

1 **A calibrated surface complexation model for carbonate-oil-brine interactions coupled**
2 **with reservoir simulation- application to controlled salinity water flooding**

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5 **Abstract**

6 Vast majority of past studies that have been conducted on controlled salinity water flooding
7 (CSWF) use diffuse layer model (DLM) that calculates only the surface potential, which can
8 be significantly different from the ζ -potential of the interface. Importantly, stability of the
9 water-film (between the oil and the rock surface) which dictates ultimate oil recovery is
10 related to ζ -potential. As such, using DLM calculated surface potential (directly) for CSWF
11 can be misleading. Additionally, most of the existing DLMs use integer charges instead of
12 fractional charges to model carbonate-brine interactions, which may not represent the actual
13 carbonate crystallographic. We present a triple layer surface complexation model (TLM)
14 which offers the option to locate and distribute charge of the adsorbing ion(s) at three
15 locations. TLM can therefore calculate potentials at three different locations within the Stern
16 layer. To the best of our knowledge, only few authors have used TLM to simulate CSWF.
17 However, some surface reactions were ignored in these models. For instance, adsorption of
18 monovalent ions such as Na^+ and Cl^- ions was ignored in some of the few available TLMs.
19 Also, the effect of basic-oil components was not considered in some TLMs, and lastly, some
20 TLMs used integer charges for the carbonate surface group. This study introduced a
21 comprehensive TLM that includes all these complexities. Moreover, we introduced a new
22 wettability indicator (WI) that is related to the electrostatic forces between the oil-brine and
23 the rock-brine interfaces. That is, WI was calculated from ζ -potentials at the oil-brine and
24 rock-brine interfaces.

25 The TLM, built in a geochemical simulator, PHREEQC, was then coupled with UTCHEM, a
26 multiphase reservoir simulator. The developed simulator based on the TLM-CSWF model
27 was tested against several experimentally measured oil recovery data sets. Results of the
28 model suggest that Oil basic component significantly impacts oil-brine interface ζ -potential
29 irrespective of temperature, brine composition, and ionic strength. On the otherhand, Na^+ ions
30 in brine may influence oil-brine ζ -potential, and this relates to temperature, brine
31 composition, and ionic strength. The results further suggest that injection of (sulfate-free)
32 diluted brine in chalk resulted to increased oil adhesion, shifting the reservoir to oil-wet
33 condition. Hence, no additional oil is recovered with this brine injected at tertiary oil recovery
34 stage. Finally, the results showed that wettability is related to ζ -potentials at the oil-brine and
35 rock-brine interfaces, and the carbonate rock would be strongly oil-wet or water-wet only at
36 significantly large magnitude of ζ -potentials at the interfaces.

37 **Keywords:** Low salinity water flooding, Disjoining pressure, Electrical double layer,
38 Wettability alteration, Zeta potential, Controlled salinity water flooding.

39

40 **1. Introduction**

41 CSWF was observed in 1959 when Martin¹ identified higher oil production from fresh water
42 injection in sandstone. It was, however, not recognized until Morrow et al.²⁻⁴ began to do
43 deeper investigation. Currently, many researchers and industries are working tremendously to
44 get more insight into this EOR method. Although there have been numerous reported cases
45 of positive impact of CSWF on oil recovery²⁻⁷, and laboratory experiments show that high
46 recovery is related to CSWF compared to conventional water flooding, however, the
47 underlying mechanism behind the process is not well understood and still opens for further
48 research. In recent years, several mechanisms behind the improved oil recovery have been
49 proposed with some researchers either confirming or refuting them. Studies conducted so far
50 associate the improved oil recovery to wettability alteration in carbonate reservoirs. It is
51 stated that the introduction of CSW into the reservoir induces water-rock-oil interactions
52 which results to wettability alteration⁸.

53 It has been proposed that the wettability alteration is related to the water film stability subject
54 to electrical charges that are generated at the oil-brine and rock-brine interfaces^{6,9-12}.
55 Therefore, brine, which is capable of generating same polarities of ζ -potential at the oil-brine
56 and rock-brine interface will produce a more stable water film between the oil and the rock
57 surface, making the reservoir water wet. Alternatively, Austad et al.⁷; Fathi et al.¹³; Strand et
58 al.¹⁴ and Zhang et al.^{15,16} proposed multi-component ion exchange as the mechanism behind
59 the wettability alteration in carbonate reservoirs. They indicated that adsorption of some
60 specific ions (Ca^{+2} , Mg^{+2} , SO_4^{-2}) can lead to desorption of adsorbed oil from the rock surface,
61 which shifts the reservoir to water-wet state. Other proposed mechanisms responsible for the
62 wettability alteration include rock dissolution^{17,18} and interfacial tension reduction¹⁹.

63 Successful works have proven that improved oil recovery is not exclusively caused by the
64 total dissolved salt, but specific composition and concentrations of the wettability-altering
65 species in the injection water^{5,7}. The interaction between reservoir rocks and fluids, focusing
66 on ionic composition and salinity has been studied by several authors. It was established that
67 rock-brine-oil interaction (i.e.: wettability alteration) is controlled predominantly by pH and
68 potential determining ions (PDI) such as Ca^{2+} , Mg^{2+} , CO_3^{-2} , SO_4^{-2} , and the presence or
69 absence of these ions dictates the amount of oil that can be recovered by CSWF^{7,8,16,20-25}.
70 Ligthelm et al.²⁶, on the other hand, reported that wettability alteration is effective when ionic
71 strength is lowered rather than the action of PDI. Some researchers have also argued that
72 CSWF is complex and explaining it with a single mechanism is difficult^{18,27,28}.

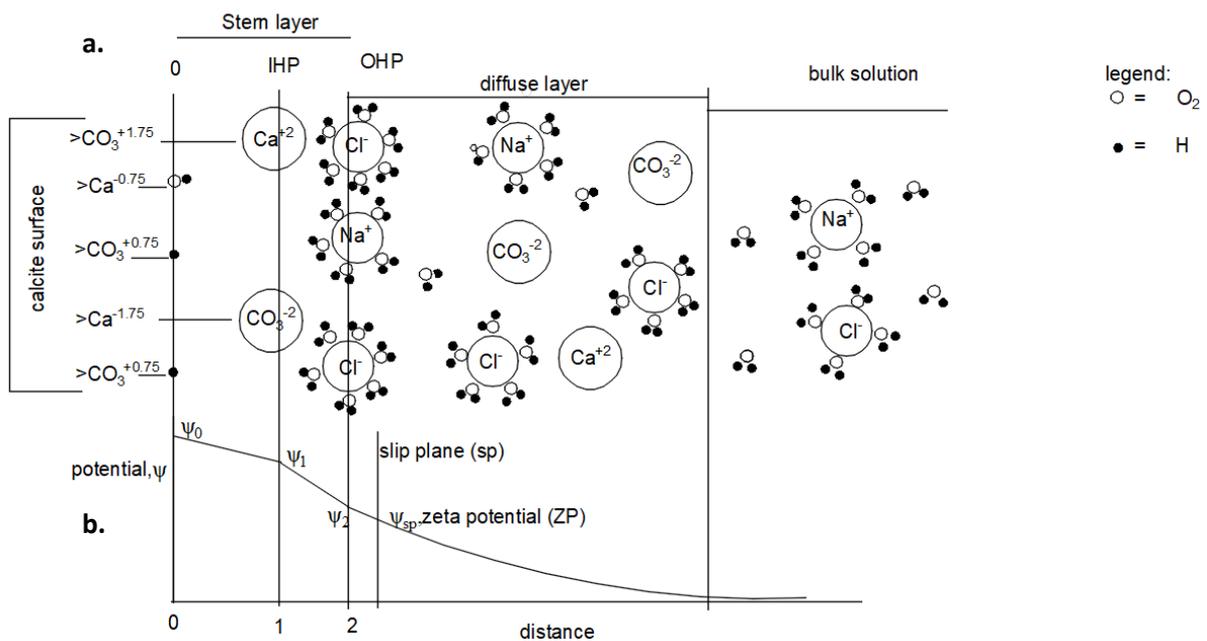
73 **1.1. Theory of electrical double layer (EDL) and zeta potential (ZP)**

74 When a carbonate rock comes into contact with an electrolyte solution, the chemical state of
75 the carbonate surface is usually altered. This leads to the separation of electrical charge at the
76 carbonate-solution interface²⁹. An excess of charge at the carbonate surface is balanced
77 through electrostatic interaction with counter-ions, which are attracted from the adjacent
78 solution to the carbonate surface^{10,29}. This generates first layer at the mineral surface, which
79 is often referred to as the Stern layer. Subsequently, a second layer is generated around the
80 first layer because it could not completely neutralize the surface. This second layer is termed
81 as diffuse layer, and the two layers, together, is called electrical double layer (Figure 1a). It

82 should be noted that the diffuse layer contains both counter-ions and co-ions, with the co-ions
 83 concentration increasing towards the bulk electrolyte solution. It is worth mentioning that the
 84 ions in the Stern layer are strongly adhered to the surface and are compact while the ions in the
 85 diffuse layer are mobile¹⁰.

86 The Stern layer can further be divided into two as inner Helmholtz layer and outer Helmholtz
 87 layer. Thus, inner Helmholtz layer refers to the region between the 0-plane and the inner
 88 Helmholtz plane (IHP) whereas outer Helmholtz layer is the region between the IHP and the
 89 outer Helmholtz plane (OHP). While 0-plane denotes the hydrolysis layer (where OH⁻ and H⁺
 90 are chemi-bonded to the surface ions), IHP defines location of dehydrated ions that are
 91 closely attached to the surface. The OHP, however, defines locations of hydrated ions^{29,30} that
 92 are far from the surface. The IHP and the OHP can also be referred to as 1-plane and 2-plane,
 93 respectively. The Helmholtz layers can be described as capacitors with capacitances C1
 94 (capacitance between the 0-plane and the 1-plane) and C2 (capacitance between the 1-plane
 95 and the 2-plane). The electric potential within the EDL varies with distance from the surface
 96 (Figure 1b), and the potential obtained at the slip plane is called zeta ζ -potential (Figure 1b).

97



98

99 Figure 1: (a) sketch of the electrical double layer at the carbonate-brine interface. The stern layer is described by
 100 three planes: the 0-plane which denotes the hydrolysis layer where OH⁻ and H⁺ are chemi-bonded to the surface
 101 ions; the 1-plane which is location for adsorbed ions closer to the surface; and the 2-plane which is location for
 102 adsorbed ions farther from the surface (b) Schematic representation of electrical potential variation with distance
 103 from the rock surface^{29,30}. The charges deposited at the calcite surface are results of the rock interactions with
 104 the electrolyte ions.

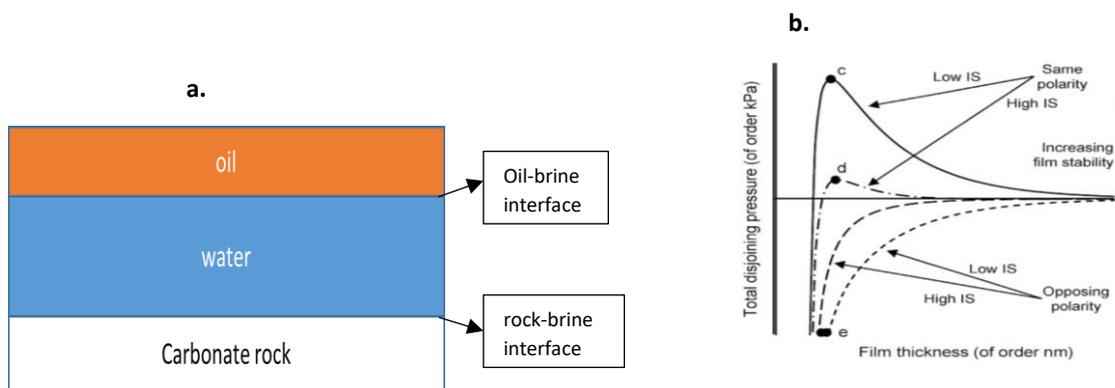
105 1.2. Stability of the water film between the oil and reservoir rock

106 In oil reservoirs, contact between the rock surface and oil is dictated by the stability of the
 107 water film between the oil and the rock surface¹¹. If the water film is unstable, then, oil can
 108 easily adhere to the rock surface, making the reservoir oil-wet or mixed-wet (Figure 2a). The
 109 water film stability is dictated by the disjoining pressure existing between the rock and the

110 fluids. In other word, disjoining pressure can be described as the force that tends to separate
 111 the oil-brine and rock-brine interfaces. It should be noted that a negative disjoining pressure
 112 attracts the two interfaces³¹, making the reservoir oil-wet (Figure 2b).

113 Three forces, namely, van der Waals forces (VDWF), structural forces (SF) and double layer
 114 forces (DLF) of electrostatic in nature contribute to the disjoining pressure. The summation
 115 of these force components is expressed as the total disjoining pressure^{10,31}. For oil-brine-rock
 116 system, VDWF is always considered attractive (i.e.: negative contribution to DP) while SF is
 117 repulsive. On the other hand, DLF can be attractive or repulsive depending on the polarities
 118 of ζ -potential at the oil-brine and rock-brine interfaces. For instance, if the oil-brine and rock-
 119 brine interfaces have the same polarity, DLF will be repulsive, and its contribution to DP will
 120 be positive. This suggests that it is the DLF which dictates DP and water film stability.

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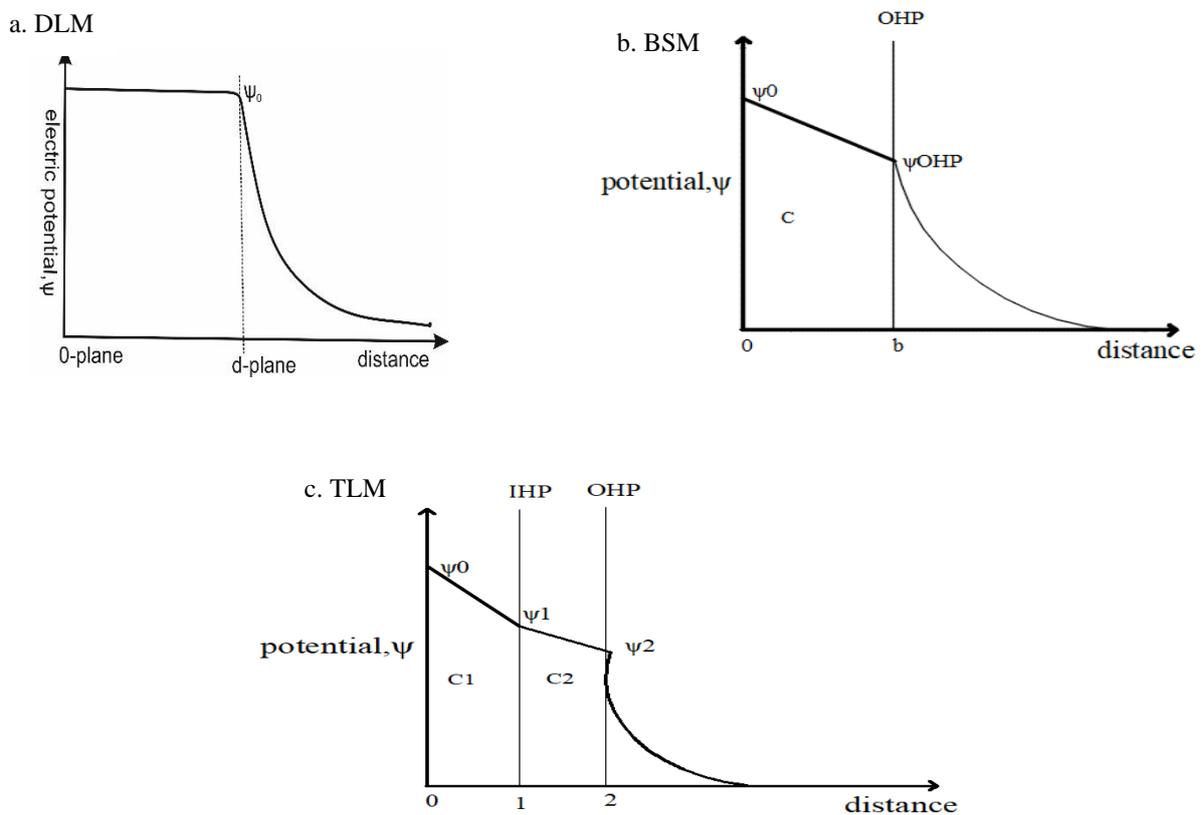
123 Figure 2: schematic representation of: (a) rock-brine-oil system in equilibrium; (b) disjoining pressure isotherm
 124 (Jackson et al.⁶). “c” in the disjoining pressure isotherm denotes stable water-film at low ionic strength; “d” is
 125 partially stable water-film at high ionic strength; and “e” is unstable water-film. Conditions “c” and “d” occur
 126 under same polarities of ζ -potential at the oil-brine and rock-brine interfaces whereas condition “e” denotes
 127 opposite ζ -potential at the interfaces. High ionic strength reduces magnitude of ζ -potential and double layer
 128 thickness, thus, DP can be reduced. “IS” in Figure b signifies ionic strength.

129 1.3. Surface complexation model (SCM) for CSWF

130 Surface complexation models have been used to characterize crude oil-rock-brine (CORB)
 131 interactions in the reservoir^{5,10,17,18,23,32-48}. They have the capability to describe surface
 132 adsorption/desorption phenomena of CORB using chemical reactions, mass balance, charge
 133 balance and equilibrium constants⁴⁹. Some available SCM includes basic Stern model, BSM
 134 (Figure 3b), diffuse layer model, DLM (Figure 3a) and triple layer model, TLM (Figure 3c).
 135 It should be noted that each model differs from the other in its structural representation of
 136 mineral-solution interface. That is, location and configuration of adsorbed species at the
 137 surface⁴⁹. Vast majority of past studies that have been conducted on CSWF use
 138 DLM^{5,17,23,32,42,50-52}, which calculates only the potential at the surface (0-plane). It is
 139 noteworthy that surface potential can be significantly different from the ζ -potential.
 140 Importantly, stability of the water-film which dictates ultimate oil recovery is related to ζ -
 141 potential. As such, using DLM calculated surface potential (directly) for CSWF can be
 142 misleading. Therefore, DLM calculated potential needs to be modified in order to estimate ζ -
 143 potential. That is, a correlation such as Debye-Huckel approximation or Gouy-Chapmann
 144 relation is applied to estimate ζ -potential from DLM calculated surface potential. However,

145 Debye-Huckel approximation is valid at low potential values (surface potential < 25mV),
 146 which limits its application. Furthermore, with asymmetrical solution, complex equations are
 147 required to calculate ζ -potential from the surface potential (Israelachvili.⁵³). BSM, on the
 148 other hand, assumes that protonation/deprotonation reactions take place at the 0-plane, while
 149 all adsorption reactions of ions from the bulk electrolyte take place at the b-plane. In other
 150 words, BSM does not distinguish the Stern layer as IHP and OHP. BSM has been used by
 151 some investigators to model rock-brine interactions^{54,55}. TLM, on the other hand, relies on the
 152 theory that charges are distributed on the 0-plane, the IHP and OHP, which could result in a
 153 ζ -potential value that is calculated directly from the model itself rather than using correlations
 154 to find the ζ -potential as the diffuse layer models require.

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159 Figure 3: (a) schematic representation of diffuse layer model: It comprises of an empty stern layer and a diffuse
 160 layer. Electric potential remains constant from the surface till the onset of the diffuse layer (d-plane), where it
 161 begins to decrease exponentially with distance. (b) Sketch of BSM: It does not separate the Stern layer into IHP
 162 and OHP. (c) Sketch of TLM: The stern layer is described by three planes: the '0-plane', the IHP (1-plane), and
 163 the OHP (2-plane). It requires two capacitance values (C1 and C2) and distribution of its electric potential is
 164 consistent with the EDL theory.

165

166 TLM has been used successfully to model rock-brine interactions (in environmental studies)
 167 by several researchers^{30,56-60}. Stipp⁶¹, through a study conducted on carbonate-brine
 168 interactions indicated that the charge obtained at the calcite lattice ions ($>Ca$ and $>CO_3$) is not
 169 an integer but rather a fraction. Stipp⁶¹ further mentioned that the charge is ± 0.333 if the
 170 bond is pure ionic. This suggests that using integer charges to model carbonate interactions
 171 may not represent the actual carbonate crystallographic. TLM is capable of modelling
 172 carbonate-brine reactions which involve fractional charges. Moreover, the distribution of

173 TLM electric potential is consistent with the electrical double layer (EDL) theory. To the best
174 of our knowledge, only few studies have reported the use of TLM to model CORB
175 interactions and CSWF oil recovery process. Recently, Bonto et al.⁴¹ modelled CSWF but
176 used TLM for the carbonate-brine interactions and DLM for the oil-brine interactions. In
177 addition, their TLM was validated with only one experimental result. Takeya et al.^{37,38} also
178 used TLM to model CORB interactions, however, some oil-brine surface reactions were
179 ignored in the model. Additionally, there is limited literature on oil-brine SCM, and most of
180 the available ones use equilibrium constants at 25°C to model the reactions at various
181 temperatures. Subsequently, a new improved model that can incorporate all these factors is
182 needed to effectively characterise CORB interactions and CSWF process.

183 This study seeks to develop a comprehensive SCM that is capable of modelling and
184 predicting CORB interactions at different temperatures, brine composition/salinity, carbonate
185 mineralogy and oil composition. A TLM was made from Charge-Distribution Multi-site
186 Complexation (CD-MUSIC) built in PHREEQC. We included all the above discussed factors
187 in the developed SCM. In modelling CSWF, the effect of the CSW on oil recovery is
188 simulated via a shift in relative permeability using wettability interpolant (WI). Past papers
189 have proposed various WI models which includes bond product sum (BPS)^{39,40,62,63}, stability
190 number (SN)⁶⁴, available adsorption site⁴¹, concentration of adsorbed oil species at the rock
191 surface^{32,33}. It is interesting to note that reliability of some of these proposed WI have been
192 questioned by some authors as they failed to predict oil recovery trend. For instance, Korrani
193 et al⁶⁴ did not observe correlation between oil recovery and BPS as this WI failed to predict
194 most of the simulated oil recovery data. Also, SN showed no correlation with oil recovery
195 when utilised by Bonto et al⁴¹ to simulate CSWF data. We introduced a new WI that is
196 related to the electrostatic forces between the oil-brine and the rock-brine interfaces. That is,
197 this WI was calculated from ζ -potentials at the oil-brine and rock-brine interfaces. The SCM
198 model was then coupled with a reservoir simulator, UTCHEM, to simulate CSWF oil
199 recovery in carbonate reservoirs. Finally, the model was verified by matching it to several
200 experimentally measured ζ -potential and oil recovery data sets.

201

202 **2. Methodology**

203 A TLM model that calculates oil-brine and carbonate-brine interactions is introduced in the
204 study. The model is made from CD-MUSIC, which is a powerful tool for modelling solid-
205 solution interactions. The TLM is coupled with UTCHEM to simulate CSWF in carbonate
206 porous media. The method developed in this study includes three steps:

- 207 a. Modelling carbonate-brine and oil-brine ζ -potentials: PHREEQC is used to simulate
208 ζ -potentials at the oil-brine and rock-brine interfaces. This was achieved by matching
209 the model to several oil-brine and rock-brine experimentally measured ZP data sets
- 210 b. Modelling CSWF: low salinity waterflooding was simulated using a reservoir
211 simulation package, UTCHEM, coupled with PHREEQC. This coupled model is
212 referred to as TLM-CSWF model
- 213 c. Model validation with published CSWF data sets: the TLM-CSWF model was
214 validated with experimentally measured CSWF data sets

215 **2.1. Modelling carbonate-brine and oil-brine zeta potential**

216 Equilibrium constants and capacitances were estimated for oil-brine and carbonate-brine
217 interactions separately. Oil-brine interaction parameters were first estimated followed by
218 carbonate-brine reaction parameters.

219

220 **2.1.1. Estimating oil-brine reaction equilibrium constants and capacitances**

221 ***a. Oil surface site density determination***

222 Buckley et al.¹¹ indicated that the active surface sites at the oil-brine interface are the acidic
223 and basic components in the crude oil. Two sites, namely, acid site and base site were
224 therefore considered. It should be pointed out that oil acid site-density (N_{COOH}) and base site-
225 density (N_{NH}) were calculated from the total acid number (TAN) and total base number
226 (TBN) of the oil, respectively, using Equation (1 - 2)^{41,64,65}:

227

$$228 \quad N_{COOH} \left(\frac{\text{no. sites}}{\text{nm}^2} \right) = 0.602 \times 10^6 \times \frac{TAN(\text{mgKOH/g oil})}{1000 \times a_{oil} \times MW_{KOH}} \quad (1)$$

$$229 \quad N_{NH} \left(\frac{\text{no. sites}}{\text{nm}^2} \right) = 0.602 \times 10^6 \times \frac{TBN(\text{mgKOH/g oil})}{1000 \times a_{oil} \times MW_{KOH}} \quad (2)$$

230 Where: a_{oil} denotes oil specific surface area in m^2/g , and MW_{KOH} is the molecular weight of
231 KOH, and 0.602×10^6 is a conversion factor from mol/m^2 to $\text{no. sites}/\text{nm}^2$. The TAN and
232 TBN, therefore, are input parameters for acidic and basic sites-densities determination. In this
233 study, we assumed an oil specific surface area of $1.0 \text{ m}^2/\text{g}$.^{40,64}

234 ***b. Locating and distributing charge of the adsorbed ion at the oil-brine interface:***

235 Electrolyte ions interacting with the oil surface have various sizes, and as a result, these ions
236 may be located at different distances from the oil surface⁶⁶. Protonation/deprotonation
237 reactions were assumed to occur in the 0-plane^{30,37,41,55} whereas other sorption reactions were
238 modelled to take place at the 1-plane^{37,41}. Charge change occurring in the 0-plane (i.e.: Z0)
239 and 1-plane (i.e.: Z1) due to the sorption reaction is calculated using Equations 3 and 4⁵⁷:

240

$$241 \quad Z0 = \Delta n_H V_H + f V_{me} \quad (3)$$

$$242 \quad Z1 = (1 - f) V_{me} + \sum m_i z_i \quad (4)$$

243 where Δn_H denotes change in proton at the surface, V_H is valence of the proton,
244 V_{me} is valence of central atom in the aqueous complex, m_i denotes number of ligands present
245 in the 1-plane, z_i is charge of those ligands in the 1-plane and f is charge distribution
246 fraction, which accounts for fraction of V_{me} distributed to the 0-plane. In most cases, the
247 adsorbed ions are treated as point charges, as such; their overall charge is deposited at one
248 specific plane. Consequently, $f = 0$. Based on Taketa et al.³⁷, we assigned the charge of the
249 adsorbed ion to one plane. For instance, the total charge (+2) of Ca^{+2} ion is assumed to be
250 centered at the 1-plane in the Stern layer. Hence, charge change, Z1 at the 1-plane is +2
251 whereas charge change, Z0 at the 0-plane is -1 (due to loss of one proton from the oil
252 surface).

253 **c. Capacitance values:**

254 Previous SCM for carbonate rocks have used large capacitance values. One of such models is
 255 the constant capacitance model developed by Cappellen et al.⁶⁷; where high capacitance value
 256 was used for the carbonate-brine interface. Constant capacitance models, similar to BSM
 257 require only one capacitance value. Wolthers et al.³⁰ also used high capacitance values of
 258 100F/m² for both C1 (capacitance between the 0-plane and the 1-plane) and C2 (capacitance
 259 between the 1-plane and the 2-plane) in their TLM model. However, such high capacitance
 260 values are deemed to be unrealistic and unreasonable with their usage being challenged by
 261 some authors, including, Heberling et al.⁵⁵. They argued that such high capacitance values
 262 would give a Stern layer thickness below 1.0Å. Sjø et al.⁵⁸, when employed C1 and C1 values
 263 of 100F/m² in their TLM, the modelled sorption isotherms were all straight while the
 264 experimental isotherms were strongly curved. Heberling et al.⁵⁵ indicated that the total
 265 capacitance, C_T of the Stern layer should be within the range between 0.1 F/m² and 2.8 F/m².
 266 Some recent SCM have utilized low values of C1 and C2 consistent with the range of values
 267 proposed by Heberling et al.⁵⁵. Bonto et al.⁴¹ used C1 = 1.3F/m² and C2 = 4.5F/m² for a
 268 carbonate-brine TLM. Sjø et al.⁵⁸ also employed constant C2 value of 4.5F/m² while varying
 269 C1 within the range between 1.3 – 3.0F/m². Li et al (2010) (cited in Sjø et al.⁵⁸) estimated C1
 270 and C2 values of 2.8F/m² and C2 4.5F/m², respectively for calcite. Based on Li et al's, we
 271 used C1 = 2.8 F/m² and C2 = 4.5 F/m². Although, capacitance values might change at
 272 different temperatures, but to reduce the number of tuning parameters the above mentioned
 273 capacitances were used in the entire work. Moreover, Wolthers et al³⁰ and Sjø et al^{58,59} did not
 274 observe significant change in the potentials calculated from variations in the capacitance
 275 values. The optimized oil-brine interface reaction parameters are shown by Table 1.

276 Table 1: optimized oil-brine interface reaction parameters. Z0, Z1, correspond to charge change at the 0 and 1
 277 planes, respectively. The enthalpy change was calculated using Van't Hoff equation.

No.	Reactions	log_K at:		Z0	Z1	ΔH°, KJ/mol
		25°C	50°C			
1	>RCOOH <=> >RCOO ⁻ + H ⁺	-4.8	-4.5	-1	0	22.13
2	>N + H <=> >NH ⁺	3.92	3.5	1	0	-30.99
3	>RCOOH + Na ⁺ <=> >RCOONa + H ⁺	-4.2	-4.52	-1	1	-23.61
4	>RCOOH + Ca ⁺² <=> >RCOOCa ⁺ + H ⁺	-3.1	-3.63	-1	2	28.04
5	>RCOOH + Mg ⁺² <=> >RCOOMg ⁺ + H ⁺	-3.58	-3.2	-1	2	-39.1
6	C1, F/m ²	2.8				
7	C2, F/m ²	4.5				

278
 279 **d. ζ-potential estimation**

280 Following other investigators [^{30,37,41,42,68}], we computed ζ-potential assuming that slip plane
 281 coincides with the OHP.⁶⁸. That is, ζ-potential = ψ_{OHP}, where ψ_{OHP} is the potential at the
 282 outer Helmholtz plane calculated by PHREEQC. Hereafter, we matched our model 2-plane
 283 potential to the experimentally measured ζ-potential data sets.

284 2.1.2. Estimating carbonate-brine reaction equilibrium constants and capacitances

285 *a. Carbonate surface site density determination*

286 Two calcite lattice ions, calcium ($>Ca$) and carbonate ($>CO_3$) were considered at the calcite-
287 water interface. Following Stipp⁶¹, fractional charge of 0.25 was assumed for calcite
288 ($>Ca^{+0.25}$; $>CO_3^{-0.25}$) in this study. Bonto et al.⁴¹ and Wolthers et al.³⁰ assumed fractional
289 charge of 0.667 while Heberling et al.⁵⁴ used fractional charge of 0.5. Song et al.⁶⁹ on the
290 other hand, assumed fractional charge of 0.25, consistent with Stipp⁶¹. It should be
291 emphasized that the total surface charge density is not affected by the magnitude of the
292 fractional charge⁵⁴. When calcite is in contact with aqueous solution, its surface sites get
293 hydrated and then protonation/deprotonation reactions take place at 0-plane to yield two new
294 complexes $>CaOH^{-0.75}$ and $>CO_3H^{+0.75}$. Consequently, these principal surface sites; $>CaOH^{-0.75}$,
295 $>CaOH_2^{+0.25}$, $>CO_3H^{+0.75}$, and $>CO_3^{-0.25}$ were used in our model. Moreover, it was
296 assumed that site-density equals 4.95 sites/nm² for each site^{54,69}. Based on Brady &
297 Krumhansl⁷⁰ and Heberling et al.⁵⁴, specific surface area was set to 1.0m²/g.

298 *b. Locating and distributing charge of the adsorbed ion at the rock-brine interface*

299 Similar to the oil-brine interface model, protonation/deprotonation reactions were assumed to
300 occur in the 0-plane, with other sorption reactions occurring in the 1 and 2 planes. One major
301 challenge in SCM is identifying location of the adsorbing ions in the Stern layer. While some
302 authors assume and place all the adsorbing ions either in the 1-plane or the 2-plane, others
303 distribute them between the 1- and 2-planes. For instance, Rahnemaie et al.⁵⁶ specified that
304 monovalent ions such as Cl^- , Na^+ have weak interactions with mineral surfaces, and these
305 ions are adsorbed at the OHP. Bonto et al.⁴¹; and Sørensen et al.⁵⁸, however, modelled all the
306 adsorbing ions at the IHP. Heberling et al.⁵⁵, on the contrary, modelled all the adsorbing ions
307 at the OHP in their developed BSM. Wolthers et al.³⁰ ran sensitivity analysis by simulating
308 CO_3^{2-} , Ca^{+2} and HCO_3^- sorption at the IHP. In another model, the ions were simulated at the
309 OHP. However, potentials calculated from the two models were similar. Takeya et al.⁵³ on
310 the other hand, assumed that Na^+ and Cl^- ions are adsorbed in the diffuse layer while
311 divalent ions are adsorbed at the IHP. In this study, Na^+ and Cl^- ions adsorptions are modelled
312 at the OHP, whereas divalent ions adsorption is modelled at the IHP. Charge change in the
313 planes (i.e.: Z0, Z1) as a result of the sorption reactions are calculated with equations 4 and 5.
314 Also, charge change occurring in the 2-plane (i.e.: Z2) is calculated using equation 5.

315 Regarding CO_3^{2-} , SO_4^{2-} adsorption, part of the adsorbed species is incorporated into the
316 calcite surface (0-plane) through ligand exchange, whereas the remaining part is present in
317 the 1-plane⁵⁷. Consequently, charge of central atom in these ions is distributed between the 0-
318 plane and the 1-plane. Wolthers et al.³⁰ assumed that $f = 0.4$, and further proposed that the
319 value of f does not significantly affect the modelling results. Based on Sørensen et al.⁵⁸, f was set to
320 0.24 in this study. For instance, considering monodentate adsorption of CO_3^{2-} ion ($>CaOH^{-0.75}$
321 + $CO_3^{2-} \rightleftharpoons >CaCO_3^{-1.75} + OH^-$); $Z0 = (-1 \times 1) + (0.24 \times 4) = -0.04$; $Z1 =$
322 $(1 - 0.24) \times (4) + (2 \times (-2)) = -0.96$. On the other hand, the charge of adsorbed Ca^{+2} ,
323 Mg^{+2} , Cl^- and Na^+ was assigned to one plane, as such, $f = 0$.

324
325

326 **c. Capacitance values**

327 The capacitance values used for the oil-brine interface reaction calculations are used for the
 328 modelling of rock-brine interface reactions. That is $C1 = 2.8 \text{ F/m}^2$ and $C2 = 4.5 \text{ F/m}^2$. The
 329 optimized carbonate-brine interface reaction parameters are given by Table 2.

330 Table 2: optimized carbonate-brine interface reaction parameters. Z0, Z1, Z2 denote charge change at the 0, 1,
 331 and 2 planes, respectively. The optimized log-K values are consistent with several literature values^{5,30,32,41,52}.

No.	Reaction	log-K at:			Z0	Z1	Z2
		25°C	65°C	120°C			
8	$>\text{CaOH}^{+0.75} + \text{H}^+ \Leftrightarrow >\text{CaOH}_2^{+0.25}$	11.8	10.82	9.89	1	0	0
9	$>\text{CaOH}^{+0.75} + \text{CO}_3^{-2} \Leftrightarrow >\text{CaCO}_3^{-1.75} + \text{OH}^-$	1.25	1.35	1.5	-0.04	-0.96	0
10	$>\text{CaOH}^{+0.75} + \text{SO}_4^{-2} \Leftrightarrow >\text{CaSO}_4^{-1.75} + \text{OH}^-$	2.47	2.86	3.1	0.44	-1.44	0
11	$>\text{CaOH}_2^{+0.25} + \text{Cl}^- \Leftrightarrow >\text{CaOH}_2^{+0.25} \dots\dots\text{Cl}^-$	-1.1	-3.35	-5.4	0	0	-1
12	$>\text{CO}_3\text{H}^{+0.75} \Leftrightarrow >\text{CO}_3^{-0.25} + \text{H}^+$	-3.54	-3.0	-3.0	-1	0	0
13	$>\text{CO}_3\text{H}^{+0.75} + \text{Ca}^{+2} \Leftrightarrow >\text{CO}_3\text{Ca}^{+1.75} + \text{H}^+$	-2.9	-2.35	-1.3	-1	2	0
14	$>\text{CO}_3\text{H}^{+0.75} + \text{Mg}^{+2} \Leftrightarrow >\text{CO}_3\text{Mg}^{+1.75} + \text{H}^+$	-2.9	-2.15	-1.27	-1	2	0
15	$>\text{CO}_3^{-0.25} + \text{Na}^+ \Leftrightarrow >\text{CO}_3^{-0.25} \dots\dots\text{Na}^+$	-1.15	-2.1	-2.7	0	0	1
16	C1, F/m ²	2.8					
17	C2, F/m ²	4.5					

332

333 **2.2. Implementing CSWF**

334 UTCHEM, a three-dimensional, non-isothermal, multiphase flow simulator developed by the
 335 University of Texas at Austin.⁷¹ is used to simulate core flooding experiments carried out on
 336 cylindrical rock samples. Assess to UTCHEM was acquired from the University of Texas at
 337 Austin in 2009, when it was an open source. One-dimensional numerical models with 30 grid
 338 blocks in x-direction were used to simulate CSWF processes that were conducted on core
 339 samples in the previous studies. A wettability indicator calculated from ζ -potentials was
 340 implemented in the model to account for the effect of CSWF on oil recovery. We achieved
 341 this by coupling UTCHEM with PHREEQCRM. PHREEQC, a general-purpose geochemical
 342 simulator, is capable of modelling interactions between water and gases, surface complexes,
 343 minerals, ion exchangers, and solid solutions⁷². However, coupling PHREEQC with
 344 multiphase simulators can be inefficient when running millions of calculations⁷².
 345 PHREEQCRM is designed specifically to ease coupling of PHREEQC with multiphase flow
 346 simulators. It offers a high-level interface that permits flow simulators to implement
 347 geochemical reactions with a minimum amount of programming, whilst ensuring utilisation
 348 of the full functionality of PHREEQC's reaction capabilities. Thus, it allows one to use
 349 PHREEQC as a reaction engine for the transport simulator⁷². The method utilized to model
 350 the CSWF is described below:

351 **a. Coupling UTCHEM with PHREEQCRM**

352 Although, in fluid flow, transport and geochemical reactions occur simultaneously, this work
 353 solved transport and reaction equations separately, using UTCHEM for fluid transport and

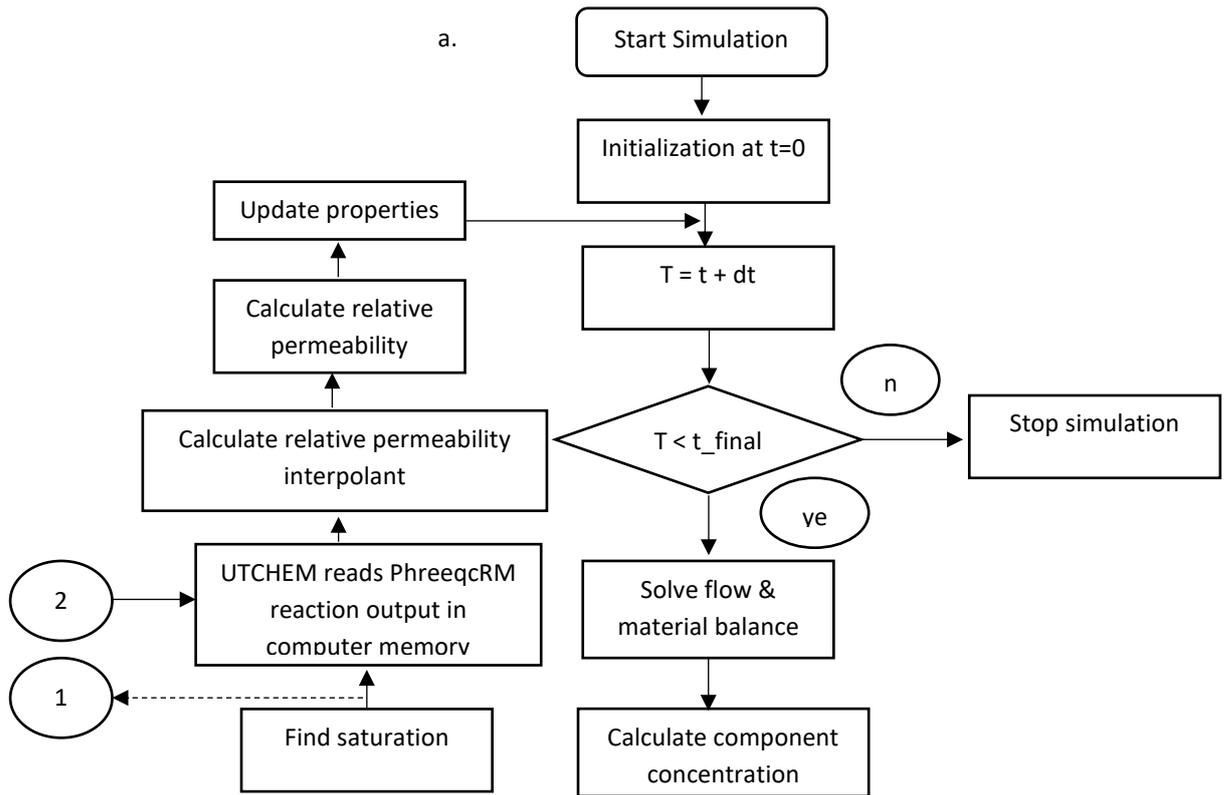
354 PHREEQCRM for geochemical reaction calculations. A sequential non-iterative approach
355 reported by Korrani et al.^{43,51,73,74} and Parkhurst & Wissmeier.⁷² was adopted. Thus, this
356 approach does not require iteration between the two simulators.⁴³ In this method, chemical
357 reactions are not involved when UTCHEM solves the mass conservation equation. It is worth
358 mentioning that PHREEQCRM calculated number of moles of mineral and surface species
359 are saved automatically at each time step.^{43,75} Hence, it is only the solution components that
360 are modified at each time step.⁴³ The coupling steps are summarized below:

- 361 i. UTCHEM calculates elements concentration (mol/l) in brine after each time-step in
362 each numerical grid-block
- 363 ii. This data is exported to PHREEQCRM, which simulates the zeta potential at the oil-
364 brine and rock-brine interfaces
- 365 iii. Zeta potential is imported into UTCHEM model, which is then used to compute
366 wettability interpolant for relative permeability calculation. Also, PHREEQCRM
367 calculated elements concentrations are imported into UTCHEM to update its brine
368 concentration
- 369 iv. With the recalculated relative permeability for each grid-block, the next time step is
370 simulated and produces new ion concentrations
- 371 v. The procedure repeats until the final time-step, consistent with the experimental data
372 is reached

373 Figure 4 below shows the UTCHEM-PHREEQCRM flowchart. It is important to note that
374 total hydrogen, total oxygen, and charge imbalance (CB) are also transported to
375 PHREEQCRM. To obtain equivalent volume of solution (V_{H_2O}) in UTCHEM and
376 PHREEQCRM grid-blocks, UTCHEM grid block volume (in litres), water saturation and
377 porosity are used in PHREEQCRM to calculate V_{H_2O} . The data transfer (i.e.: reading of data)
378 between UTCHEM and PHREEQCRM occurred in the computer memory, as such, writing
379 and/or reading of files is not required. We verified our coupled UTCHEM-PHREEQCRM
380 model with PHREEQC before using it for the CSWF simulations. Detailed description of the
381 verification process is given in the discussion of results section (section 3.3).

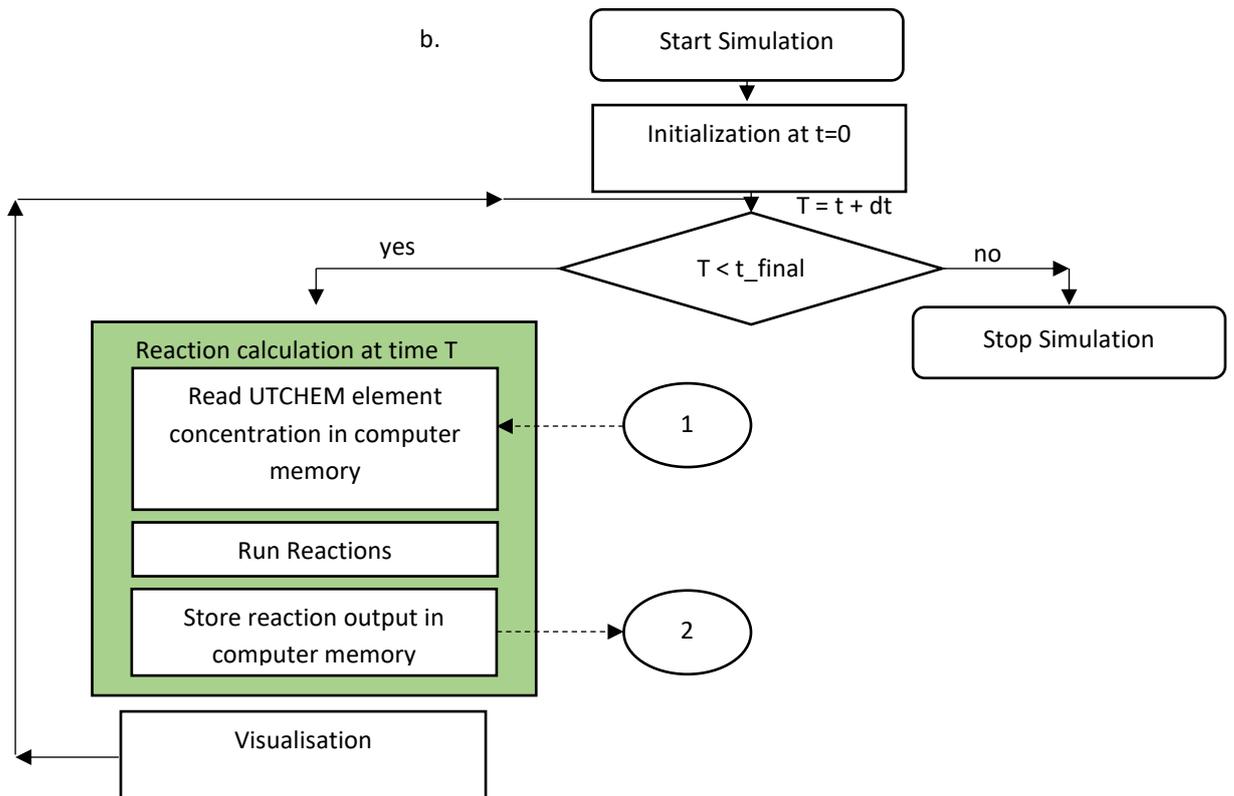
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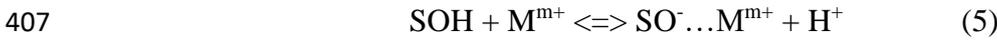
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387

Figure 4: UTCHEM-PHREEQCRM coupling flowchart. (a) UTCHEM simulator, and (b) PHREEQCRM simulator.

388 **b. Implementation of wettability alteration**

389 In our UTCHEM CSWF simulation, we model wettability alteration due to the low salinity
 390 effect via a shift in relative permeability curves. Therefore, two sets of relative permeability
 391 curves are used; one for the initial conditions of brine salinity and the other, for final state,
 392 where the total concentration of the pore-space aqueous phase is reduced to the salinity of the
 393 injected low salinity brine. The two relative permeability curves are then interpolated to
 394 obtain the relative permeability consistent with the current carbonate-oil-brine (COB)
 395 condition. We developed wettability interpolant that considers ζ -potentials at oil-brine and
 396 rock-brine interfaces. Several researchers^{39-41,76} have pointed out that oil surface species (i.e.:
 397 COO^- , COOCa^+ , NH_2^+ , COOMg^+) can be adsorbed at the carbonate surface to alter
 398 wettability. Nonetheless, it is important to note that a certain amount of work must be done
 399 for the adsorption of ionic species in electrostatic models. This electrostatic work done is
 400 equivalent to $\exp\left(\frac{mF\psi}{RT}\right)$,⁵⁷, where F is Faraday constant $\left(96485 \frac{\text{C}}{\text{mol}}\right)$; R is universal gas
 401 constant (8.314 J/K.mol) ; T is absolute temperature in K; ψ is potential in volts and m
 402 denotes charge at the surface. Bonto et al⁴¹ indicated that oil species must travel through two
 403 electrostatic fields (i.e.: oil-brine interface EDL & rock-brine interface EDL) before arriving
 404 at the carbonate surface. They further developed a parameter called available adsorption site
 405 (Equations 7 and 8), AAS, from triple layer reactions proposed by Goldberg.^{49,77} (Equations 5
 406 and 6):



408
$$K = \frac{[\text{SO}^- \dots \text{M}^{m+}][\text{H}^+]}{[\text{SOH}][\text{M}^{m+}]} \exp\left(\frac{F(m\psi_1 - \psi_0)}{RT}\right) \quad (6)$$

409 Then, AAS for COB:
$$\text{AAS}_{\text{Ca}} = \frac{[\text{CaOH}_2^{+0.333}]}{\exp\left(\frac{\psi_{\text{rock}} - \psi_{\text{oil}}}{T}\right)} \quad (7)$$

410
$$\text{AAS}_{\text{CO}_3} = \frac{[\text{CO}_3^{-0.333}]}{\exp\left(\frac{\psi_{\text{oil}} - \psi_{\text{rock}}}{T}\right)} \quad (8)$$

411 Where SOH is the mineral surface species, M^{m+} is ion M in brine with charge m, $\text{SO}^- \dots \text{M}^{m+}$
 412 is surface adsorbed ion M, ψ_1 is potential at 1-plane, ψ_0 is potential at 0-plane, and K is
 413 equilibrium constant for the reaction. Large AAS implies high available $\text{CaOH}_2^{+0.333}$ and/or
 414 $\text{CO}_3^{-0.333}$ sites to adsorb oil, signifying low oil recovery. We adopted this formulation and
 415 developed a wettability parameter.

416 Regarding COB system, SOH and M^{m+} are equivalent to rock-brine and oil-brine surface
 417 species, respectively. $\text{SO}^- \dots \text{M}^{m+}$ also corresponds to the adsorbed oil species at the rock
 418 surface. However, numerous competing reactions occurring between the rock and the oil
 419 surface species make it difficult to identify the specific species responsible for wettability
 420 alteration³⁹. Brady et al^{39,40} suggested several of these COB reactions and proposed that the
 421 electrostatic linkages of $>\text{CaOH}_2^+$ and COO^- , and also $>\text{CO}_3^-$ and NH^+ are dominants. They
 422 further explained that the presence of Ca^{+2} , Mg^{+2} and SO_4^{-2} ions in brine can affect the
 423 electrostatic linkage. That is, SO_4^{-2} adsorption at the carbonate surface can reduce $>\text{CaOH}_2^+$

424 sites whereas Ca^{+2} , Mg^{+2} adsorptions can reduce COO^- sites at the oil surface. Ding et al⁷⁶
 425 also attributed adsorption of oil to the interactions between: $>\text{CaOH}_2^+$ and COO^- , $>\text{CO}_3\text{Ca}^+$
 426 and COO^- , $>\text{CO}_3\text{Mg}^+$ and COO^- . On the other hand, Korrani et al⁴⁴ did not observe any
 427 correlations between sum product of the surface species and oil recovery as it failed to predict
 428 most of the CSWF that they conducted. Nonetheless, oil adhesion does not depend on only
 429 surface species but also the electrostatic force (electrostatic work) between the oil and the
 430 rock surface, as observed in Equation 7 - 8. That is, irrespective of the surface linkage
 431 involved, amount of the adsorbing species relates to the electrostatic force between oil and
 432 rock.

433 We propose a wettability indicator, β , that is related to the total electrostatic work. This count
 434 for the total work associated with two planes with ζ -potentials. Therefore, the proposed
 435 wettability indicator is calculated from the ζ -potentials at the oil-brine and the rock-brine
 436 interfaces, and the value of β gives an indication of the wetting condition of the reservoir. β
 437 is calculated as:

$$438 \quad \begin{cases} \beta = \exp\left[\frac{F(|\psi_{ob}| + |\psi_{rb}|)}{RT}\right] \times (-1)^n, & \text{for } (\psi_{ob} \times \psi_{rb}) \neq 0 \\ \beta = 0, & \text{for } (\psi_{ob} \times \psi_{rb}) = 0 \end{cases} \quad (9)$$

439 where:

440 $n = 2$; for $(\psi_{ob} \times \psi_{rb}) > 0$

441 $n = 1$; for $(\psi_{ob} \times \psi_{rb}) < 0$

442 ψ_{ob} and ψ_{rb} are ζ -potentials (in volts, V) at the oil-brine and the rock-brine interfaces,
 443 respectively. $(-1)^n$ in Equation 9 simplifies the effect of charge (m) on the total work. A
 444 high value of the wettability indicator implies strong electrostatic forces (either attractive or
 445 repulsive) between the oil and the rock. The reservoir is classified as an oil-wet system when
 446 $\beta < 0$, and this occurs when the ζ -potentials are of the opposite polarities. $\beta > 0$ occurs
 447 when both ζ -potentials are of the same polarities, indicating a water-wet reservoir. However,
 448 the reservoir is neutral wet or intermediate wet when $\beta = 0$, which happens when one or both
 449 ζ -potentials are zero. Therefore, if wettability is controlled by the electrostatic interactions,
 450 then only when the electrostatic repulsion (or attraction) between rock-brine and oil-brine
 451 interfaces is strong, i.e., both ζ -potentials at rock-brine and oil-brine interfaces are of
 452 significant magnitude and same (or opposite) polarities, that the mineral surface will be
 453 strongly water-wet (or oil-wet). In CSWF, the objective is to increase β from its initial value
 454 to a positively larger value at the final state to improve the oil recovery factor.

455 To apply the new wettability indicator concept in CSWF simulations, two sets of β are
 456 calculated: one for the initial conditions of brine salinity ($\beta^{initial}$) and one for the final state,
 457 where the total concentration of the pore-space aqueous phase is reduced to the salinity of the
 458 injected CSW (β^{final}). Then, during a time-step, β^t consistent with the current COB
 459 condition is calculated. The relative permeability interpolant, ω , is therefore calculated as:

$$460 \quad \omega = \frac{\beta^t - \beta^{final}}{\beta^{initial} - \beta^{final}} \quad (10)$$

461 $[\omega = \max(\omega, 0) \text{ or } \omega = \min(\omega, 1)]$

462 β^t is assumed to not exceed $\beta^{initial}$ or β^{final} , and even at some point in transition, from oil-
 463 wet to water-wet where β^t exceeds $\beta^{initial}$ or β^{final} , ω calculated will be zero or one. We
 464 then interpolated end-point relative permeabilities and Corey's exponents (Equations 11 –
 465 14):

466
$$K_{ro}^o = \omega K_{ro}^{ow} + (1 - \omega) K_{ro}^{ww} \quad (11)$$

467
$$K_{rw}^o = \omega K_{rw}^{ow} + (1 - \omega) K_{rw}^{ww} \quad (12)$$

468
$$n_o = \omega n_o^{ow} + (1 - \omega) n_o^{ww} \quad (13)$$

469
$$n_w = \omega n_w^{ow} + (1 - \omega) n_w^{ww} \quad (14)$$

470 Reduction in residual oil saturation due to CSWF effect was expressed using Equation 15,
 471 similar to interpretation of the end-point relative permeability curves:

472
$$S_{or} = \omega S_{or}^{ow} + (1 - \omega) S_{or}^{ww} \quad (15)$$

473 where: K_{ro}^{ww} corresponds to the end-point relative permeability to oil at water-wet condition,
 474 K_{ro}^{ow} is end-point relative permeability to oil at oil-wet condition, and K_{ro}^o is current end-
 475 point relative permeability to oil. K_{rw}^{ww} denotes end-point relative permeability to water at
 476 water-wet condition, K_{rw}^{ow} is end-point relative permeability to water at oil-wet state and K_{rw}^o
 477 is current end-point relative permeability to water. Also, n_o^{ow} is oil Corey's exponent at oil-
 478 wet state, n_o^{ww} is oil Corey's exponent at water-wet state and n_o is current Corey's exponent
 479 for oil. n_w^{ow} is water Corey's exponent at oil-wet state, n_w^{ww} is water Corey's exponent at
 480 water-wet state and n_w is current Corey's exponent for water. S_{or}^{ww} corresponds to residual oil
 481 saturation at water-wet state; S_{or}^{ow} is residual oil saturation at oil-wet condition and S_{or}
 482 denotes current residual oil saturation.

483 Finally, relative permeability to water (K_{rw}) and oil (K_{ro}) during CSWF process is calculated
 484 from Brooks and Corey's correlation (Equations 16 - 18):

485
$$K_{rw} = K_{rw}^o (S_n)^{nw} \quad (16)$$

486
$$K_{ro} = K_{ro}^o (1 - S_n)^{no} \quad (17)$$

487
$$S_n = \frac{S_w - S_{wc}}{1 - S_{wc} - S_{or}} \quad (18)$$

488 where S_w denotes water saturation; S_{wc} is irreducible water saturation; S_n is normalized water
 489 saturation.

490 **2.3. CSWF data sets for validation of the model**

491 To investigate the accuracy of the proposed TLM-CSWF model, it was tested against
 492 different sets of experimental results that were reported by Fathi et al.¹³, Yousef et al.⁷⁸,
 493 Austad et al.⁷, and Sharma & Mohanty⁷⁹. Fathi et al.¹³ performed tertiary CSWF experiments

494 where formation brine (FW) was first injected followed by seawater (SW), and then 10000
 495 times diluted SW (SW/10000). Similarly, Yousef et al.⁷⁸ and Austad et al.⁷ conducted tertiary
 496 CSWF tests. The experimental data from these studies is given by Table 3 and 4, and we used
 497 these oil recovery results in the next sections of the study.

498 Table 3: Properties of rock and oil used by the authors

Property	Fathi (2010)	Yousef (2010)	Austad (2012)	Sharma & Mohanty (2018)
Porosity, fraction	0.45	0.25, 0.2465	0.18	0.28
Permeability, mD	1 - 2	39.6, 68.3	1.2	20
Diameter, cm	3.81	3.8, 3.81	3.8	3.81
Length, cm	7.0	16.24, 23.65	8.1	30.48
Initial Water saturation, fraction	0.08	0.104, 0.144	0.07	1.0
Initial Pressure, bar	10	13.8	10	6.89
Reservoir Temperature, °C	120	100	110	120
Injection rate, cm ³ /day	36	1440	144	173.74
AN, mg KOH/g oil	1.9	0.25	0.7	-
BN, mg KOH/g oil	-	-	0.42	-
Oil density, g/cm ³ at 25°C	0.811	0.72 at 100°C	0.818 at 20°C	-
Oil viscosity, cp at 25°C	3.38	2.03 at 100°C	3.8 at 20°C	-
Injection sequence	FW=>SW	FW=>SW=>0.5SW =>0.1SW=>0.05SW	FW=>0.01FW	a. FW=>SW b. FW=>SW=>SW4SO4

499 Table 4: Composition of the brines used by the authors. For SW₂SO₄⁻² and SW₄SO₄⁻², SO₄⁻² concentration in
 500 the SW is increased by two-fold and four-fold, respectively.
 501

Fathi et al (2010), mol/l								
Brine/ion	Na ⁺	Ca ²⁺	Mg ²⁺	SO ₄ ⁻²	Cl ⁻	K ⁺	HCO ₃ ⁻	TDS
FW	1.0	0.029	0.008	0.0	1.07	0.005	0.009	62800 (ppm)
SW	0.45	0.013	0.045	0.024	0.525	0.01	0.002	33390 (ppm)
Yousef (2010), ppm								
FW	59491	19040	2349	350	132060	0	354	213734 (ppm)
SW	18300	650	2110	4290	32200	0	120	57670 (ppm)
Austad (2012), mol/l								
FW	2.62	0.437	0.076	0	3.643	0	3e-3	208940 (ppm)
FW/100	262e-2	4.37e-3	7.6e-4	0	3.643e-2	0	3e-5	2089.4 (ppm)
Sharma & Mohanty (2018), ppm								
FW	41411	11686	2763	215	103002	0	0	149160 (ppm)
SW	12891	510	1600	3485	26578	0	0	41127 (ppm)

502

503 3. Results and Discussion

504 3.1. oil-brine interface ζ -potential

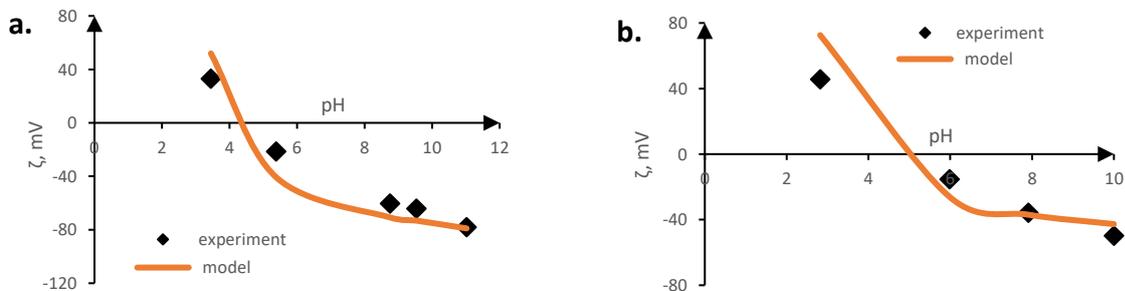
505 Before using the proposed TLM model for CSW simulations, we validated it with
506 experimentally measured ζ -potentials from past studies. It should be noted that matching our
507 model to experimental ζ -potential data was performed with PHREEQC software. To test the
508 model reliability, different cases of experimental data were used (i.e., experiments with
509 different oil and brine properties). Experimentally, oil-brine ζ -potential is measured by
510 Electrokinetics using oil-water emulsions. For simplification, single-stage equilibration and
511 two-stage equilibration were used to describe the experimental condition at which ζ -potential
512 was measured. Single-stage equilibration denotes the state whereby ζ -potential is measured
513 after initial equilibration of the oil-brine emulsion without modifying its pH, salinity, or
514 composition. Two-stage equilibration represents the state whereby ζ -potential is measured
515 after the initial equilibrated emulsion is modified. Thus, either pH of the equilibrated
516 emulsions is altered (by addition of HCl/NaOH) or addition of specific brine(s). It is worth
517 noting that whichever method was involved in the measurement, the same approach was
518 followed in the modelling. Furthermore, we compared the ζ -potentials from our TLM with
519 outputs from the existing oil-brine SCM.

520 3.1.1. Comparing the oil-brine TLM with experimental cases

521 In this part, ζ -potentials of the oil-brine interface from four experimental cases were
522 compared with the proposed TLM in this study, which is explained below:

523 *Case 1:*

524 We first present results of the model matched to the experimental results of Alshakhs &
525 Kovscek.⁹ (Figure 5). They measured oil-brine ζ -potential at 25°C (brine composed of Na, Cl,
526 Mg, SO₄). Measurement was undertaken at two-stage equilibration state, by modifying pH of
527 the initial equilibrated oil-brine emulsion solution. We calculated acid site-density of 12.35
528 sites/nm² and base site-density of 13.4 sites/nm² from the TAN (1.15 mgKOH/g oil) and TBN
529 (1.25 mgKOH/g oil), respectively. We also used our earlier calculated capacitances (C1 =
530 2.84, C2 = 4.48 F/m²). Hence, the only parameter that we tuned in matching the model to the
531 experimental data was oil-brine interface reactions constants. The optimized reactions
532 constants are provided in Table 1.



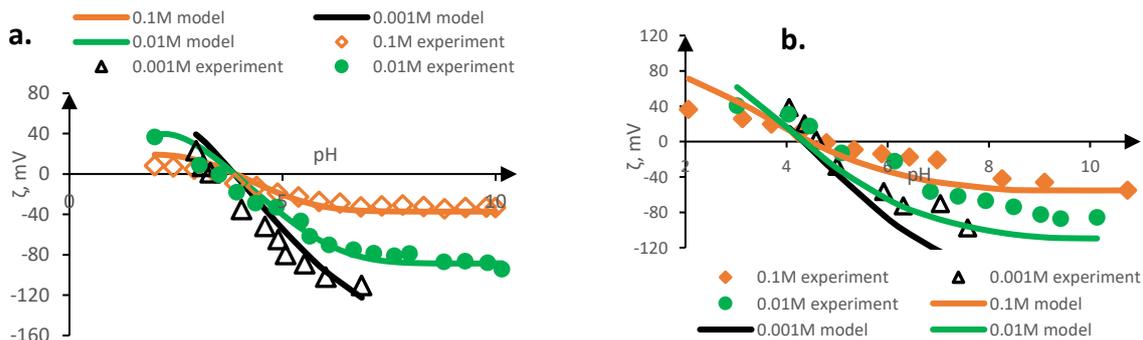
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534 Figure 5: comparison of the model (this study) and experimental data (Alshakhs & Kovscek.⁹) of oil-brine ζ -
535 potential. (a) 1000 times diluted sea water, and (b) 100 times diluted MgSO₄

536

537 *Case 2:*

538 The oil-brine interface model validation was extended to the experimental ζ -potential data of
539 Buckley et al.¹¹ (Figure 6). They measured ζ -potential using NaCl brines of different
540 concentrations (i.e.: 0.1, 0.01, 0.001M) and two different oils (Moutray and Leduc oil) at
541 25°C. They used two-stage equilibration process by modifying pH of the equilibrated
542 emulsion solution. Also, we used our capacitance values ($C1 = 2.84$ and $C2 = 4.48$ F/m²) and
543 the optimized oil-brine reactions constants generated from the previous match (i.e.: Alshakhs
544 & Kavscek.⁹ matched equilibrium constants). The authors reported TAN of 0.26 mgKOH/g
545 oil and 0.15 mg KOH/g for Moutray and Leduc oil, respectively. However, TBN was not
546 given. Therefore, we directly used the reported acid site-density of 0.5/nm² and 1.55/nm² for
547 Moutray and Leduc oil, respectively. Also, we used the reported base site-density of 0.1/nm²
548 and 1.4/nm² for Moutray and Leduc oil, respectively. The model matches well with the
549 experimental data. ζ -potential of both oils remained positive until the iso-electric point (IEP),
550 where it begins to shift towards negative. The ζ -potential increasingly becomes negative with
551 increasing pH because the acidic oil component greatly dissociates at high pH value,
552 generating more negative charges at the oil-brine interface. It can be observed that magnitude
553 of the ζ -potential decreases with increasing NaCl concentration while polarity remained
554 unchanged. As we mentioned earlier, increasing ionic strength decreases ζ -potential.

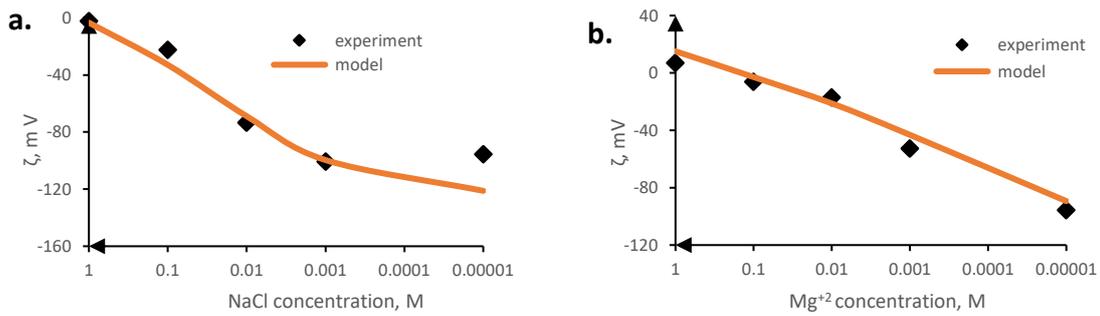


555

556 Figure 6: comparison of the model (this study) and experimental data (Buckley et al.¹¹) of oil-brine ζ -potential
557 with various concentrations of NaCl brine. (a) Moutray oil, and (b) Leduc oil

558 *Case 3:*

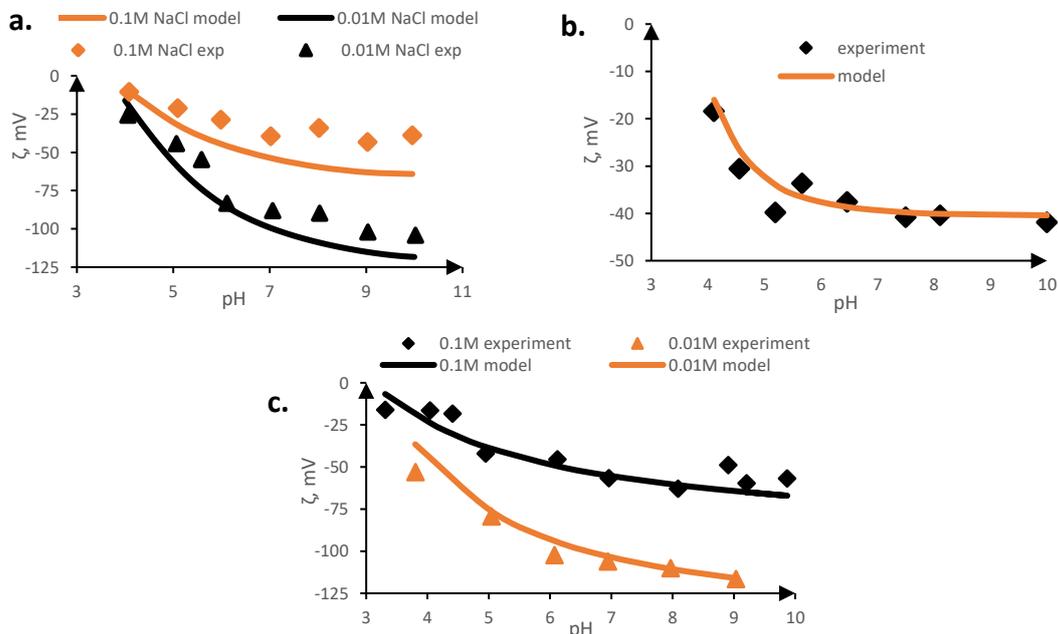
559 We also matched our oil-brine interface model to experimental ζ -potential results of Lu et
560 al.⁸⁰. They measured oil-brine ζ -potential using two different brines (NaCl and MgCl₂) of
561 varying concentrations. The experiment was conducted under single-stage equilibration
562 process at 25°C. Again, we used the same oil-brine reactions constants optimized earlier and
563 our calculated capacitance values. We obtained acid site-density (1.93 sites/nm²) and base
564 site-density (12.2 sites/nm²) calculated from the reported TAN (0.18 mgKOH/g oil) and TBN
565 (1.14 mgKOH/g oil), respectively. The model predicted accurately the ζ -potential trend
566 (Figure 7).



567
 568 Figure 7: comparison of the model (this study) and experimental data (Lu et al.⁸⁰) oil-brine ζ -potential with
 569 various concentrations of NaCl and MgCl₂ brines. (a) NaCl brines, and (b) MgCl₂ brines

570 *Case 4:*

571 Our next match is Chow & Takamura.⁸¹ oil-brine ζ -potential data measured at 25°C. Two
 572 separate brines: NaCl brine of different concentrations, and NaCl-CaCl₂ mixture were used.
 573 Also, two oil types (bitumen and Moutray oil) were used for the experiment. The authors
 574 reported only TAN (0.26 mgKOH/g oil) for the Moutray oil and TAN (2.0 mgKOH/g oil) for
 575 the bitumen. We calculated bitumen acid site-density (21.5 sites/nm²) and Moutray oil acid
 576 site-density (2.79 mgKOH/g oil) from their TAN. We therefore matched the ζ -potential data
 577 to our model by using the base sites-densities as tuning parameter. Capacitances and all other
 578 oil-brine reactions constants remained unchanged. The model results are shown by Figure 8.
 579 Base site-densities were estimated as 0.35 site/nm² for bitumen, and 0.27 site/nm² for
 580 Moutray oil. Some of the model results could not match the experimental data, and this could
 581 be caused by the base site-densities used in the model.



582
 583
 584 Figure 8: comparison of the model (this study) and experimental data (Chow & Takamura.⁸¹) of oil-brine ζ -
 585 potential with two different oils and various brines. (a) Moutray oil and NaCl brine, (b) Moutray oil and NaCl-
 586 CaCl₂ mixture, and (c) bitumen and NaCl brine.

587 **3.1.2. Comparing the oil-brine TLM with DLM**

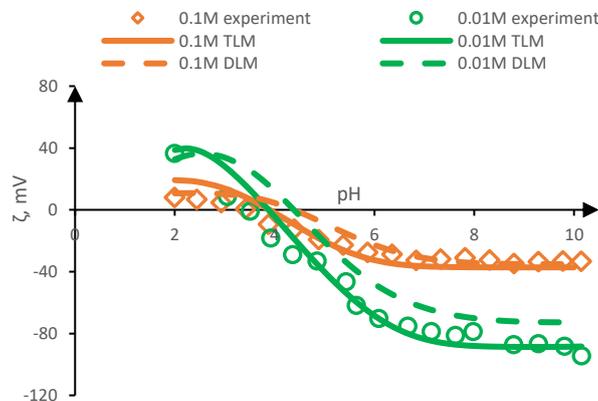
588 We now employed existing oil-brine SCM to simulate some experimental ζ -potential data
 589 sets. Brady et al.^{40,41} proposed DLM for oil-brine interface interactions (Table 5). However,
 590 their model was not matched with experimental ζ -potential data because the authors were
 591 more interested in surface species, which were used in bond product estimation. We used
 592 their model parameters and also our TLM to calculate experimental ζ -potential of Buckley et
 593 al.¹¹. We do not intend to compare the two models but to demonstrate that TLM calculated
 594 potentials can be used directly as ζ -potential, without the need to employ any correlations for
 595 their estimation. It should be pointed out that the NaCl solution used for the experiment is a
 596 symmetrical electrolyte solution. Moreover, some of the DLM potentials exceeded 25mV,
 597 hence, Gouy-Chapmann relation (Equation 19).^{53,64} was used to estimate ζ -potential from the
 598 DLM surface potential:

$$599 \quad \zeta = \psi_x = \frac{4k_b}{e} \gamma \exp(-Kx) \quad (19)$$

$$600 \quad \gamma = \tanh\left(\frac{e\psi_o}{4k_bT}\right) \quad (20)$$

$$601 \quad \frac{1}{K} = \left(\frac{\epsilon_r \epsilon_0 k_b T}{2N_A e^2 I}\right)^{0.5} \quad (21)$$

602 where: I = ionic strength (mol/m³), ϵ_0 = permittivity of free space ($8.854 \times 10^{-12} \text{ C}^2/\text{J.m}$),
 603 ϵ_r = relative permittivity of water (78.5 at 25°C), k_b = Boltzmann constant. Also, T = absolute
 604 temperature (K), N_A = Avogadro number ($6.02 \times 10^{23} \text{ mol}^{-1}$), e = elementary charge
 605 ($1.602 \times 10^{-19} \text{ C}$), $\frac{1}{K}$ = Debye length (m), x = slip plane distance (m), ψ_o = surface potential
 606 (Volts), and ζ = zeta potential (Volts). To compute DLM ζ -potential, we assumed that $x =$
 607 0.6 nm .¹¹. The result shows that both the TLM and DLM produced good match with the
 608 experimental ζ -potential data for the 0.1M NaCl solution (Figure 9). The TLM, however,
 609 offered a better match for the 0.01M NaCl solution. As we have indicated earlier, DLM ζ -
 610 potential computation from surface potential involving asymmetrical solution would require
 611 complex equation.⁵³. CSWF, usually, involves asymmetrical solution, which implies that
 612 complex correlation is required to estimate zeta potential from the DLM calculated surface
 613 potential. As such, TLM, which estimates ζ -potential directly without the need to introduce
 614 any correlation is suggested.



615
 616 Figure 9: comparison of oil-brine interface potential calculated with our model (TLM) and DLM proposed by
 617 Brady et al^{40,41}. Buckley et al experimentally measured ζ -potential was used for the modelling.¹¹.

Table 5: Brady et al proposed DLM ^{39,40,70}

No.	Reaction	log-K at 25°C
1.1	$>\text{RCOOH} \rightleftharpoons >\text{RCOO}^- + \text{H}^+$	-5.0
2.1	$>\text{NH}_2 \rightleftharpoons >\text{N} + \text{H}^+$	-6.0
3.1	$>\text{RCOOH} + \text{Ca}^{+2} \rightleftharpoons >\text{RCOOCa}^+ + \text{H}^+$	-3.8
4.1	$>\text{RCOOH} + \text{Mg}^{+2} \rightleftharpoons >\text{RCOOMg}^+ + \text{H}^+$	-4.0

619

620

621

622 3.1.3 Comparing the oil-brine TLM with existing TLMs

623 Another existing oil-brine SCM compared with our TLM is Takeya et al.³⁷ proposed TLM.
624 The authors measured oil-brine interface ζ -potential at 50°C using various brine, and also
625 modelled their experimental data with a TLM. However, they did not consider Na^+
626 adsorption and $>\text{NH}$ reactions in their model. On matching our TLM to the experimental ζ -
627 potential data, three scenarios were simulated: (a) both $>\text{NH}$ and Na^+ surface reactions
628 considered in the model, (b) only $>\text{NH}$ surface reactions omitted from the model, and (c)
629 only Na^+ surface reaction omitted from the model. We calculated acid site-density (4.19
630 sites/nm²) from the reported TAN (0.39 mgKOH/g oil), and base site-density (20 sites/nm²)
631 from the TBN (1.86 mgKOH/g oil). Takeya et al.³⁷ did not report brines and emulsion pH,
632 hence, we assumed brines pH of 7.0. Using our calculated capacitance values ($C1 = 2.84$; $C2$
633 $= 4.48 \text{ F/m}^2$), new oil-brine reactions constants were optimized (as this experiment was
634 conducted at 50°C) by matching the model to Takeya et al.³⁷ data sets. The optimized
635 equilibrium constants are given in Table 6 .

636

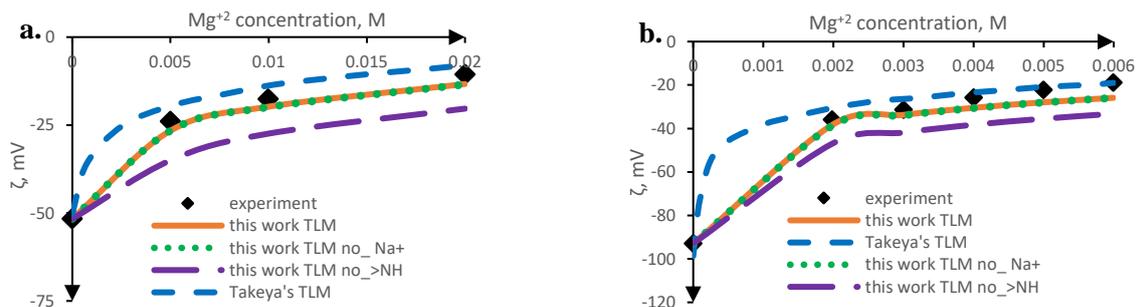
Table 6: oil-brine reaction constants at 50°C.

No.	Reaction	log-K at 50°C
1	$>\text{RCOOH} \rightleftharpoons >\text{RCOO}^- + \text{H}^+$	-4.5
2	$>\text{NH}_2 \rightleftharpoons >\text{N} + \text{H}^+$	3.5
3	$>\text{RCOOH} + \text{Na}^+ \rightleftharpoons >\text{RCOONa} + \text{H}^+$	-4.52
4	$>\text{RCOOH} + \text{Ca}^{+2} \rightleftharpoons >\text{RCOOCa}^+ + \text{H}^+$	-3.63
5	$>\text{RCOOH} + \text{Mg}^{+2} \rightleftharpoons >\text{RCOOMg}^+ + \text{H}^+$	-3.2

637

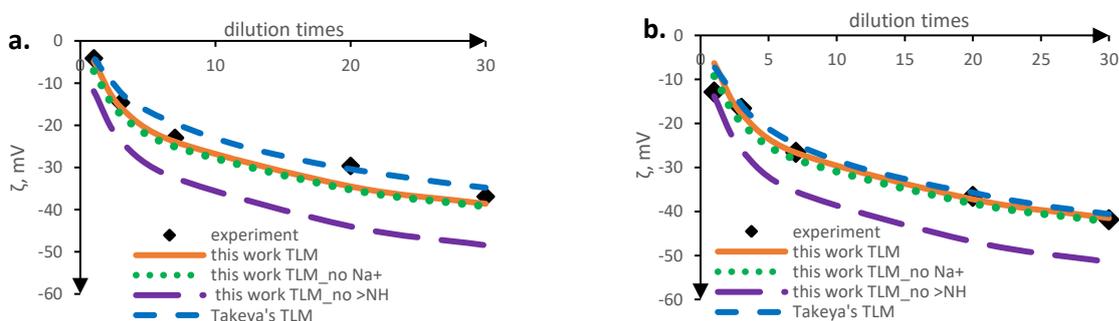
638 It can be observed that omitting Na^+ ion surface reaction from the model did not have any
639 impact on the ζ -potential results (Figures 10 and 11). On the other hand, $>\text{NH}$ omission
640 significantly affected the model ζ -potential results.

641



642

643 Figure 10: comparison of our oil-brine TLM to Takeya et al.³⁷ TLM. (a) measured ζ -potential at constant pH of
 644 7, and (b) measured ζ -potential at constant ionic strength of 20mM. “TLM_no Na⁺” denotes the model
 645 calculation where Na⁺ ion adsorption is omitted from the oil-brine interface reaction calculations. Likewise,
 646 “TLM_no >NH” is for >NH omission.



647

648 Figure 11: comparison of our oil-brine TLM to Takeya et al.³⁷ TLM. (a) seawater measured ζ -potential, and (b)
 649 formation water ζ -potential. “TLM_no Na⁺” denotes the model calculation where Na⁺ ion adsorption is omitted
 650 from the oil-brine interface reaction calculations. Likewise, “TLM_no >NH” is for >NH omission.

651 We further investigated this observation by calculating the oil-brine interface reactions at
 652 25°C. This time, we used our 25°C oil-brine reactions constants while maintaining all other
 653 parameters (i.e.: acid and base sites-densities; capacitances, brine properties). It should be
 654 noted that we compare only our model results since Takeya et al.³⁷ did not perform
 655 experiments at 25°C. It can be identified from Figure 12 that removal of both Na⁺ and >NH
 656 surface reactions reduced the calculated ζ -potential at 25°C, although, the magnitude is brine-
 657 related. Moreover, the impact of >NH surface reaction is greater than the effect of Na⁺. At
 658 50°C, kinetic energy of the species increases and the divalent ions having higher affinity to
 659 the surface, more of these ions reach the oil surface than Na⁺. Therefore, the obtained results
 660 for Na⁺ surface reaction at 25°C and 50°C can be related to temperature as removing Na⁺
 661 surface reactions at 50°C did not affect ζ -potential. Other influencing factor can be the
 662 dissociation of the carboxylic group with temperature.

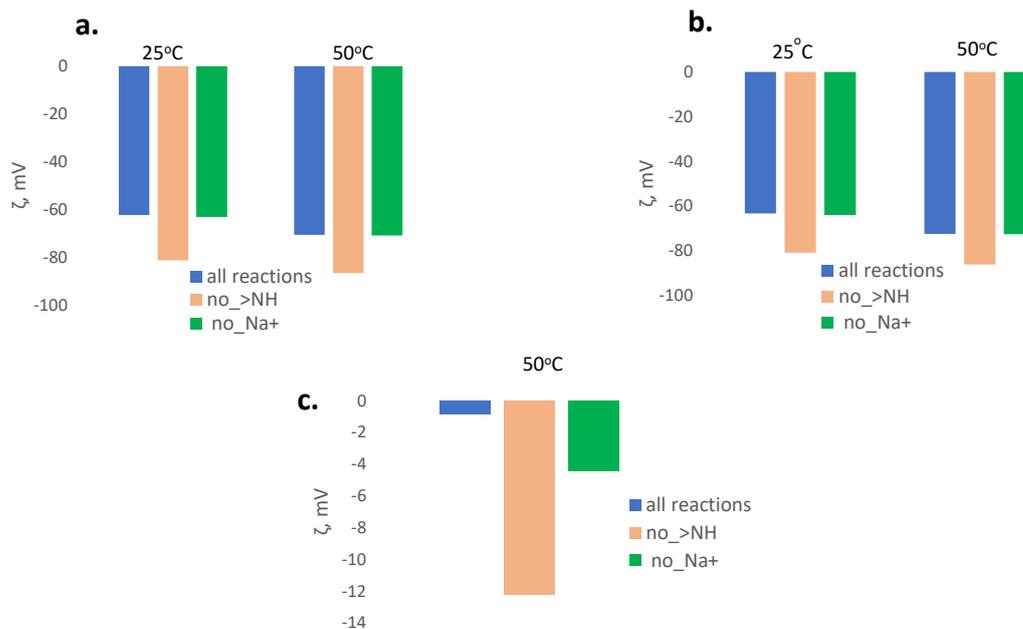


Figure 12: effects of >NH and Na⁺ surface reactions on oil-brine ζ -potential at 25°C.

663
664

665 The BN/AN ratio of the Takeya et al.³⁷ experimental oil is approximately 5.0, and we thought
 666 this might have contributed to the observed >NH ζ -potential results. We therefore employed
 667 Alshakhs & Kavscek⁹ experimental data we earlier matched our model to (Figure 5). This oil
 668 has BN/AN ratio of approximately 1.0, and we performed this calculation at 50°C and 25°C.
 669 It should be noted that we compare only our model results. We observed that omitting the
 670 Na⁺ surface reaction did not have any impact on the oil-brine interface ζ -potential at both
 671 50°C and 25°C, whereas >NH omission produced more negative ζ -potential (Figure 13a).
 672 This suggests that the observed >NH trend might not be related to BN/AN ratio. To confirm
 673 this, we used Alshakhs & Kavscek⁹ SW/1000 brine and Takeya et al.³⁷ oil properties, and
 674 calculated ζ -potential at 50°C and 25°C. Again, similar trend was observed (Figure 13b).
 675 Another ζ -potential data was computed from Takeya et al.³⁷ SW and Alshakhs & Kavscek⁹
 676 oil. This calculation was performed to study the relationship between ionic strength, brine
 677 composition and Na⁺ surface reactions. Unlike Alshakhs & Kavscek⁹ SW/1000 brine which
 678 is devoid of Ca⁺² and K⁺, Takeya et al.³⁷ SW contains these ions. Also, ionic strength of
 679 Alshakhs & Kavscek⁹ SW/1000 brine is 1.05 mM, whereas ionic strength of Takeya et al.³⁷
 680 SW is 0.782 M. We have already indicated that using the Alshakhs & Kavscek⁹ SW/1000
 681 brine with Takeya et al.³⁷ oil or Alshakhs & Kavscek⁹ oil, Na⁺ surface reaction did not
 682 contribute to ζ -potential. However, removal of Na⁺ surface reaction reduced the calculated ζ -
 683 potential from Takeya et al.³⁷ SW and Alshakhs & Kavscek⁹ oil (Figure 13c).

684



685

686

687 Figure 13: effects of Na^+ and $>\text{NH}$ surface reactions on oil-brine ζ -potential at different temperatures, oil and
 688 brine composition. (a) calculations from Alshakhs & Kovscek⁹ SW/1000 brine and oil properties; (b)
 689 calculations from Alshakhs & Kovscek⁹ SW/1000 brine and Takeya et al.³⁷ oil properties; (c) calculations from
 690 Takeya et al.³⁷ SW and Alshakhs & Kovscek⁹ oil properties.

691 It can be proposed from the model results that $>\text{NH}$ group significantly impacts oil-brine
 692 interface ζ -potential irrespective of temperature, brine composition, and ionic strength. On
 693 the other hand, Na^+ ion in brine may influence oil-brine ζ -potential, and this relates to
 694 temperature, brine composition, and ionic strength. Therefore, Takeya et al.³⁷ TLM being
 695 able to predict the experimental ζ -potential data could be related to the small acid site-density
 696 used by the authors. That is, they used acid site-density of 0.47sites/nm^2 , which we obtained
 697 4.19sites/nm^2 when calculated from the TAN. This implies reduced available carboxylic acid
 698 ($>\text{COOH}$ group) which would dissociate to produce negative ζ -potential values. Based on the
 699 above discussion, we suggest that $>\text{NH}$ group and Na^+ ion surface reactions can be included
 700 in oil-brine SCM as they can impact the calculated oil-brine ζ -potential.

701

702 3.2. Carbonate-brine interface ζ -potential

703 Like the oil-brine interface TLM, the carbonate-brine interface TLM was validated by
 704 matching the model to different cases of rock-brine experimental ζ -potential data. Moreover,
 705 the carbonate-brine TLM was compared with existing SCM.

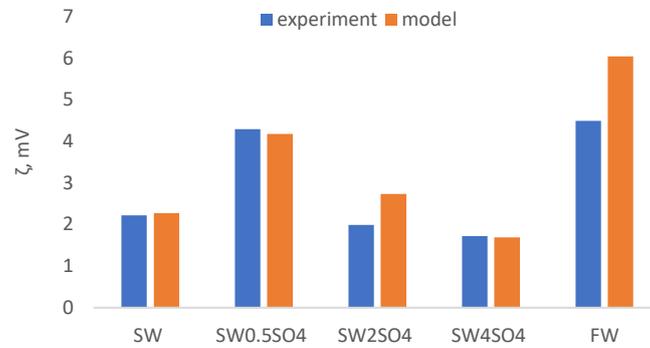
706 3.2.1. Comparing of rock-brine TLM with experimental cases

707 In this part, ζ -potentials of the rock-brine interface from three experimental cases were
 708 compared with the proposed TLM in this study, which is explained below:

709 *Case 1:*

710 We validated our carbonate-brine interactions model with experimental ζ -potential results
 711 reported by Awolayo et al.⁸² (Figure 14). In their experiment, the initial equilibrium state of
 712 formation brine (FW) in contact with carbonate mineral was modified by adding seawater
 713 brines (i.e.: SW, SW0.5SO₄, SW2SO₄, SW4SO₄). The numbers in the brines denote

714 concentration of SO_4 in the specific brine. For instance, SW2SO₄ signifies SW with twice
 715 SO_4 concentration. As we have indicated in the model description, we used 4.95 site/nm² for
 716 both calcium and carbonate sites. Moreover, we used $C1 = 2.84$ and $C2 = 4.48$ F/m². The
 717 rock-brine interface reactions constants were then optimized in matching the model to the
 718 experimental ζ -potential data. The equilibrium constant generated from our model match is
 719 given in Table 2 (i.e.: 25°C constants).



720
 721 Figure 14: comparison of the model (this study) and experimental data (Awolayo et al.⁸²) of rock-brine ζ -
 722 potential.

723 *Case 2:*

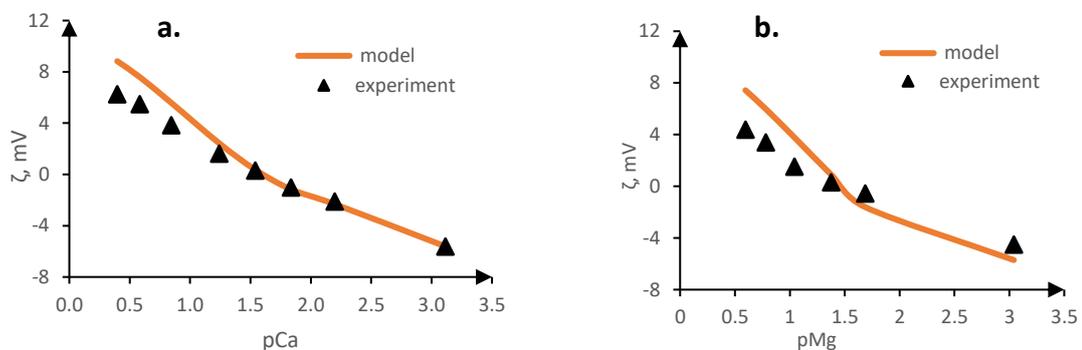
724 Our next match is ζ -potential results of Al Mahrouqi et al.²⁹ (Figure 15-17). The authors
 725 measured ζ -potential of Estailades rock with CaCl_2 , MgCl_2 or NaCl_2 brines. The optimized
 726 equilibrium constants we obtained from simulating Awolayo et al.⁸² experimental data was
 727 used to model Al Mahrouqi et al.²⁹ experimental results. Also, same values of site-density
 728 and capacitances were used.

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730

731

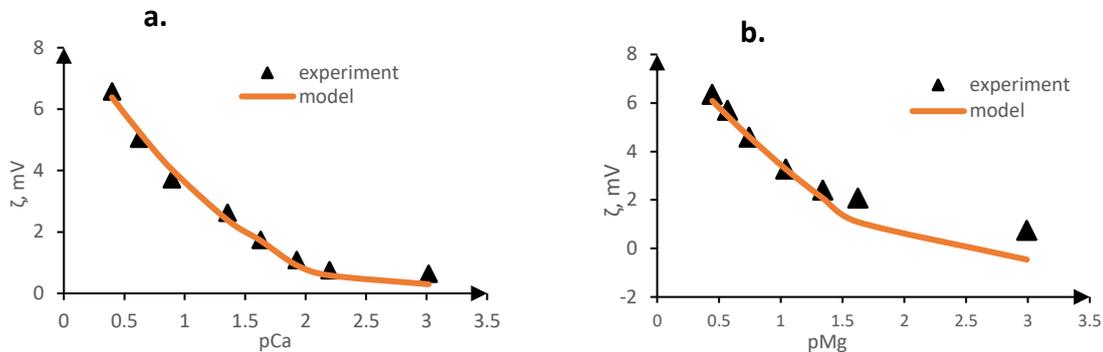
732



733
 734 Figure 15: comparison of the model (this study) and experimental data (Al Mahrouqi et al.²⁹) of rock-brine ζ -
 735 potential with various CaCl_2 and MgCl_2 brines. (a) CaCl_2 , and (b) MgCl_2 . Base electrolyte is 0.5M NaCl brine.

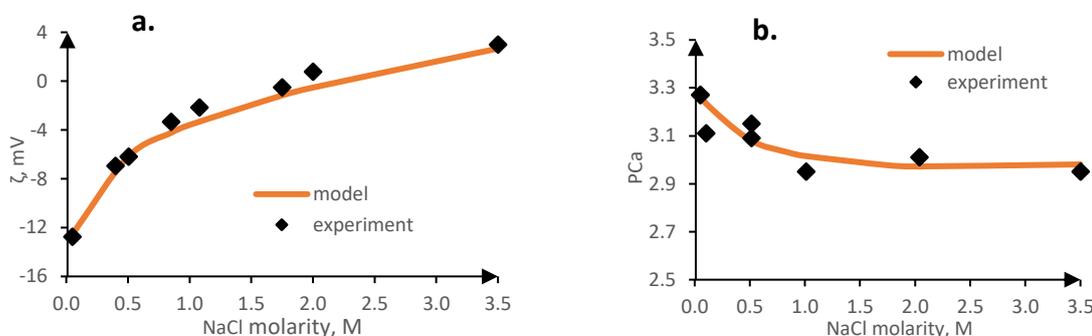
736 The authors indicated that initial equilibration of the carbonate rock with the NaCl brines
 737 produced approximately pH and pCa (i.e.: $-\log [\text{Ca}^{+2}]$) of 8.3 and 3.1 ± 0.1 , respectively. The

738 modelling results also produced approximately pH of 8.33 and pCa = 3.1 ± 0.1, after the
 739 initial equilibration with the NaCl brines.
 740



741
 742 Figure 16: comparison of the model (this study) and experimental data (Al Mahrouqi et al.²⁹) of rock-brine ζ -
 743 potential. (a) CaCl₂, and (b) MgCl₂. Base electrolyte is 2.0M NaCl brine.

744



745
 746 Figure 17: comparison of the model (this study) and experimental data (Al Mahrouqi et al.²⁹) of rock-brine ζ -
 747 potential with various NaCl concentrations. (a) ζ -potential, and (b) equilibrium pCa during the rock-NaCl
 748 brines equilibration process.

749 *Case 3:*

750 Figure 18 shows our model provides a good match with Lu et al.⁸⁰ carbonate-brine interface
 751 ζ -potential data measured at 25°C and 65°C. Here also, we used C1 = 2.84 F/m², C2 = 4.84
 752 F/m² and site-density = 4.95 sites/nm² for each site. Regarding the 25°C temperature, we used
 753 our optimized rock-brine equilibrium constants generated from the previous match (Awolayo
 754 et al.⁸² matched equilibrium constants), while new equilibrium constants were optimized for
 755 the 65°C (Table 7) by matching the model to Lu et al.⁸⁰ 65°C experimental data.

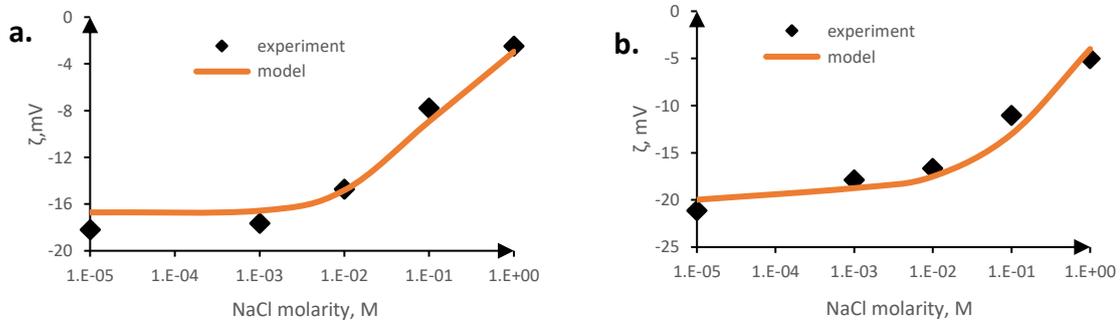
756

Table 7: rock-brine reaction constants at 65C.

No.	Reaction	log-K at 60°C
6	$>CaOH^{-0.75} + H^+ \Leftrightarrow >CaOH_2^{+0.25}$	10.82
7	$>CaOH^{-0.75} + CO_3^{2-} \Leftrightarrow >CaCO_3^{-1.75} + OH^-$	1.35
8	$>CaOH^{-0.75} + SO_4^{2-} \Leftrightarrow >CaSO_4^{-1.75} + OH^-$	2.86
9	$>CaOH_2^{+0.25} + Cl^- \Leftrightarrow >CaOH_2^{+0.25} \dots Cl^-$	-3.35
10	$>CO_3H^{+0.75} \Leftrightarrow >CO_3^{-0.25} + H^+$	-3.0

11	$>\text{CO}_3\text{H}^{+0.75} + \text{Ca}^{+2} \Leftrightarrow >\text{CO}_3\text{Ca}^{+1.75} + \text{H}^+$	-2.35
12	$>\text{CO}_3\text{H}^{+0.75} + \text{Mg}^{+2} \Leftrightarrow >\text{CO}_3\text{Mg}^{+1.75} + \text{H}^+$	-2.15
13	$>\text{CO}_3^{-0.25} + \text{Na}^+ \Leftrightarrow >\text{CO}_3^{-0.25}\cdots\text{Na}^+$	-2.1

757

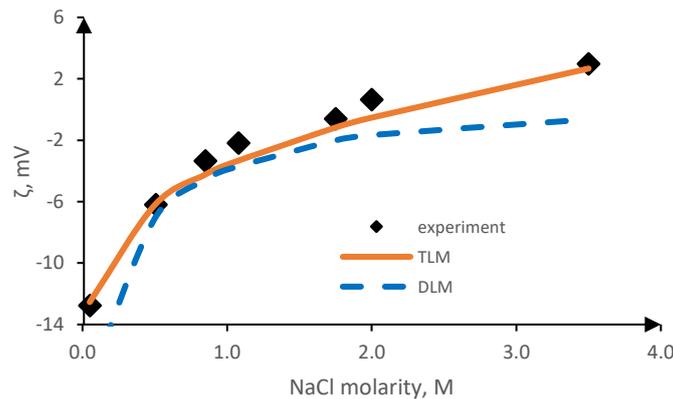


758

759 Figure 18: comparison of the model (this study) and experimental data (Lu et al.⁸⁰) of rock-brine interface ζ -
760 potential with various NaCl concentrations. (a) 25°C measured ζ -potential; (b) 65°C ζ -potential measured

761 **3.2.2. Comparing the rock-brine TLM with DLM**

762 Finally, we compared our proposed TLM with the DLM developed by Brady et al.⁴⁰. ζ -
763 potential was estimated from the DLM surface potential using the Gouy-Chapmann relation
764 (equation 20) (Israelachvili.⁵³). The result shows that the TLM calculated ζ -potential matches
765 the experimental data better than the DLM ζ -potential (Figure 19). As we indicated in the oil-
766 brine TLM versus DLM model, TLM estimates ζ -potential directly, therefore, no need to
767 introduce any correlation. The experimental results of Al Mahrouqi et al.²⁹ was used for the
768 simulation. We did not compare our TLM with the few available carbonate-brine TLM
769 because the assumptions and parameters used in those models do not differ much from this
770 work. Hence, we do not expect much difference in the simulation results.



771

772 Figure 19: results of rock-brine ζ -potential calculated with our TLM and DLM proposed by Brady et al.⁴⁰

773 **3.3. UTCHEM-PHREEQCRM model validation with PHREEQC**

774 We validated our coupled UTCHEM-PHREEQCRM model using example 11 supplied with
775 the PHREEQC software package^{75,83}. The problem consists of a column containing sodium-
776 potassium-nitrate solution in equilibrium with exchanger. The column, having 40 cells (grid
777 size, $\Delta x = 0.002\text{m}$), is then flushed with CaCl_2 solution and effluent ions concentrations were
778 retrieved. We simulated both the dispersion-free and advective-dispersive transport data with

779 our model and PHREEQC software, and matched PHREEQC effluent ions with our model
 780 (Figure 20). The advective-dispersive case has Peclet number, Pe of 40 and dispersivity, α_L
 781 of 0.002m. It should be noted that numerical dispersion in PHREEQC is negligible when
 782 $\Delta x \leq \alpha_L$ (Parkhurst & Appelo.⁷⁵). Therefore, to obtain identical Pe between UTCHEM and
 783 PHREEQC, we adopted Equation 23 reported by Korrani et al^{43,84}.

784

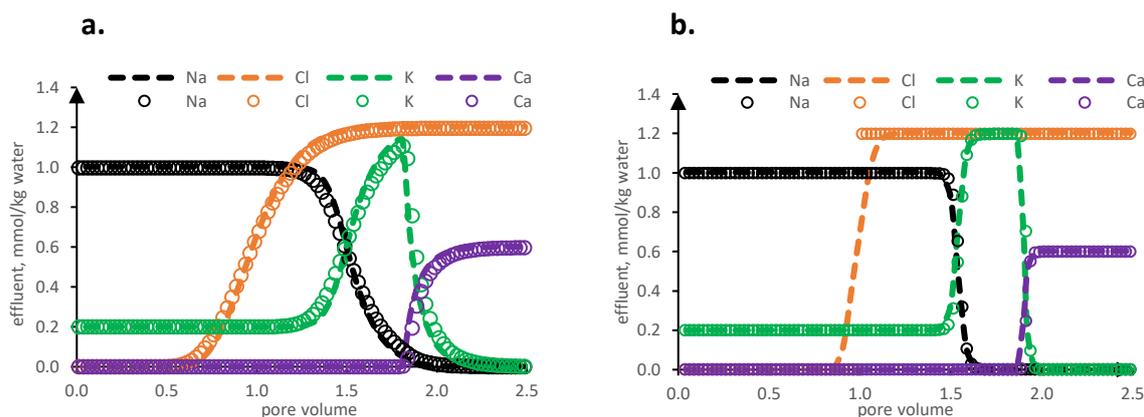
$$785 \left(\frac{N\Delta x}{\alpha_{physical} + \frac{\Delta x}{2}} \right)_{UTCHEM_PHREEQCRM} = \left(\frac{N\Delta x}{\alpha_{physical}} \right)_{PHREEQC} \quad (24)$$

786

787 N = total number of cells.

788

789



790

791 Figure 20: UTCHEM-PHREEQCRM validation with PHREEQC example 11 (Parkhurst & Appelo^{75,83}). (a)
 792 advective-dispersive results; (b) advective results. Markers denote PHREEQC results and dashes are UTCHEM-
 793 PHREEQCRM results.

794

795 3.4. UTCHEM-PHREEQCRM model validation with experimental CSWF data

796 This section presents the simulation results of our UTCHEM-PHREEQCRM model matched
 797 with the experimental CSWF data sets. Relative permeability curves are usually measured in
 798 the laboratory at the end-point wettability states. However, the CSWF experiments that are
 799 simulated in this study did not report relative permeability and capillary pressure curves.
 800 Therefore, relative permeability curves at the end points were estimated from the best fit to
 801 the experimental oil recoveries. In other word, relative permeabilities were tuned to match the
 802 model calculated oil recoveries to the experimental oil recoveries. Capillary pressure was also
 803 assumed to be zero in order to reduce the number of tuning parameters.

804

805 3.4.1. Modelling of Fathi et al.¹³ CSWF experiment

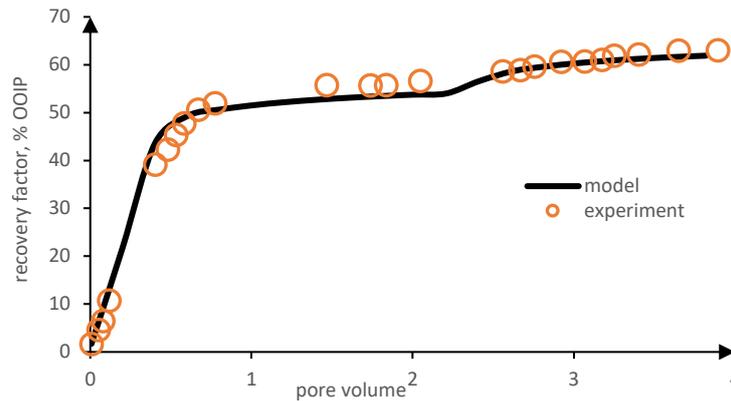
806 The proposed model was used to simulate core flooding results of Fathi et al¹³ (Figure 21).
 807 They performed tertiary CSWF by injecting FW at secondary stage and SW at tertiary stage.
 808 Secondary injection of FW recovered 56% of original oil in place (OOIP) and was increased
 809 to 63% following the SW injection. Like our previous matches, we used same capacitances,
 810 rock site-densities, but calculated the oil acid site-density (20.4/nm²). Fathi et al¹³ did not
 811 report TBN, hence, we assumed a base site-density of 20.4/nm², which is equivalent to the
 812 acid site-density. Therefore, relative permeability parameters (end-point relative permeability
 813 and Corey's exponents) were optimized to match the model to the oil recovery. The
 814 optimized relative permeabilities used to predict the results are shown by Table 8.

815

Table 8: relative permeability parameters used to simulate Fathi et al¹³ experiment

parameter	Initial value	Final value
Swc	0.08	0.08
Sor	0.4	0.34
Krow	0.5	0.5
Krw	0.2	0.2
nw	2	3
no	3	2.5

816

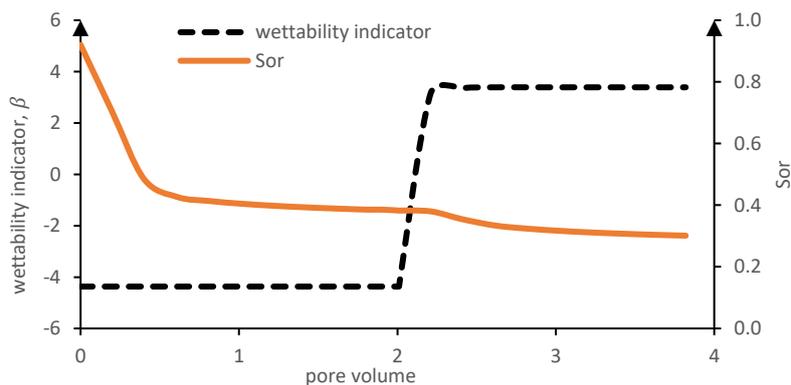


817

818

Figure 21: comparison of model (this study) to experimental data (Fathi et al¹³) of oil recovery data

819 The model calculated wettability indicator shows a shift in the wettability indicator value on
 820 switching the injection brine from FW to SW (Figure 22). That is, FW injection produced
 821 wettability indicator of -4.37, while switching the injection brine to SW increased the value to
 822 3.39. This implies increased electrostatic repulsive force between the oil and the rock surface,
 823 and thus, decreased oil adhesion. Consequently, a shift in the wettability from oil-wet towards
 824 water-wet behavior is obtained. There is further reduction in residual oil saturation (Sor)
 825 following SW injection. It can be suggested from the magnitude of the wettability indicator
 826 that wettability was shifted from weakly oil-wet to weakly water-wet.



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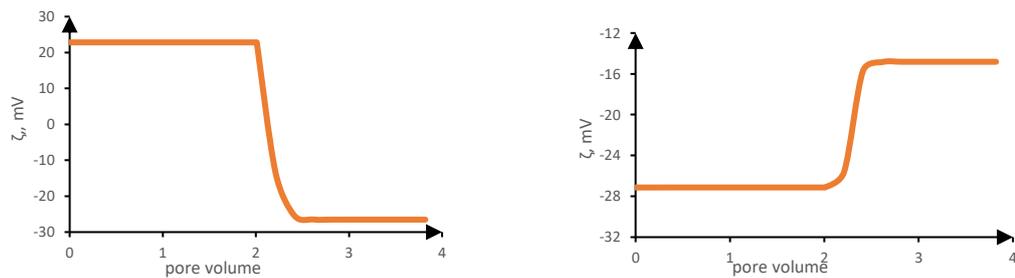
Figure 22: relationship between wettability indicator and residual oil saturation for the brine injections. FW injection produced wettability indicator of about -4.37. During this period, 56% of OOIP was recovered. Switching the injection brine to SW generated wettability indicator of about 3.39. Accordingly, additional 7% OOIP was produced.

832

833

ζ -potential of the rock-brine (Figure 23a) and the oil-brine (Figure 23b) interface shows that the two interfaces have opposite ζ -potential during the FW injection. Nonetheless, switching

834 the injection brine to SW shifted the oil-brine ζ -potential towards positive, although, it
 835 remained within negative values. It should be noted that concentration of Mg^{+2} ion in the SW
 836 is about six times the Mg^{+2} concentration in the FW. This increased the Mg^{+2} ions in the
 837 brine, shifting the reaction: $>RCOOH + Mg^{+2} \rightleftharpoons >RCOOMg^+ + H^+$ to right. The adsorbed
 838 Mg^{+2} species at the oil-brine interface is then increased, and the oil-brine ζ -potential is thus,
 839 shifted towards positive (Figure 23b). At the same time, the rock-brine ζ -potential shifted to
 840 negative values. Unlike the FW, the injected SW contains SO_4^{-2} ion and some past papers
 841 argue that adsorption of SO_4^{-2} shifts carbonate ζ -potential to negative values^{16,82,85}. It can be
 842 suggested that SO_4^{-2} -rich brine with high Mg^{+2} content may sometimes be detrimental to
 843 CSWF depending on its generated oil-brine ζ -potential.

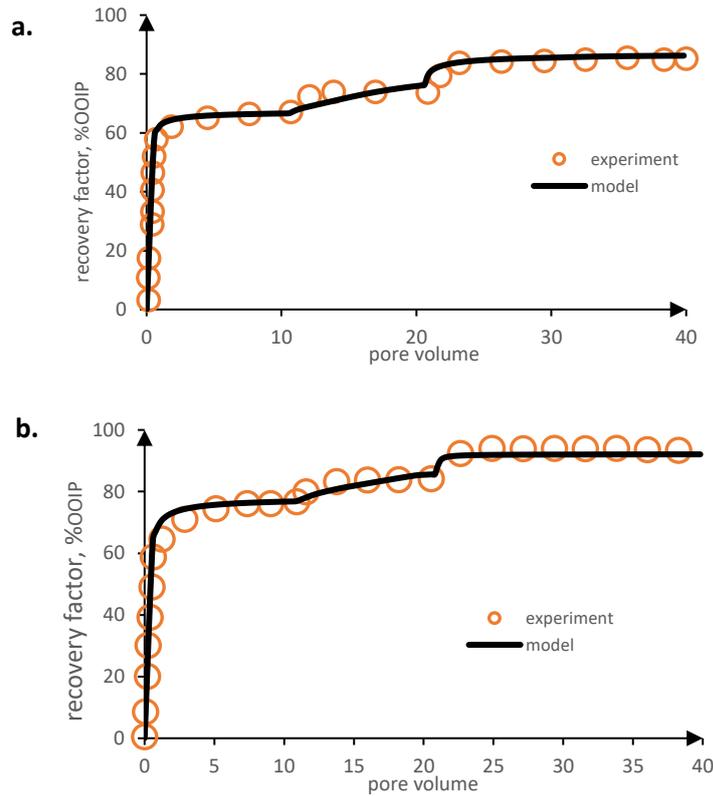


844
 845 Figure 23: calculated ζ -potential for COB system. (a) rock-brine ζ -potential, and (b) oil-brine ζ -potential.

846 3.4.2. Modelling of Yousef et al.⁷⁸ CSWF experiments

847 Yousef and co-workers conducted tertiary CSWF with limestone using series of diluted sea
 848 water. The carbonate rock was reported to compose of calcite, dolomite and anhydrite
 849 (Yousef et al⁸⁶). The authors injected SW at secondary stage, followed by successive
 850 injections of two-diluted SW (SW/2); ten-diluted SW (SW/10); twenty-diluted SW (SW/20);
 851 hundred-diluted SW (SW/100). The SW/100, however, did not recover additional oil. We
 852 simulated their oil recovery with our model and the result is shown by Figure 24.

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Figure 24: history match of model (this study) to Yousef et al⁷⁸ oil recovery data. (a) first Core flood match, and (b) second core flood match.

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We calculated acid site-density of 2.69/nm² from the TAN (0.25 mgKOH/g oil) and assumed same for base site-density since TBN was not reported. Using our capacitances and carbonate site-density values, relative permeability was optimized to match the model to the experimental oil recoveries. The optimized relative permeabilities used to predict the results are shown by Table 9.

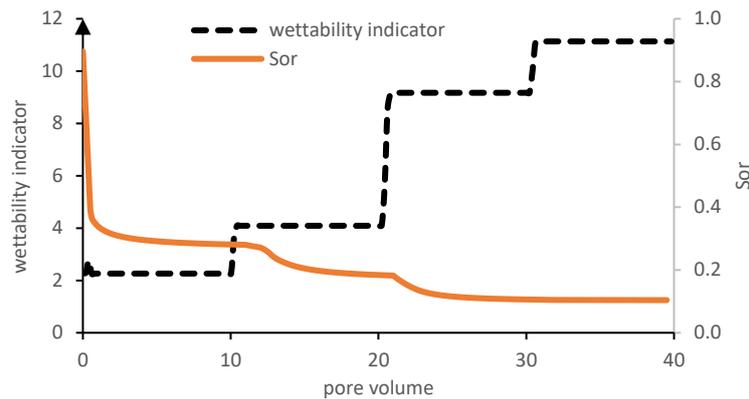
864

Table 9: relative permeability parameters used to simulate Yousef et al⁷⁸ experiments

parameter	Initial value	Final value
1 st core flood		
Swc	0.1044	0.1044
Sor	0.33	0.12
Krow	0.8	0.8
Krw	0.5	0.2
nw	2	3
no	2.2	2
2 nd core flood		
Swc	0.144	0.144
Sor	0.21	0.08
Krow	0.8	0.8
Krw	0.5	0.2
nw	2	3
no	2.2	2

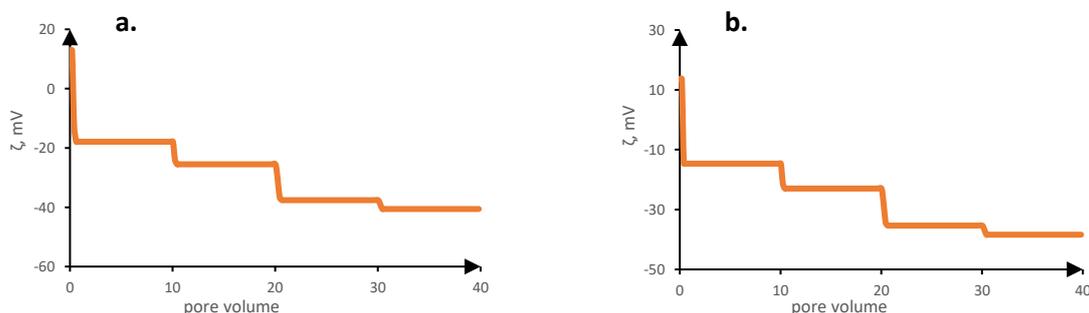
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866 Figure 25 shows that decreasing salinity of the injection brine increased the calculated
 867 wettability indicator (becoming more positive), and shifted the wettability towards water-wet
 868 state. It can be observed that the wettability indicator is much increased when the injection
 869 brine was switched from SW/2 to SW/10 compared with switching from SW to SW/2. This
 870 observation is consistent with the reported oil recovery as SW/2 injection recovered
 871 additional 7% OOIP, whereas SW/10 injection produced additional 9.12% OOIP. Injection of
 872 the SW/20 further increased the wettability indicator although no significant oil was
 873 recovered. It can be suggested that much of the movable oil was retrieved with the earlier
 874 injected brines.



875
 876 Figure 25: relationship between wettability indicator and residual oil saturation for the various injection cycles
 877 (1st core flood).

878 It can be observed from Figure 26 that the calculated ζ -potentials are positive at the initial
 879 condition, which shifted to negative values during SW injection. The rock-brine ζ -potential
 880 can be seen to be continuously becoming negative as the diluted brines are injected. During
 881 the same injection period, the oil-brine interface also generates negative ζ -potential. This is in
 882 consistent with the results reported by the authors in another published paper (Yousef et al⁸⁶).
 883 They reported negative ζ -potential at the rock-brine interface when the rock was equilibrated
 884 with SW. The ζ -potential then becomes more negative when the SW was diluted ten times,
 885 twenty times, and hundred times.



886
 887 Figure 26: calculated ζ -potential for the COB system. (a) rock-brine ζ -potential, and (b) oil-brine ζ -potential
 888 (Yousef et al⁷⁸ 1st core flood).

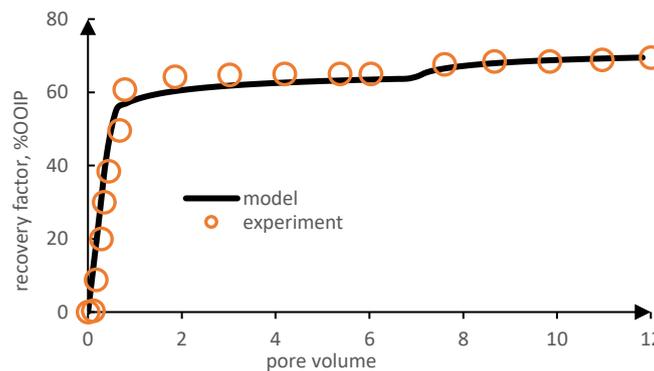
889 3.4.3. Modelling of Austad et al.⁷ CSWF experiments

890 Austad et al.⁷ performed tertiary CSWF in limestone and chalk by injecting FW at secondary
 891 stage followed by FW/100 injection. It should be noted that both brines used for the
 892 experiment were devoid of SO_4^{2-} ion. Injection of FW through the limestone core produced

893 65% OOIP, which was increased to 70% OOIP on switching to FW/100. The chalk, on the
 894 other hand, recovered 57% OOIP, and switching the injection brine to FW/100 did not
 895 recover any additional oil. Austad and colleagues explained that dissolution of anhydrite
 896 mineral present in the limestone provided SO_4^{-2} ion, and adsorption of this ion at the rock
 897 surface increased oil recovery. They further proposed that the adsorbed SO_4^{-2} co-adsorbed
 898 Ca^{+2} and Mg^{+2} leading to the release of adhered oil from the rock surface. We modelled the
 899 oil recovery data obtained from the limestone rock with our model (Figure 27). However,
 900 regarding the chalk, we qualitatively calculated adhesion number and used it to analyse
 901 Austad et al.⁷ observations. It is important to note that in simulating the limestone rock,
 902 calcite and anhydrite dissolution/precipitation reactions were included in the model while
 903 only calcite dissolution/precipitation reaction was involved in the chalk rock. Acid site-
 904 density ($7.52/\text{nm}^2$) and base site-density ($4.51/\text{nm}^2$) were calculated from the TAN (0.7
 905 mgKOH/g oil) and TBN (0.42 mgKOH/g oil), respectively. We used our capacitances ($C1 =$
 906 2.84 , $C1 = 4.48 \text{ F/m}^2$) and carbonate site-densities ($4.95/\text{nm}^2$ for each site) that are used
 907 entirely in this paper. Therefore, relative permeability parameters were optimized to match
 908 the model to the limestone oil recovery data. The optimized relative permeabilities used to
 909 predict the results are shown by Table 10.

910
 911 Table 10: relative permeability parameters used to simulate Austad et al.⁷ limestone experiment

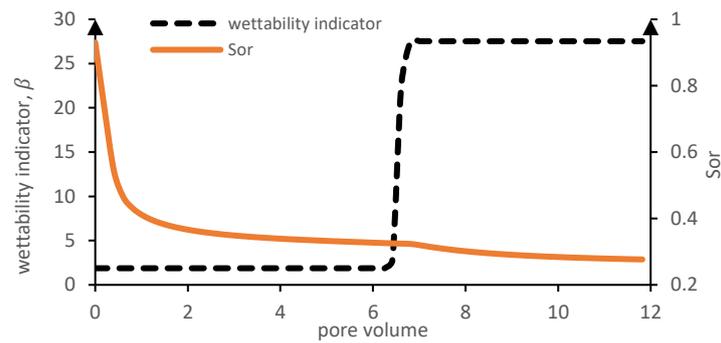
parameter	Initial value	Final value
Swc	0.07	0.07
Sor	0.32	0.28
Krow	0.6	0.6
Krw	0.2	0.2
nw	2	3
no	3	2.5



914
 915 Figure 27: history match of model (this study) to Austad et al.⁷ oil recovery data (limestone core).

916 Figure 28 shows the relationship between the calculated wettability indicator and the residual
 917 oil saturation for the limestone rock. The wettability indicator for the FW injection is 1.88,
 918 which can be described as weakly water-wet condition. Injection of FW/100 shifted the
 919 wettability towards more water-wet state with calculated wettability indicator of 27.5. This
 920 increased the oil recovery in the FW/100 injection cycle. Residual oil saturation is observed
 921 to reduce further on switching the injection brine to FW/100 brine.

922

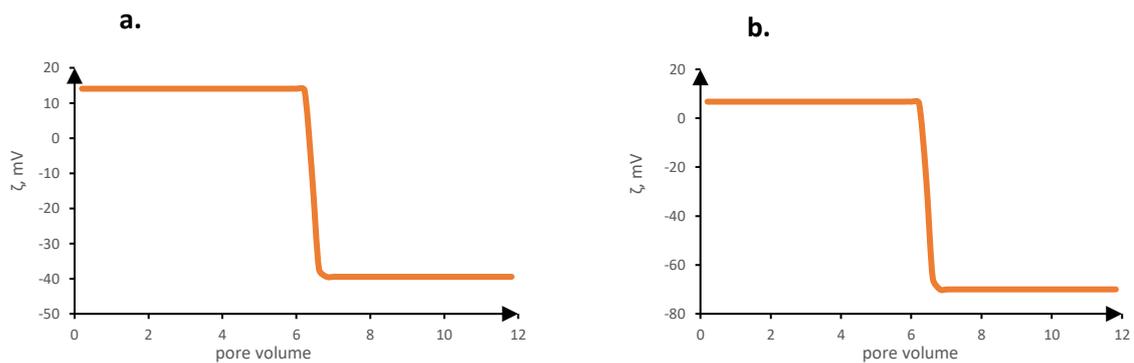


923

924 Figure 28: model results of calculated wettability indicator versus residual oil saturation (Austad et al.⁷;
925 limestone).

926 The model shows positive ζ -potentials calculated at the oil-brine and the rock-brine interfaces
927 during FW injection. However, switching the injection brine to FW/100 produced negative ζ -
928 potentials at both oil-brine and rock-brine interfaces (Figure 29). It can be observed that
929 magnitude of the FW/100 calculated ζ -potentials exceeded FW produced ζ -potentials,
930 generating high repulsive force between the oil and the rock surface. This can be attributed to
931 the additional oil recovered with the FW/100 injection.

932



933

934 Figure 29: calculated ζ -potential for the COB system. (a) rock-brine ζ -potential; and (b) oil-brine ζ -potential
935 (Austad et al.⁷; limestone rock).

936 Figure 30 shows the effluent SO_4^{-2} ion concentration during the injection cycle. Both the
937 connate water and the injection brines were devoid of SO_4^{-2} ion, therefore, the produced SO_4^{-2}
938 ion was as a result of anhydrite dissolution. The SO_4^{-2} ion also indicates the amount of
939 dissolved anhydrite. The produced SO_4^{-2} ion concentration is observed to increase when the
940 injection brine was switched to the FW/100 brine, signifying increased anhydrite dissolution.
941 Consequently, the adsorbed SO_4^{-2} ion at the rock surface would increase, shifting the ζ -
942 potential to negative values. The anhydrite dissolution, however, occurred within 1 pore
943 volumes of injection after which equilibrium between the aqueous ions and the mineral was
944 established.

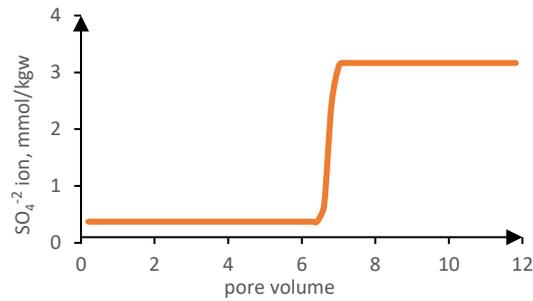
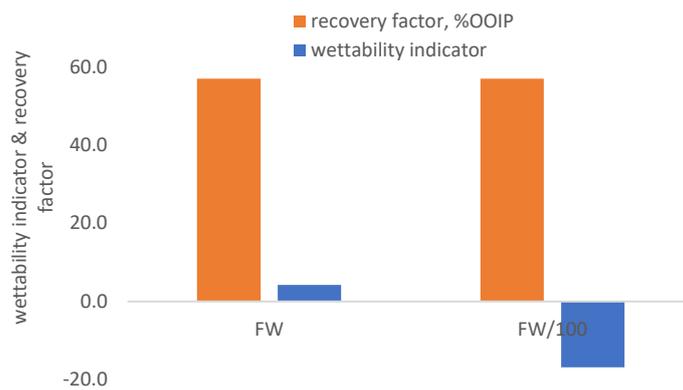


Figure 30: effluent SO_4^{2-} ion

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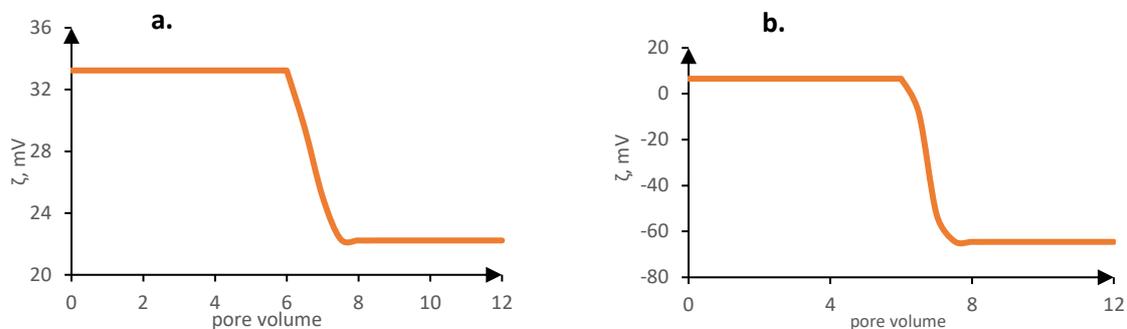
947 Figure 31 below shows qualitative results of the calculated wettability indicator for the chalk
 948 core at the end of each injection period. It can be observed that the wettability indicator at the
 949 end of FW injection is 4.23, which reduced to -16.8 following FW/100 injection. This implies
 950 increased electrostatic attraction force between the oil and the rock surface, and thus,
 951 increased oil adhesion. The authors did not observe additional oil recovery from the FW/100
 952 injection, which can be linked to the increased oil adhesion as observed from the model. They
 953 stated that carbonates without SO_4^{2-} (as anhydrite mineral, initially contained in the rock), do
 954 not show increased oil recovery with dilution, and this is exactly what the model predicted.



955
956

Figure 31: relationship between adhesion number and residual oil saturation (Austad et al.⁷; chalk core).

957 The calculated ζ -potential for the chalk shows positive ζ -potentials at both oil-brine and rock-
 958 brine interfaces during FW injection. Switching the injection brine to FW/100 produced
 959 negative ζ -potential at the oil-brine interface, whereas the rock-brine interface still produced
 960 positive ζ -potential values (Figure 32).



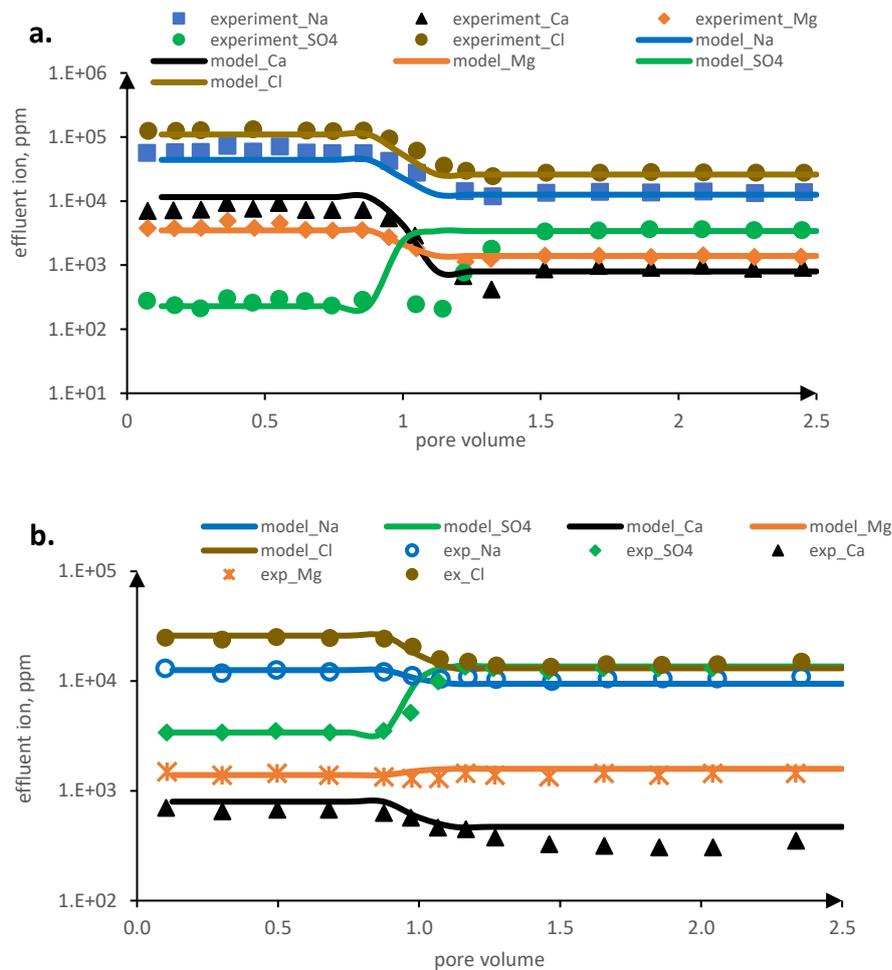
961

962 Figure 32: calculated ζ -potential for the COB system. (a) rock-brine ζ -potential; and (b) oil-brine ζ -potential
 963 (Austad et al.⁷; chalk core).

964 **3.4.4. Modelling of Sharma & Mohanty.⁷⁹ experiments**

965 We also modelled single-phase CSWF results of Sharma & Mohanty⁷⁹. In their experiment,
 966 FW was first displaced by SW, which was also displaced by SW4SO4 (i.e.: SW with SO₄⁻²
 967 ion concentration increased four times). We matched the model to the experimental effluent
 968 ion concentrations (Figure 33). The experiment was conducted at 120°C; therefore, we
 969 optimized the carbonate-brine reactions constants while maintaining capacitances and site-
 970 densities values. The obtained equilibrium constants are given in Table 2.

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975 Figure 33: Effluent ion match. (a) SW displacing FW; (b) SW4SO4 displacing SW

976 **4. Conclusions**

977 We presented a triple-layer surface complexation model to characterize carbonate-brine-oil
 978 interactions. A wettability indicator based on the ζ -potentials was suggested to offer
 979 wettability alteration resulting from brine dilution and/or composition. The developed model
 980 was tested against several experimentally measured ζ -potentials and oil recovery data sets.
 981 The model offers promising results when used at various conditions of temperature,
 982 carbonate mineralogy, brine composition and salinity. Results of the model suggest that:

- 983 • Oil basic group significantly impacts oil-brine interface ζ -potential irrespective of
 984 temperature, brine composition, and ionic strength.

- 985 • Na⁺ ions in brine may influence oil-brine ζ-potential, and this relates to temperature,
986 brine composition, and ionic strength.
- 987 • Dilutions in chalk tend to shift the reservoir towards oil-wet condition.
- 988 • Wettability is related to ζ-potentials at the oil-brine and rock-brine interfaces, and
989 carbonate rock would be strongly oil-wet or water-wet only at significantly large
990 magnitude of ζ-potentials at the interfaces.

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