a 40-dimension latent representation is obtained from each in-  
 125 put image. This value was chosen based on a parametric study,  
 126 where increasing the dimensionality of latent representation did  
 127 not improve the results (see Section 3-A in the [supplementary](#)  
 128 [document](#)). Its decoder is mirror-symmetrical, where convolu-  
 129 tional layers are transposed to transconvolutional layers [29],  
 130 and the max pooling layers are transposed to upsampling layers  
 131 [30].

132 To address the background noise that exits in holograms [31],  
 133 a denoising step is added to the autoencoder to reduce the effect  
 134 of noise on feature extraction (Section 3-C in the [supplementary](#)  
 135 [document](#)). The training parameters for the autoencoder are  
 136 described in Section 2-A of the [supplementary document](#).

### 137 3. CLUSTERING MODEL

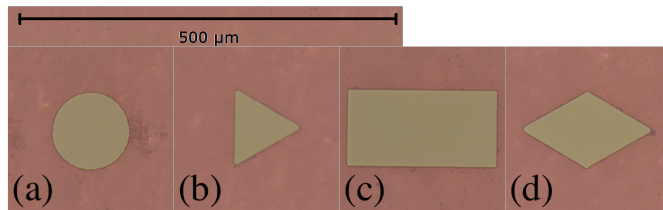
138 In this work, objects are clustered using a self-organising map-  
 139 ping (SOM) network [32]. The SOM is a well-established unsu-  
 140 pervised learning model that is built using a pre-defined 2-D net  
 141 of neurons [33]. Unlike the error-correction-based learning in  
 142 other networks (*e.g.* gradient descent in backpropagation), com-  
 143 petitive learning [32] is applied where training samples compete  
 144 for neurons to represent them. This causes different portions of  
 145 the SOM network to respond similarly to certain input samples,  
 146 creating a transfer function where similar regions of the latent  
 147 representation are mapped to the same clusters. Further details  
 148 of the SOM used in this work can be found in Section 2-B of the  
 149 [supplementary document](#).

### 150 4. DATASETS

151 For applications such as marine micro-particle imaging, it can  
 152 be difficult to prepare large datasets of real holographic imagery  
 153 for training a deep-learning autoencoder. A possible solution is  
 154 to generate synthetic holograms and use these to train a model.  
 155 The trained model can be used directly, or used as pre-trained  
 156 outputs to initialise further training using a small dataset of real  
 157 holographic images (*i.e.* transfer learning). Artificial noise is  
 158 added to the synthetic holograms to facilitate the denoising  
 159 training process in the autoencoder.

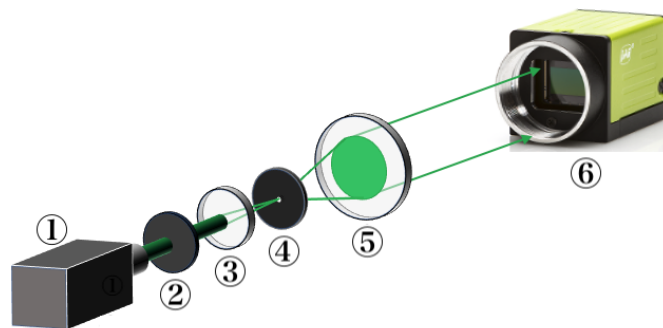
160 Experiments are performed on both the interference patterns  
 161 of raw holograms and equivalent reconstructed images of four  
 162 simple geometries: circle, triangle, rectangle, and diamond. Real  
 163 holograms are obtained using a  $200 \times 200 \text{ mm}^2$  glass plate with  
 164 these shape patterns etched on it. The diameter of the circle and  
 165 the smallest edge of other patterns is  $100 \mu\text{m}$ , as shown in Fig.  
 166 2, where the etched shapes on the plate have  $1 \text{ mm}$  separation  
 167 between them. The synthetic dataset is generated using the same  
 168 shapes without any neighbours.

169 *Real dataset:* An in-line holographic camera was used to take  
 170 holograms of the shape plate. The setup is shown in Fig. 3  
 171 and is based on a previously described system [34]. A 532 nm,  
 172 single-longitudinal mode continuous wave laser (Elforlight) is  
 173 used as the light source. The beam intensity is controlled using a  
 174 variable neutral density filter, while a spatial filter (items ③ and  
 175 ④) provide a spatially coherent and uniform beam. This beam is  
 176 collimated using a lens ⑤ before illuminating a complementary



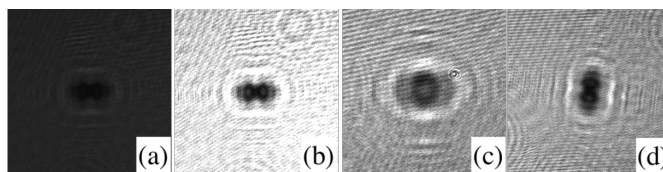
177 **Fig. 2.** Microscopic photographs of four shapes. (a) – circle; (b)  
 178 – triangle; (c) – rectangle; (d) – diamond.

179 metal-oxide-semiconductor (CMOS) image sensor (JAI GO-5100-  
 180 USB, ⑥) that has a resolution of  $2464 \times 2056$ , pixel pitch of  $3.45 \mu\text{m}$   
 181 and an active detection area of  $8.5 \text{ mm} \times 7.09 \text{ mm}$ .



182 **Fig. 3.** Schematic diagram of the in-line structure hologram  
 183 recorder used in this work. ① – laser, ② – neutral density  
 184 filter, ③ – microscopic objective lens, ④ – pinhole, ⑤ – colli-  
 185 mating convex lens, ⑥ – CMOS image sensor.

186 The shape plate is placed in the laser beam path, between  
 187 the collimating lens ⑤ and sensor ⑥. The dataset consists of  
 188 holograms where the distance of the plate from the sensor varies  
 189 between  $10 \text{ mm}$  to  $60 \text{ mm}$ , and different sensor exposure times  
 190 ( $10, 40, 70, 100, 130, 160, 190$  and  $220 \mu\text{s}$ ) and relative plate  
 191 orientations (between  $-90^\circ$  and  $90^\circ$ ) are used. Fig. 4 shows four  
 192 holograms of rectangles recorded under different conditions.



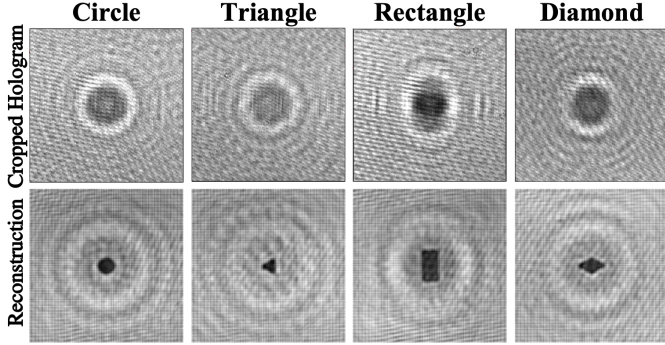
193 **Fig. 4.** Four hologram samples of a rectangle under differ-  
 194 ent conditions. (a) recorded at  $17.90 \text{ mm}$  with  $10 \mu\text{s}$  exposure  
 195 time; (b) recorded at  $17.90 \text{ mm}$  with  $220 \mu\text{s}$  exposure time; (c)  
 196 recorded at  $47.70 \text{ mm}$  with  $130 \mu\text{s}$  exposure time; (d) recorded  
 197 at  $17.85 \text{ mm}$  with  $130 \mu\text{s}$  exposure time and close to  $90^\circ$  rota-  
 198 tion with regard to positions in the other three holograms.

199 Two independent sets of real holographic data are used. One  
 200 set (Group 1) is used for autoencoder training, and the other  
 201 (Group 2) is used to test the trained models. Each hologram is  
 202 cropped to  $300 \times 300$  pixels around the target (as discussed in  
 203 Section 3-D of the [supplementary document](#)), resulting in 4,180  
 204 cropped holograms in Group 1 and 3,844 in Group 2 (see Table  
 205 1). These are reconstructed using the angular spectrum method  
 206 [35], with examples of reconstructed holograms shown in Fig. 5.



**Table 1.** Number of real holograms for each shape.

Group	Circle	Triangle	Rectangle	Diamond	Total
1	780	887	1522	991	4,180
2	891	708	1546	699	3,844

**Fig. 5.** Cropped holograms of four shapes with the size of  $300 \times 300$  and their reconstructions.

195 *Synthetic dataset:* Raw holograms are simulated from the tar-  
 196 get shapes using the angular spectrum method. The parameters  
 197 used for the simulation are shown in Table 2. The size and rec-  
 198 ording distance of the shapes are randomly selected from within  
 199 the given ranges. The centre and orientation of the shapes are  
 200 also randomly chosen, but are restricted so that the shape is fully  
 201 shown within the boundary of the image.

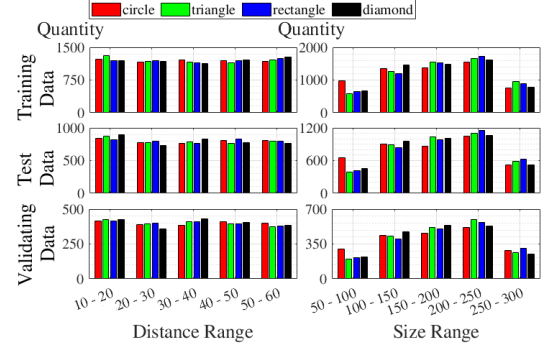
**Table 2.** Parameters used to create the synthetic holographic dataset.

Parameters	Values
shape size ( $\mu\text{m}$ )	50 – 300 with interval of 1
image size (pixel number)	$227 \times 227$
wavelength (nm)	532
pixel pitch ( $\mu\text{m}$ )	$3.45 \times 3.45$
recording distances (mm)	10 – 60 with interval of 0.5

202 In this dataset, three groups of data are created: training  
 203 data consisting of 24,000 holograms, validating data with 8,000  
 204 holograms and test data with 16,000 holograms. In each group,  
 205 the number of each shape is equal. Histograms of the recording  
 206 distances and shapes' sizes for each group are shown in Fig. 6.  
 207 Regarding the recording distance, the number of the holograms  
 208 of each shape in each range is similar. Most holograms lie within  
 209 the size range of 100 – 250  $\mu\text{m}$ , which matches the sizes of the  
 210 shapes in the glass plate (see Fig. 2).

211 The reconstructed holograms are generated using the angular  
 212 spectrum method. Two examples for each shape are shown in  
 213 Fig. 7, with the original shapes, the synthetic holograms and  
 214 their reconstructions.

215 Noise is added to the synthetic holograms by taking real  
 216 holograms without any targets and superimposing randomly  
 217 cropped regions of them as background noise in the synthetic  
 218 holograms (see Fig. 8).

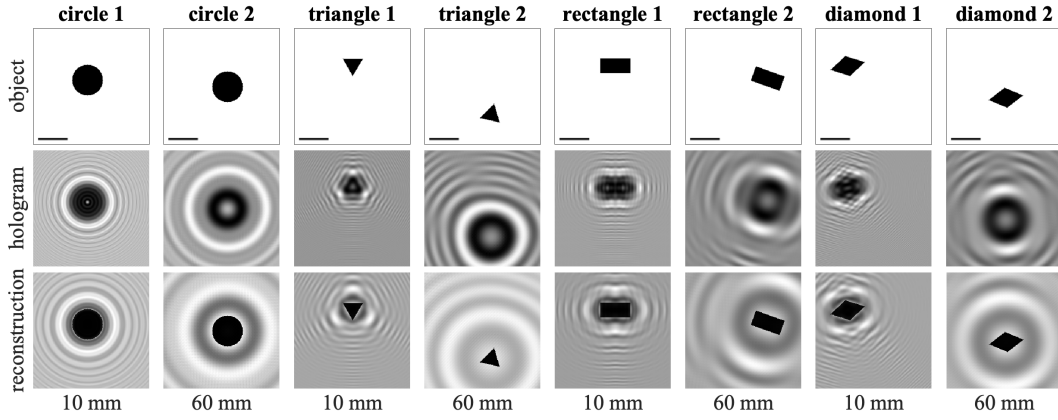
**Fig. 6.** Histogram of recording distances and shapes' sizes in three groups.

## 219 5. RESULTS AND ANALYSIS

220 The clustering performance of the proposed method was veri-  
 221 fied on the raw holograms of the entirely synthetic, entirely real  
 222 and on combined synthetic and real hologram datasets using  
 223 transfer learning. The results were compared to the equivalent  
 224 performance with reconstructed holograms for all the conditions  
 225 investigated in this work. In the first set of experiments, both  
 226 training and evaluation were performed on the synthetic data  
 227 to validate our concept. Next, experiments were performed to  
 228 cluster the real dataset. For the transfer learning experiments,  
 229 the autoencoder was pre-trained on the synthetic holograms and  
 230 fine-tuned using the real hologram data in Group 1. Afterwards,  
 231 the encoder was used to extract the latent representations from  
 232 the corresponding real hologram data in Group 2. These repre-  
 233 sentations were used as features to cluster the real holograms in  
 234 an unsupervised manner. For comparison, we also performed  
 235 transfer learning using the generic ImageNet database [24] for  
 236 pre-training. Besides this, only synthetic data and only real data  
 237 from Group 1 were respectively used for training the models.  
 238 These experimental conditions are shown in Table 3.

239 The clustering performance was assessed using the overall  
 240 accuracy and F1 score [36, 37] compared to the ground truth, and  
 241 the computational runtime. The workstation used for training  
 242 the models had an Intel i9-9900K CPU @ 3.60 GHz  $\times$  16 with  
 243 36 GB RAM and a GPU of NVIDIA GeForce RTX 2080 with 8  
 244 GB RAM. The low-power CPU board used to run the proposed  
 245 models had an Intel Atom processor E3940 @ 3.60 GHz  $\times$  4 with  
 246 8 GB RAM, which can be directly integrated into a compact  
 247 digital holographic microscope for use *in situ*.

248 All the algorithms in this work were implemented in Python  
 249 programming language. The angular spectrum algorithm [35]  
 250 was used to reconstruct a hologram at a given distance, and the  
 251 autofocusing method described in [38] was used to automatically  
 252 detect the focused reconstruction across the entire recording  
 253 distance range. In order to speed up the algorithms of angular  
 254 spectrum and autofocusing, two Python-based modules were  
 255 used: `mpi4py-fft` [39] for parallel computing the fast Fourier



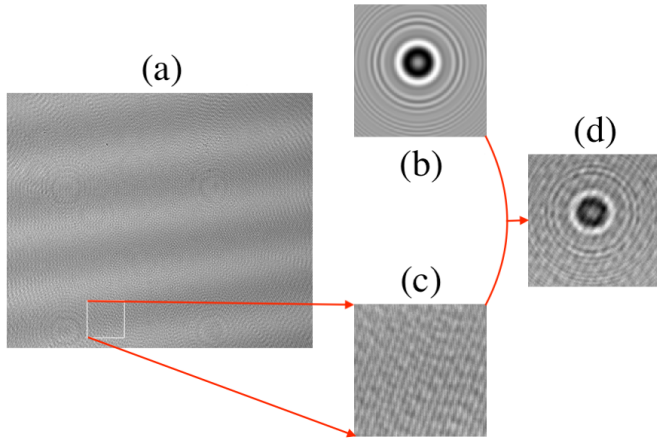
**Fig. 7.** Two examples of each shape, including original shapes (in the first row), corresponding synthetic holograms (in the second row) and their reconstructions (in the third row). Number below each column gives the recording distance of the hologram. The scale lines in the first row indicate 200  $\mu\text{m}$ .

**Table 3.** Description of four sets of experiments.

	Experiment	data for training autoencoder	data for training SOM	test data
proposed method	P	synthetic <sup>a</sup> +real (Group 1 <sup>b</sup> )	synthetic+real (Group 1)	real (Group 2 <sup>b</sup> )
comparative method	C1	ImageNet+real (Group 1)	real (Group 1)	real (Group 2)
	C2	synthetic	synthetic	real (Group 2)
	C3	real (Group 1)	real (Group 1)	real (Group 2)

<sup>a</sup> synthetic data for training.

<sup>b</sup> Group 1: real data for training; Group 2: real data for testing. See Table 1.



**Fig. 8.** An example of adding noise to the synthetic hologram. The noise image (c) is cropped from a background hologram (a), and it is added to a synthetic hologram (b) to create the final synthetic hologram (d).

256 transforms used by the algorithms, and **multiprocessing** [40] for  
 257 parallel execution of reconstruction across the recording distance  
 258 range. The autoencoder was developed, trained and tested using  
 259 **Tensorflow** [41]. The SOM model was built, trained and tested  
 260 using the open-source library of **MiniSom** [42].

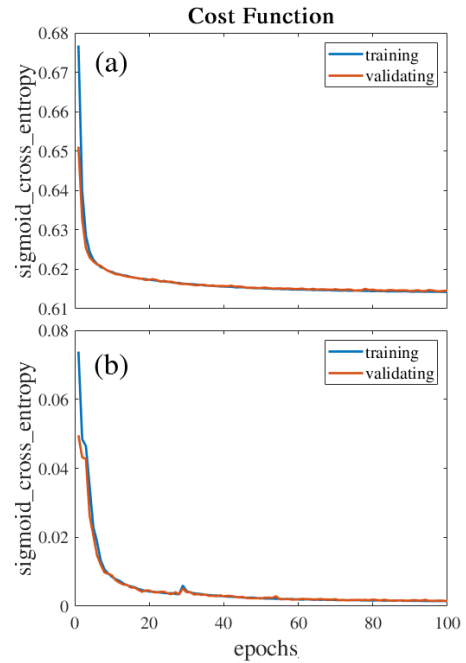
#### 261 A. Feature learning and clustering of synthetic holograms

262 The clustering performance of the proposed method was first  
 263 evaluated using the synthetic holograms. The autoencoder and  
 264 SOM were trained on the synthetic training data (raw and recon-  
 265 structed holograms respectively). Afterwards, each pair of the  
 266 trained encoder and SOM were used to cluster the correspond-  
 267 ing raw and reconstructed datasets for testing.

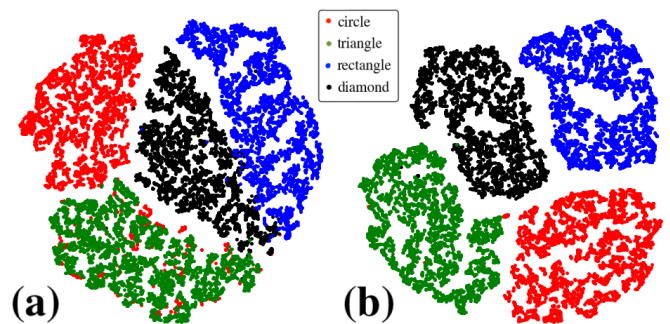
268 Fig. 9 shows the loss of the autoencoder on the training  
 269 dataset (24,000 holograms) and validation dataset (8,000 holo-  
 270 grams) for 100 epochs. The fact that the loss is similar for train-  
 271 ing and validation indicates that the model is able to generalise,  
 272 without over-fitting the synthetic data. The result also shows  
 273 that convergence is achieved after ~40 epochs.

274 Fig. 10 shows the TSNE (t-distributed stochastic neighbour  
 275 embedding) [43] plots of the latent representations extracted  
 276 from the raw and reconstructed holograms in the test data by  
 277 the corresponding trained encoders. It shows that there is larger  
 278 separation between the different shapes in the reconstructed  
 279 holograms, with some merging between different shapes occurs  
 280 in the plot of the raw data. Some raw holograms of circles  
 281 are mixed with the triangle cluster, and this is reflected in the clus-  
 282 tering scores of these shapes being lower in the raw holograms  
 283 than the reconstructed holograms.

284 The autoencoder and SOM were trained five times, and each  
 285 trained encoder and SOM pair were used to cluster the corre-  
 286 sponding raw and reconstructed synthetic datasets for testing.  
 287 The clustering performance of the SOM was compared to two  
 288 different classification methods. It should be noted that while  
 289 the SOM can cluster the dataset in a fully unsupervised manner,  
 290 the classifiers used for comparison both require labelled training  
 291 data of the target shapes, where in this case the ground truth  
 292 synthetic data was available. The first method used a support  
 293 vector machine (SVM) [44] that was trained on the features ex-  
 294 tracted from the training data by the encoder. The trained SVM  
 295 was then used to classify the test data (training parameters are



**Fig. 9.** Loss curves for autoencoder training and validation on the raw (a) and reconstructed (b) synthetic holograms. Each loss value is the mean of the results from five experiments.



**Fig. 10.** TSNE visualisation of the latent representation space extracted by the encoder for (a) the raw and (b) the reconstructed synthetic hologram test data.

296 given in Section 2-C of [the supplementary document](#)). The sec- 355  
297 ond method used AlexNet<sup>1</sup> to directly classify the input images 356  
298 based on the labelled training data. Table 4 shows their perfor- 357  
299 mance for the raw and reconstructed holograms in the test data. 358  
300 Clustering using the proposed unsupervised method - SOM - 359  
301 achieves a high accuracy of 94.4% and 97.3% for the raw and 360  
302 reconstructed holograms, respectively. The corresponding F1 361  
303 scores for each target shape are lower for the raw holograms 362  
304 than the reconstructed holograms. The two supervised classi- 363  
305 fiers achieve higher accuracy scores, which is expected since 364  
306 labelled training data is provided to the classifiers. The results 365  
307 show that a high level of accuracy can be achieved when directly 366  
308 analysing raw holograms that is comparable to processing re- 367  
309 constructed holograms. This has significant implications for *in* 368  
310 *situ* applications as it avoids the large computational overhead 369  
311 needed to reconstruct holograms. The main advantage of the un- 370  
312 supervised approach is that it does not require any human labels 371  
313 for training, which is generally time-consuming to generate and 372  
314 is challenging for applications where the exact target classes in 373  
315 the dataset are not initially known. An interesting observation 374  
316 is that the SVM classifier achieved close to 100% accuracy using 375  
317 the same features as the SOM. This indicates that it is the SOM 376  
318 that limits clustering performance and not encoder. 377

319 Table 5 shows the time taken for the different computations 378  
320 carried out in the experiment. The autoencoder and SOM were 379  
321 trained on the workstation, and testing the trained models was 380  
322 done on the low-power CPU board to reflect a realistic *in situ* 381  
323 operating scenario. The time required to train the autoencoder and 382  
324 SOM are almost identical for the raw and reconstructed holo- 383  
325 grams. The biggest cost is in the reconstruction of the holograms, 384  
326 which takes more than 13 times the combined training time. This 385  
327 processing step is not needed when interpreting raw holograms 386  
328 directly. Clustering the entire test dataset of 16,000 images using 387  
329 each trained encoder and SOM pair takes approximately 1,500 388  
330 s, *i.e.* and average of  $\sim 0.09$  s to process each hologram input. 389  
331 This would allow real-time clustering on the lower-power CPU 390  
332 board for an image acquisition rate of up to 10 Hz. However, 391  
333 reconstructing each hologram on the same lower-power CPU 392  
334 board takes  $\sim 14$  s per image, which forms significant bottleneck 393  
335 for real-time clustering of reconstructed holograms. It should 394  
336 be noted that hardware optimisation, such as the use of Field 395  
337 Programmable Gate Array (FPGA) or Graphics Processing Unit 396  
338 (GPU) embedded single board computers can allow real-time re- 397  
339 construction at faster rates [7–9]. However, this comes at the cost 398  
340 of higher power consumption, which is not ideal for long term 399  
341 monitoring applications where low-power electronics solutions 400  
342 are required. 401

## 343 B. Feature learning and clustering of real holograms

344 In our proposed method (P), experiments were performed where 403  
345 the autoencoder was first pre-trained on the synthetic training 404  
346 holograms and then fine-tuned using a small set of real holo- 405  
347 grams (Group 1) using transfer learning (see Section 2-D in [the](#) 406  
348 [supplementary document](#)). Similarly, the SOM pre-trained on 407  
349 the synthetic training data was also fine-tuned using the fea- 408  
350 tures of the holograms in Group 1 extracted by the fine-tuned 409  
351 autoencoder. The fine-tuned encoder and SOM were then used 410  
352 to extract and cluster the latent representations from real holo- 411  
353 grams in the test dataset in Group 2. The real holograms for 412  
354 testing were fed to the fine-tuned autoencoder and SOM. For 413  
414

comparison, three other sets of experiments were carried out 415  
with the real test holograms: C1. the autoencoder was pre-  
trained on the ImageNet dataset<sup>1</sup> (2012 [24]) and fine-tuned on  
the real holographic training data; the SOM was trained on the  
real training data based on the features extracted by the trained  
encoder; C2. the autoencoder and SOM were trained only on  
the synthetic training data; C3. the autoencoder and SOM were  
trained only on the real training data. These experiment condi-  
tions are summarised in Table 3. The parameters for fine-tuning  
the autoencoder and SOM are kept the same as those used in pre-  
training (see Section 2-A&B in [the supplementary document](#)).

The latent representations of the real test holograms extracted  
by the encoders from these four experiments are visualised in  
Fig. 11, and the results of clustering are shown in Table 6. Com-  
pared to the TSNE plots of the synthetic data in Fig. 10, the latent  
representations have decreased separation between the points of  
different shapes, where this is likely due to the unmodelled com-  
plexities of recording real holograms compared to generating  
synthetic ones. The TSNE visualisation for the proposed transfer  
learning method P (encoder pre-trained on synthetic data and  
fine-tuned on real data) shows good separation between the dif-  
ferent shape classes for the raw holograms (Fig. 11-(a-1)), with  
the rectangles clearly separated from other shapes. However,  
there is some mixing between the circle, triangle and diamond  
classes, which we expect to degrade the clustering performance  
for these shapes. A similar trend is seen for the conditions C1  
(Fig. 11-(b-1)) and C2 (Fig. 11-(c-1)). For C3 (Fig. 11-(d-1)), which  
was trained only on the real holograms, we see a higher level of  
mixing overall, and so we expect poor clustering performance.  
This result shows that the use of synthetic data and transfer  
learning can benefit feature extraction. A possible explanation  
for the better performance is that availability of a large number  
of training examples, where there are only 24,000 images in the  
synthetic training data, and 1,281,167 images in the ImageNet  
2012 training dataset, both of which are larger than the 4,180 real  
holograms available for training in Group 1.

For the reconstructed holograms, although there is some  
change in the TSNE for conditions P (Fig. 11-(a-2)), C1 (Fig. 11-  
(b-2)) and C2 (Fig. 11-(c-2)), the degree of mixing and separation  
are similar to the raw holograms. For condition C3 (Fig. 11-(d-2))  
however, there is a clear reduction in mixing and improvement  
in the separation of the rectangles. For conditions P, C1, and C2,  
the TSNE distributions for the raw holograms and reconstructed  
holograms have different appearances but it is not clear if either  
has a clear advantage over the other. This is favourable as we  
do not expect a large differences in performance when interpret-  
ing the raw holograms, which has a far lower computational  
overhead than the reconstructed holograms.

Regarding the differences between P (synthetically pre-  
trained and fine-tuned using real data) and C2 (synthetic data  
trained encoder), some insight can be drawn from Fig. 12, which  
shows two output images of each shape restored by the autoen-  
coders for conditions P and C2 respectively. The autoencoder  
trained only on the synthetic reconstructed data with denoising  
allows it to restore reconstructed holograms with clear shape  
outlines, but fine-tuning the model on the real reconstructed  
holograms reduces this capability, as seen by the distortion of  
the diamond shape and rounding of the triangles. For raw holo-  
grams however, the fine-tuned autoencoder retains the distinc-  
tive characteristics of the original inputs better than the autoen-  
coder trained only on the synthetic holograms. This is noticeable

<sup>1</sup> The image input size is changed to  $227 \times 227 \times 1$  instead of  $227 \times 227 \times 3$ . Its  
output class number is changed to 4. The training parameters are the same with  
those used to train the autoencoder.

<sup>1</sup> The images were converted into grayscale.



**Table 4.** Results of the three methods based on the F1 scores and accuracy when used to cluster/classify the synthetic holograms in the test dataset.

	Shape	Encoder+SOM		Encoder+SVM		AlexNet	
		F1 Score	Accuracy	F1 Score	Accuracy	F1 Score	Accuracy
Raw Holograms	Circle	0.933 ( $\pm 0.009^a$ )		0.980 ( $\pm 0.007$ )		1.000 ( $\pm 0$ )	
	Triangle	0.930 ( $\pm 0.006$ )	94.4%	0.980 ( $\pm 0.004$ )	98.9%	1.000 ( $\pm 0$ )	99.8%
	Rectangle	0.966 ( $\pm 0.009$ )	( $\pm 0.4\%$ )	1.000 ( $\pm 0$ )	( $\pm 0.3\%$ )	1.000 ( $\pm 0$ )	( $\pm 0.1\%$ )
	Diamond	0.948 ( $\pm 0.013$ )		1.000 ( $\pm 0$ )		1.000 ( $\pm 0$ )	
Reconstructed Holograms	Circle	0.975 ( $\pm 0.014$ )		1.000 ( $\pm 0$ )		1.000 ( $\pm 0$ )	
	Triangle	0.978 ( $\pm 0.013$ )	97.4%	1.000 ( $\pm 0$ )	99.9% ( $\pm 0.1\%$ )	1.000 ( $\pm 0$ )	100.0%
	Rectangle	0.980 ( $\pm 0.017$ )	( $\pm 1.5\%$ )	1.000 ( $\pm 0$ )		1.000 ( $\pm 0$ )	( $\pm 0\%$ )
	Diamond	0.962 ( $\pm 0.025$ )		1.000 ( $\pm 0$ )		1.000 ( $\pm 0$ )	

<sup>a</sup> standard deviation.

Note: Each value is the mean of the results from five experiments.

**Table 5.** Processing time for the models used to extract features from and cluster the raw and reconstructed holograms. The times shown are for processing the entire training and test datasets, where training is performed on a high-performance workstation, and testing is performed on a low-power single board CPU.

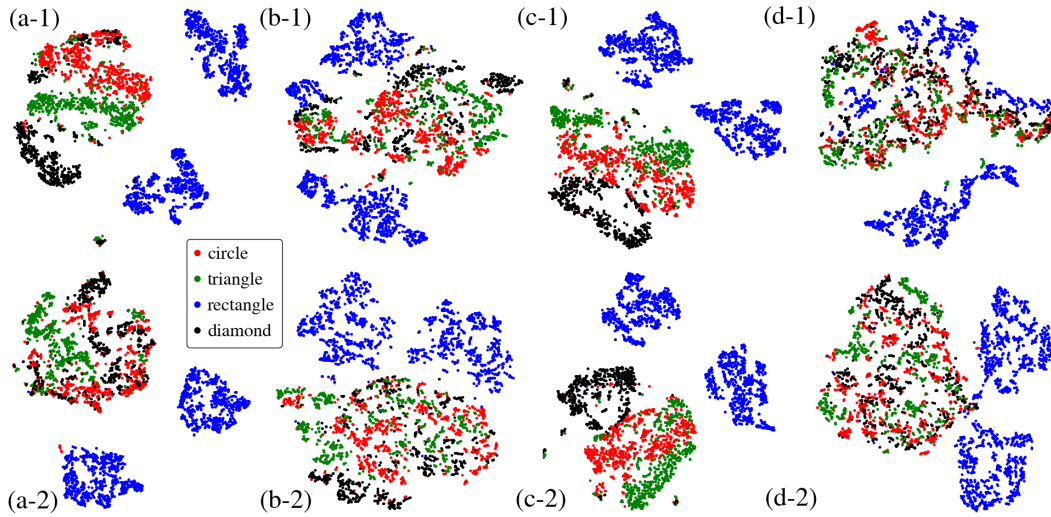
	Time (s) <sup>a</sup>				
	Reconstruction	Autoencoder	SOM	Reconstruction	Clustering
	for training <sup>b</sup>	training	training	for testing <sup>b</sup>	for testing
Raw Holograms	-	3,229	3.8	-	1472
Reconstructed Holograms	42,240	3,235	3.9	226,240	1477

<sup>a</sup> average value of five experiments.

<sup>b</sup> image size:  $227 \times 227$ ; reconstruction distance range: 10 – 60 mm with step 0.1 mm; no manual operation included.

Note: Training was carried out on the workstation and testing was done on the CPU board.





**Fig. 11.** TSNE visualisations of the latent representations extracted by the encoder for raw (first row) and reconstructed (second row) real test holograms. (a) shows the results for the encoder trained using the proposed condition P; (b) shows the results for the encoder trained using condition C1; (c) shows the results for the encoder trained using condition C2; and (d) shows the results for the encoder trained using condition C3. A description of the conditions is given in Table 3.

416 for the restored images of the raw circles, where the entirely syn- 454  
 417 thetically trained autoencoder deforms the interference fringes, 455  
 418 making them appear triangular.

419 The clustering performance of the real test holograms (Group 2) using the corresponding encoder and SOM pairs (Table 3) are shown in Table 6. The poorest performance is for the models were trained only on the real data (C3), where the raw holograms achieves the accuracy of 47.1% and the reconstructed holograms achieves 58.4%. The improved performance for the reconstructed holograms, particularly for the rectangles is expected based on the TSNE visualisation of the latent representations used for clustering. When the models were trained only on the synthetic data (C2), the accuracy increases for both raw and reconstructed holograms to 64.1% and 70.2%, respectively. In both C2 and C3, the reconstructed holograms perform better than the raw holograms. For the two transfer learning methods, the accuracy achieved for raw holograms further increases to ~76%, while the accuracy in the reconstructed holograms (~68%) is comparable to condition C2. Regarding accuracy, the models trained on the synthetic and real data (P) have similar performance with the models trained on the ImageNet and real data (C1), where the differences in the results are within the order of experiment repeatably. This is somewhat unexpected based on the TSNE plots, where the ImageNet pre-trained (C1) encoder appears to have a higher level of mixing between shapes than the synthetically pre-trained (P) encoder (see Fig. 11). A possible explanation is that the SOM used is limiting the ability to separate the shapes in P due to the merged boundaries between the shapes, and this is leading to a similar degree of confusion as the more intermixed distributions between the shapes in C1. Another unexpected result is that the accuracy in the raw holograms is higher than the reconstructed holograms after using transfer learning. This is reflected in Fig. 12, which shows that transfer learning does not facilitate the encoder to extract better representations from reconstructed holograms.

451 The performance across classes is not uniform based on the F1 score in each set of experiments. The rectangles are always resolved the best, and the circles resolved the worst both in the

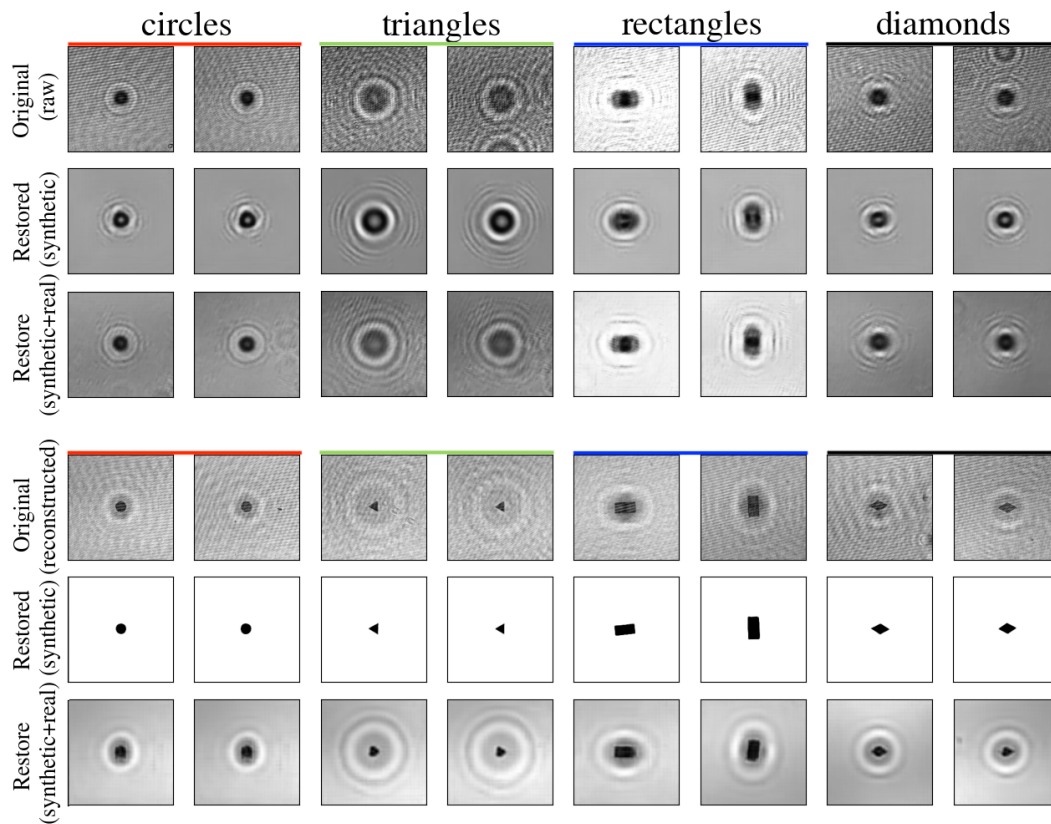
454 raw and reconstructed holograms. After using transfer learning, the circles and diamonds are better resolved in the raw holograms than the reconstructed holograms. The corresponding confusion matrices of the raw and reconstructed holograms from the experiments using condition P are shown in Fig. 13. In the raw holograms, there is a high degree of confusion between the circles and triangles. A possible reason for this can be seen in Fig. 11, where the restored interference fringes of the circles look similar to the triangles. In the reconstructed holograms, there is greater confusion between the circles and diamonds, which can again be seen in Fig. 11, where the restored diamonds have lost characteristic information about their shape.

## 6. CONCLUSIONS

Object clustering can be efficiently performed on raw holograms to achieve comparable performance to equivalent reconstructed holograms for the shapes investigated in this work. This offers significant gains in computational efficiency, which is compelling for *in situ* applications where real-time interpretation cannot keep up with the rate of data acquisition using low power CPUs. The key findings are:

- Deep-learning autoencoders can be used to extract latent representations from both raw and reconstructed holograms in a fully unsupervised manner. We demonstrate a modified CNN architecture that preserves geometric structure in the original images when extracting latent representations. When using an SOM as a clustering model, the accuracy of the raw and reconstructed holograms achieved 94.4% and 97.4% respectively for the synthetic dataset generated in this work. While the accuracy is nearly 100% both in the raw and reconstructed holograms when an SVM is used as a classifier to classify the same dataset. This reflects that the proposed autoencoder has the capability to extract good representations from raw holograms, and the clustering performance limited by the SOM that was used for unsupervised clustering.

- A three-order gain in computational efficiency can be achieved by directly interpreting raw holograms compared to reconstructed holograms using the same processing hardware.



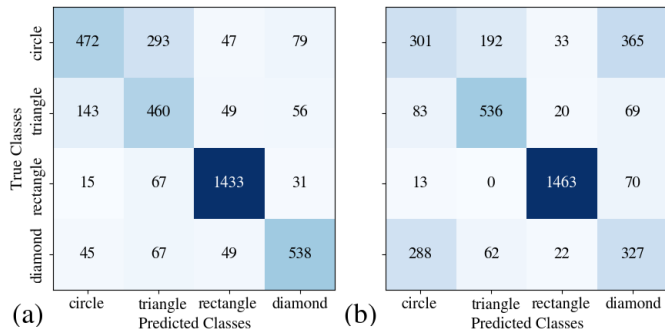
**Fig. 12.** Examples of input and restored output images for each shape using the autoencoders trained only on the synthetic data (C2), and synthetically pre-trained and fine-tuned with real data (P) respectively. The first three rows show the results for raw holograms, the bottom three rows show the results for reconstructed holograms.

**Table 6.** Clustering results from condition P and conditions C1 – C3 respectively, based on F1 score and accuracy when used to cluster the real test holograms (Group 2).

	Shape	Condition P (transfer learning)		Condition C1 (transfer learning)		Condition C2		Condition C3	
		F1 Score	Accuracy	F1 Score	Accuracy	F1 Score	Accuracy	F1 Score	Accuracy
Raw Holograms	Circle	0.614 ( $\pm 0.023^a$ )	75.9%	0.601 ( $\pm 0.063$ )	76.2%	0.136 ( $\pm 0.082$ )	64.1%	0.274 ( $\pm 0.095$ )	47.1%
	Triangle	0.615 ( $\pm 0.044$ )	( $\pm 1.3\%$ )	0.605 ( $\pm 0.065$ )	( $\pm 2.6\%$ )	0.560 ( $\pm 0.022$ )	( $\pm 3.8\%$ )	0.409 ( $\pm 0.109$ )	( $\pm 11.9\%$ )
	Rectangle	0.917 ( $\pm 0.020$ )		0.926 ( $\pm 0.022$ )		0.891 ( $\pm 0.061$ )		0.646 ( $\pm 0.170$ )	
	Diamond	0.729 ( $\pm 0.053$ )		0.737 ( $\pm 0.044$ )		0.549 ( $\pm 0.074$ )		0.351 ( $\pm 0.091$ )	
Reconstructed Holograms	Circle	0.382 ( $\pm 0.030$ )	68.1%	0.414 ( $\pm 0.044$ )	67.7%	0.271 ( $\pm 0.022$ )	70.2%	0.216 ( $\pm 0.137$ )	58.4%
	Triangle	0.702 ( $\pm 0.078$ )	( $\pm 3.0\%$ )	0.526 ( $\pm 0.024$ )	( $\pm 1.8\%$ )	0.767 ( $\pm 0.146$ )	( $\pm 7.9\%$ )	0.538 ( $\pm 0.102$ )	( $\pm 7.8\%$ )
	Rectangle	0.947 ( $\pm 0.006$ )		0.912 ( $\pm 0.011$ )		0.950 ( $\pm 0.026$ )		0.868 ( $\pm 0.100$ )	
	Diamond	0.429 ( $\pm 0.042$ )		0.596 ( $\pm 0.050$ )		0.568 ( $\pm 0.083$ )		0.342 ( $\pm 0.147$ )	

<sup>a</sup> standard deviation.

Note: Each value is the mean of the results from five experiments.



**Fig. 13.** Confusion matrices of the clustering results for models pre-trained on synthetic and fine-tuned on real holograms (Group 1 in Table 1) (P) for raw (a) and reconstructed (b) holograms in the real test data (Group 2 in Table 1).

It takes ~0.09 second on average to process a hologram on a low-power CPU board. This makes it possible to interpret holograms in real time when data are collected by a low-power sensor platform.

• Synthetic data can be used to train autoencoder-based clustering of real holograms. Comparing the results for raw and reconstructed holograms, the synthetically trained encoders achieved 64.1% and 70.2% accuracy, respectively. This is significantly better than the results from the models trained only on the real training holograms. Further gains in performance can be achieved using transfer learning techniques, where the models are synthetically pre-trained, and then fine-tuned using real holograms. This increased the accuracy when processing raw holograms to 75.9%. Similar gains in accuracy were not however, achieved for the reconstructed holograms. This performance is comparable to the performance achieved when using a far larger (1.2 million images as opposed to 24,000 synthetic images) generic image database for pre-training, where it is suggested that the SOM used for clustering limits the final accuracy achieved by the proposed method.

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**Data availability.** Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

**supplementary document.** See the supplementary document for supporting content.

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